

**SF3674 DIFFERENTIAL GEOMETRY,  
GRADUATE COURSE, FALL 2016,  
READING INSTRUCTIONS AND EXERCISES**

MATTIAS DAHL, HANS RINGSTRÖM

LECTURE 6, TUESDAY OCTOBER 11

**Reading instructions.** The sixth lecture was an overview of homogeneous spaces, symmetric spaces, and the holonomy of a Riemannian manifold. The contents roughly corresponds to:

- Lie groups, basics, [3, Appendix B, pp. 446-452].
- Killing fields, the isometry group of a Riemannian manifold as a Lie group, homogeneous spaces, [3, Chapter 9, pp. 249-262].
- Symmetric spaces [4, Chapter 10.1-10.2] (but not the details of the Lie algebra description in Section 10.1.3).
- Holonomy [4, Chapter 10.3]

Symmetric spaces are also treated in [3, Chapter 11]. Further reading on holonomy can be found in [1] and [2].

**Exercises.**

- (1) O'Neill [3] problems 9.14, 9.15 (p. 260).
- (2) Petersen [4] exercises 10.5.1, 10.5.2, 10.5.9, 10.5.11, 10.5.13 (pp. 392-393).

REFERENCES

- [1] Robert Bryant. Recent advances in the theory of holonomy. *Astérisque*, (266):Exp. No. 861, 5, 351–374, 2000. Séminaire Bourbaki, Vol. 1998/99.
- [2] Dominic D. Joyce. *Riemannian holonomy groups and calibrated geometry*, volume 12 of *Oxford Graduate Texts in Mathematics*. Oxford University Press, Oxford, 2007.
- [3] Barrett O'Neill. *Semi-Riemannian geometry*, volume 103 of *Pure and Applied Mathematics*. Academic Press, Inc. [Harcourt Brace Jovanovich, Publishers], New York, 1983. With applications to relativity.
- [4] Peter Petersen. *Riemannian geometry*, volume 171 of *Graduate Texts in Mathematics*. Springer, Cham, third edition, 2016. URL: <http://dx.doi.org/10.1007/978-3-319-26654-1>, doi:10.1007/978-3-319-26654-1.