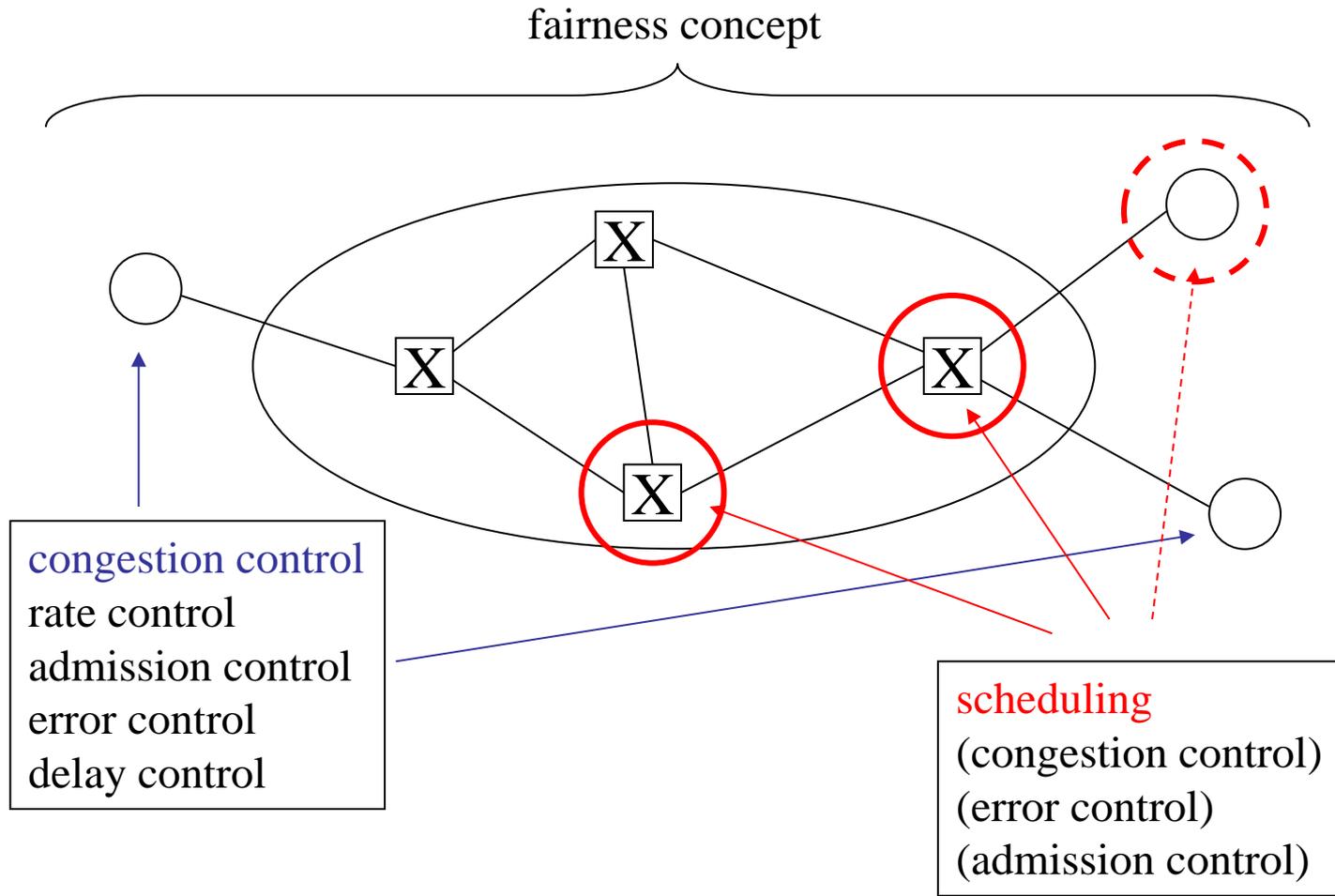


# EP2210

## Scheduling

- Lecture material:
  - Bertsekas, Gallager, 6.1.2.
  - MIT OpenCourseWare, 6.829
  - A. Parekh, R. Gallager, "A generalized Processor Sharing Approach to Flow Control - The Single Node Case," IEEE Infocom 1992

# Scheduling



# Scheduling - Problem definition

- Scheduling happens at the routers (switches) – or at user nodes if there are many simultaneous connections
  - many flows transmitted simultaneously at an output link
  - packets waiting for transmission are buffered
- Question: which packet to send, and when?
- Simplest case: FIFO
  - packets of all flows stored in the same buffer in arrival order
  - first packet in the buffer transmitted when the previous transmission is complete
  - packet transmission in the order of packet arrival
  - packet arriving when buffer is full dropped
- Complex cases: separate queues for flows (or set of flows)
  - one of the first packets in the queues transmitted
  - according to some policy
  - needs separate queues and policy specific variable for each flow
    - PER FLOW STATE

# Scheduling - Requirements

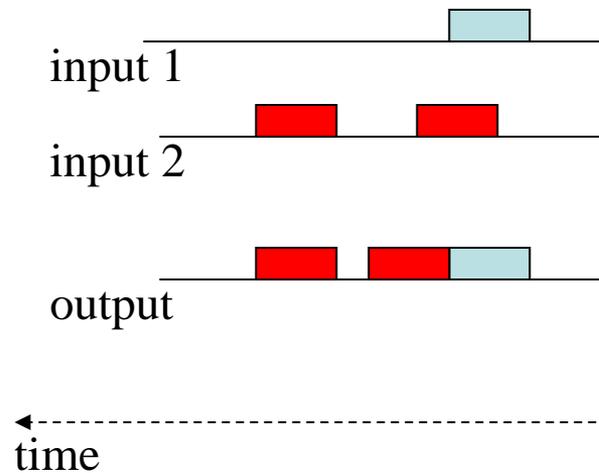
- Fair bandwidth allocation
  - for elastic (or best effort) traffic
  - all competing flows receive the some “fair” amount of resources
- Provide performance guarantees for flows or aggregates
  - service provisioning in the Internet (guaranteed service per flow)
  - guaranteed bandwidth for SLA, MPLS, VPN (guaranteed service for aggregates)
  - integrated services in mobile networks (UMTS, 4G)
- Performance guarantees
  - throughput, delay, delay variation, packet loss probability
  - performance guarantees should be de-coupled (coupled e.g., high throughput -> low delay variation)
- Easy implementation
  - has to operate on a per packet basis at high speed routers

# Scheduling – Implementation issues

- Scheduling discipline has to make a decision before each packet transmission – every few microseconds
- Decision complexity should increase slower than linearly with the number of flows scheduled
  - e.g., complexity of FIFO is 1
  - scheduling where all flows have to be compared scales at least linearly
- Information to be stored and managed should scale with the number of flows
  - e.g., with per flow state requirement it scales at least linearly (e.g., queue length or packet arrival time)
- Scheduling disciplines make different trade-off among the requirements on fairness, performance provisioning and complexity
  - e.g., FIFO has low complexity, but can not provide fair bandwidth share for flows

# Scheduling classes

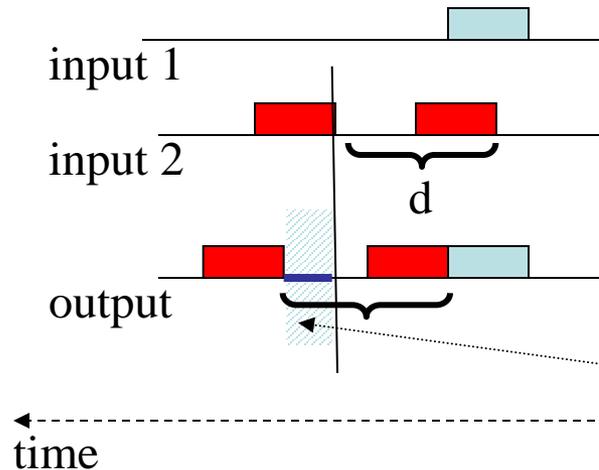
- Work-conserving
  - server (output link) is never idle when there is packet waiting



- utilizes output bandwidth efficiently
- burstiness of flows may increase → loss probability at the network nodes on the transmission path increases
- latency variations at each switch → may disturb delay sensitive traffic

# Scheduling classes

- Nonwork-conserving
  - add rate control for each flow
  - each packet assigned an eligibility time when it can be transmitted
    - e.g, based on minimum  $d$  gap between packets
  - server can be idle if no packet is eligible



server idle, while packet waiting from input 2

- burstiness and delay variations are controlled
- some bandwidth is lost
- can be useful for transmission with service guarantees.

# Scheduling for fairness

- The goal is to share the bandwidth among the flows in a “fair” way
  - fairness can be defined a number of ways (see lectures later)
  - here fairness is considered for one single link, not for the whole transmission path
- Max-min fairness
  - *Maximize* the *minimum* bandwidth provided to any flow not receiving all bandwidth it requests
  - E.g.: no maximum requirement, single node – the flows should receive the same bandwidth
  - Specific cases: weighted flows and maximum requirements

# Max-min fairness

- *Maximize the minimum* bandwidth provided to any flow not receiving all bandwidth it requests

C: link capacity

B(t): set of flows with data to transmit at time t  
(backlogged (saturated) flows)

n(t): number of backlogged flows at time t

$C_i(t)$ : bandwidth received by flow i at time t

**Case: without weights or max. requirements**

$$C_i(t) = \frac{C}{n(t)}$$

**Case: weights**

$w_i$ : relative weight of flow i

$$C_i(t) = \frac{w_i}{\sum_{j \in B(t)} w_j} C$$

**Case: max. requirements**

$r_i$ : max. bandwidth requirement for flow i

$\alpha(t)$ : fair share at time t

$$C_i(t) = \min(r_i, \alpha(t))$$

$$\alpha(t) : \sum_{j \in B(t)} \min(r_j, \alpha(t)) = C$$

# Max-min fairness

C: link capacity

B(t): set of backlogged flows at time t

$C_i(t)$ : bandwidth received by flow i at time t

## Case: weights

$w_i$ : relative weight of flow i

$$C_i(t) = \frac{w_i}{\sum_{j \in B(t)} w_j} C$$

## Case: max. requirements

$r_i$ : max. bandwidth requirement for flow i

$\alpha(t)$ : fair share at time t

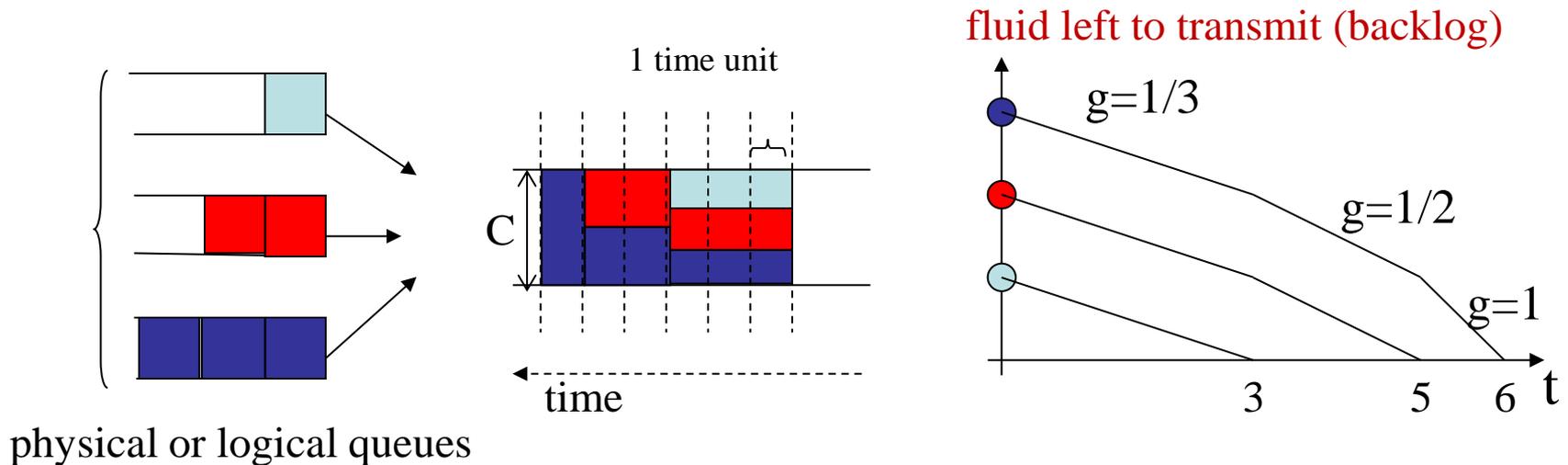
$$C_i(t) = \min(r_i, \alpha(t))$$

$$\alpha(t) : \sum_{j \in B(t)} \min(r_j, \alpha(t)) = C$$

- Calculate fair shares:
  - 3 backlogged (saturated) flows, equal weights, link capacity 10.
  - 3 backlogged flows, weights 1,2,2 link capacity 10
  - 4 backlogged flows, max requirements: 2, 3, 4, 5, link capacity 11.
  - 3 backlogged flows, rate requirements: 2,4,5, the link capacity is 11.  
What are the fair shares now?

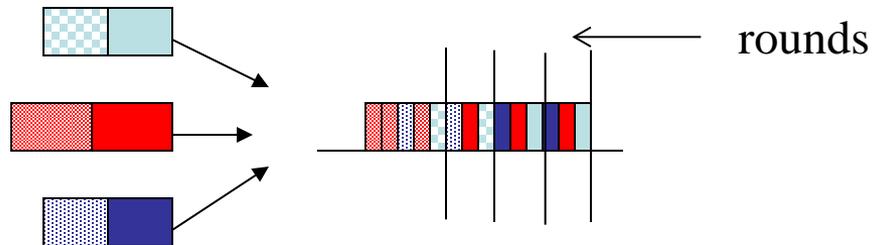
# Fair queuing-for max-min fairness

- Fluid approximation
  - fluid fair queuing (FFQ) or generalized processor sharing (GPS)
  - idealized policy to split bandwidth
  - assumption: dedicated buffer per flow
  - assumption: flows from backlogged queues served simultaneously (like fluid)
  - not implementable, used to evaluate real approaches
  - used for performance analysis if per packet performance is not interesting

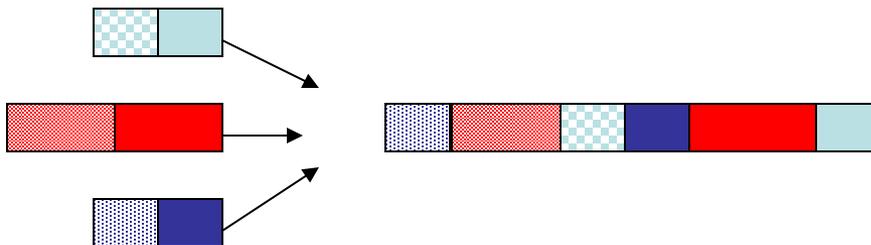


# Packet-level Fair queuing

- How to realize GPS/FFQ?
- Bit-by-bit fair queuing
  - one bit from each backlogged queue in rounds (round robin) – still not possible to implement



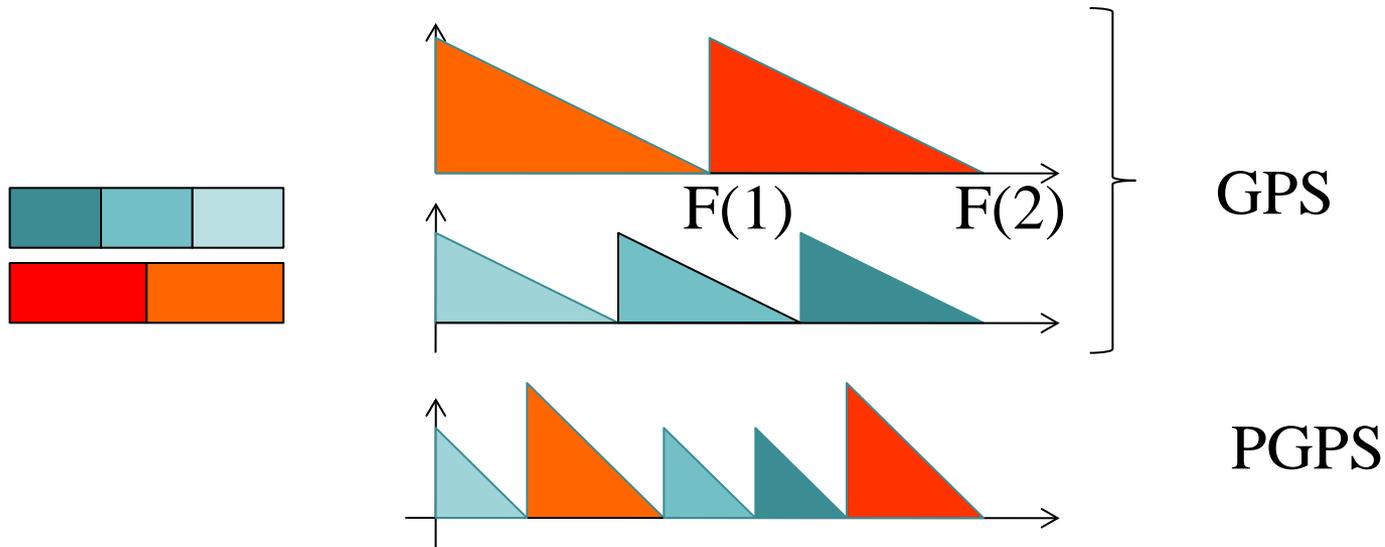
- Packet-level fair queuing
  - one packet from each backlogged queue in rounds ???



Flows with large packets  
get more bandwidth!  
More sophisticated schemes  
required!

# Packetized GPS (PGPS)

- How to realize GPS/FFQ?
- Try to mimic GPS
- Transmit packets that would arrive earliest with GPS
  - Finishing time ( $F(p)$ )
- Quantify the difference between GPS and PGPS



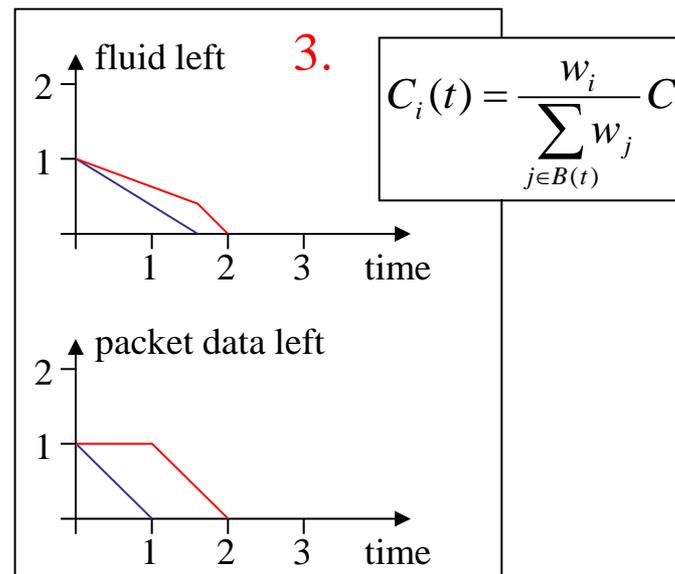
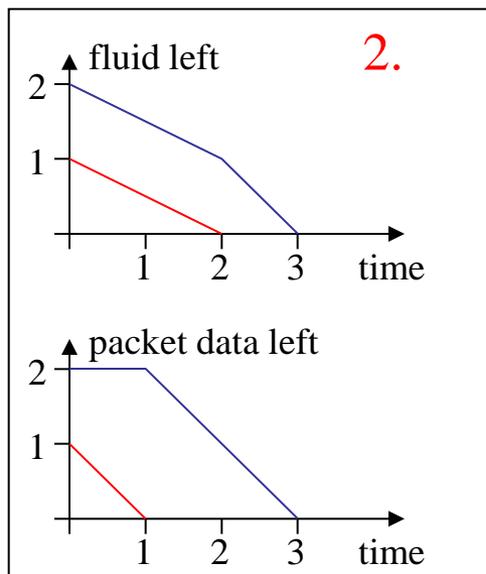
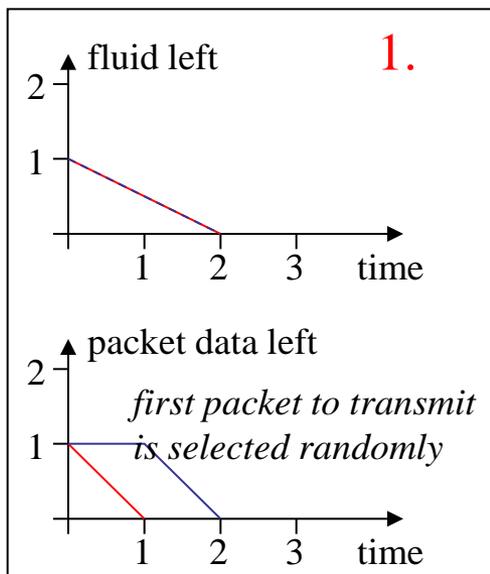
# Fair queuing – group work

- Packet-by-packet GPS (PGPS)
  - Compare GPS (fluid) and PGPS (packetized) in the following scenarios – draw diagrams “backlogged traffic per flow vs. time”.
  - Consider one packet in each queue.  $C=1$  unit/sec
1. Two flows, equal size packets, same weight,  $L1=L2=1$  unit
  2. Two flows, different size packets, same weight  $L1=1, L2=2$  units
  3. Two flows, same packet size, different weight,  $L1=L2=1$  unit,  $w1=1, w2=2$

$$C_i(t) = \frac{w_i}{\sum_{j \in B(t)} w_j} C$$

# Fair queuing – group work

- Compare GPS (fluid) and PGPS (packetized) in the following scenarios – draw diagrams “backlogged traffic per flow vs. time”.
- Consider one packet in each queue.  $C=1$  unit/sec
- 1. Two flows, equal size packets, same weight,  $L1=L2=1$  unit
- 2. Two flows, different size packets, same weight  $L1=1, L2=2$  units
- 3. Two flows, same packet size, different weight,  $L1=L2=1$  unit,  $w1=1, w2=2$



# Scheduling summary

- Scheduling:
  - At the network nodes and at the edge
  - To provide quality guarantees or fairness
  - Work-conserving and non-work-conserving
- Max-min fairness in a single link, with weights and max. rate requirement
- GPS for max-min fairness in a fluid model
- PGPS (or WFQ) in the packetized version
  - Schedule according to finish time in GPS
  - Guaranteed performance compared to GPS
- Next lecture: PGPS in detail, work-conserving and non-work-conserving scheduling

# Reading assignment

- A. Parekh, R. Gallager, "A Generalized Processor Sharing Approach to Flow Control - The Single Node Case," IEEE Transaction on Networking, 1993, Vol.1, No.3.
  - Read from I to III-before part A
- H. Zhang, "Service Disciplines for Guaranteed Performance Service in Packet-Switching Networks," Proceedings of the IEEE, Oct, 1995, pp. 1374-1396
  - Read sections I, II, and III.