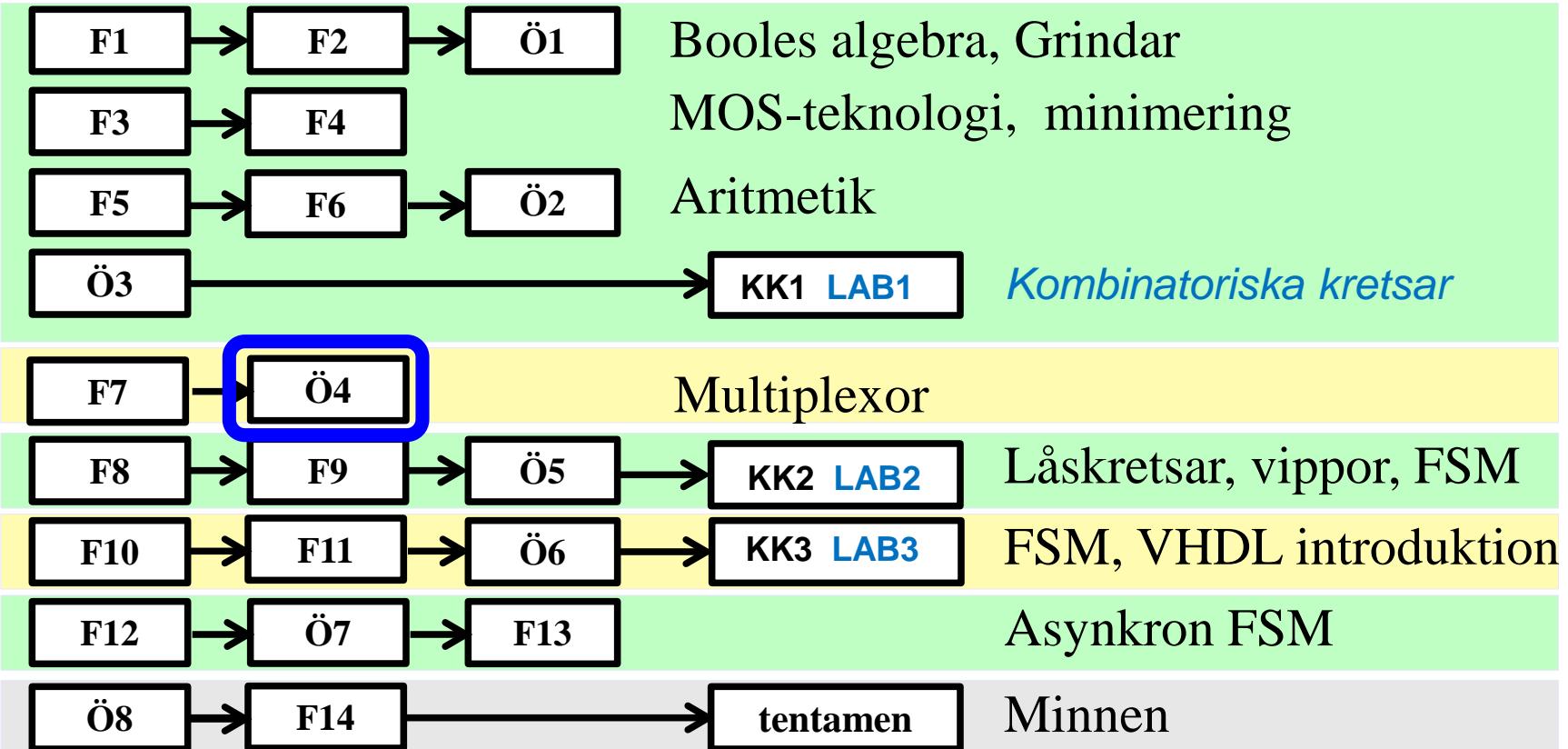
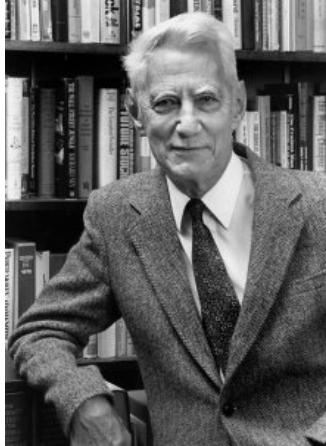


IE1204 Digital Design



*Föreläsningar och övningar bygger på varandra! Ta alltid igen det Du missat!
Läs på i förväg – delta i undervisningen – arbeta igenom materialet efteråt!*

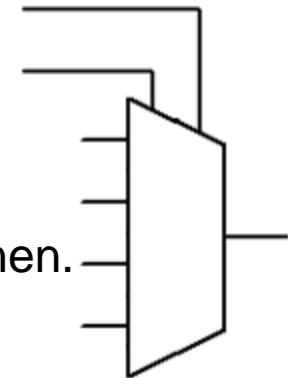
Shannon dekomposition



Claude Shannon
matematiker/elektrotekniker
(1916 –2001)

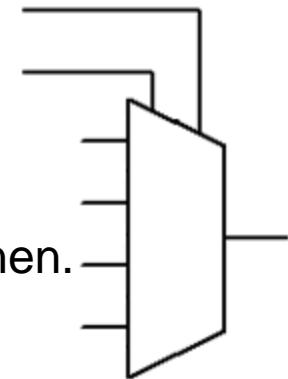
(ÖH 8.6)

Visa hur en 4-to-1 **multiplexor** kan användas som "funktionsgenerator" för att tex. Generera OR-funktionen.

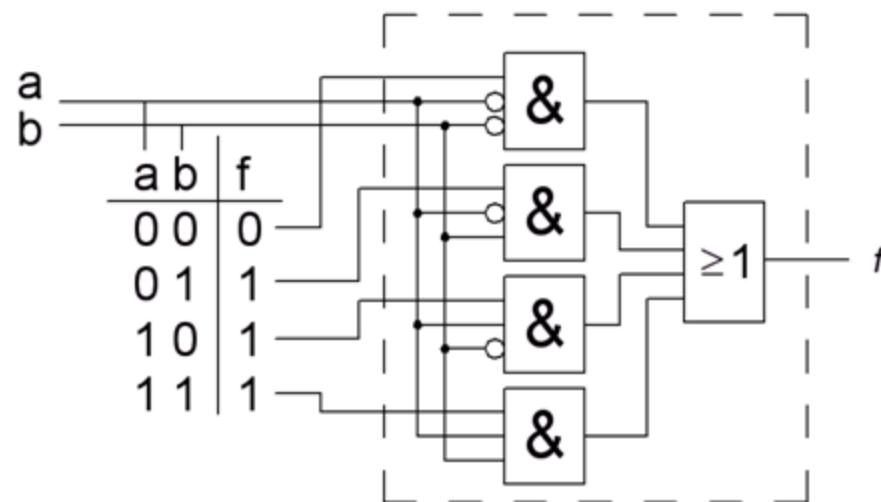


(ÖH 8.6)

Visa hur en 4-to-1 multiplexor kan användas som "funktionsgenerator" för att tex. Generera OR-funktionen.

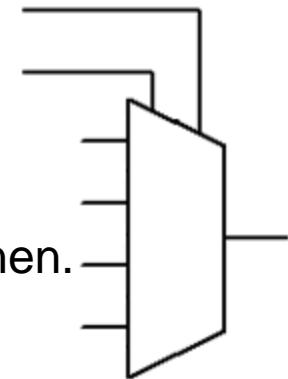


Multiplexor *som funktionsgenerator*

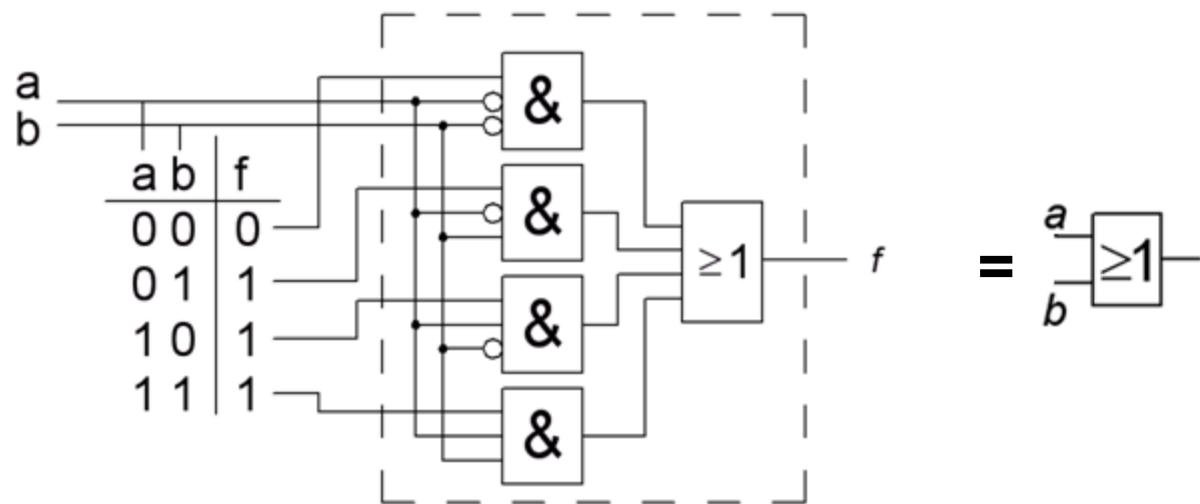


(ÖH 8.6)

Visa hur en 4-to-1 multiplexor kan användas som "funktionsgenerator" för att tex. Generera OR-funktionen.



Multiplexor *som funktionsgenerator*



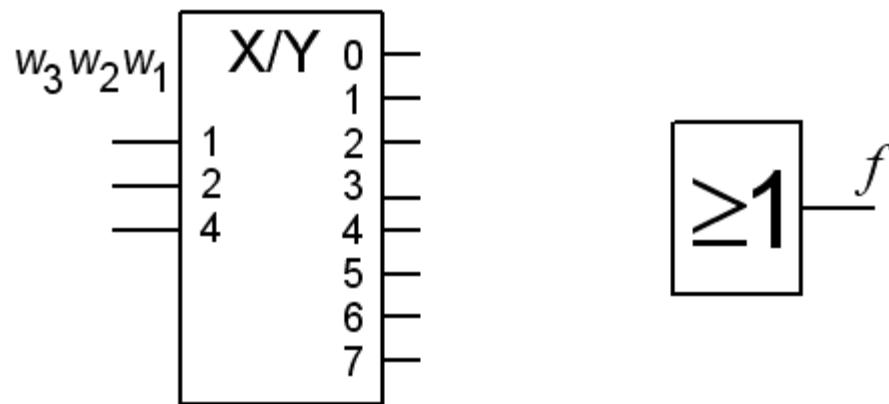
William Sandqvist william@kth.se

BV 6.1

Show how the function

$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 4, 5, 7)$$

can be implemented using a 3-to-8 **decoder** and an OR gate.

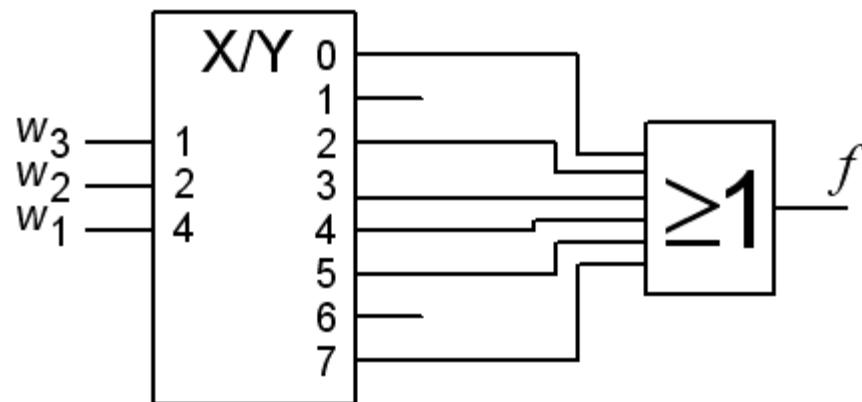


BV 6.1

Show how the function

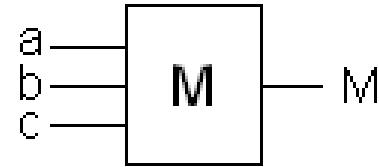
$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 4, 5, 7)$$

can be implemented using a 3-to-8 **decoder** and an OR gate.



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ÖH 8.7



En majoritetsgrind antar på utgången samma värde som en *majoritet* av ingångarna. Grinden kan tex. användas i feftolerant logik, eller till bildbehandlingskretsar.

- a) (Ställ upp grindens sanningstabell och minimera funktionen med Karnaughdiagram. Realisera funktionen med AND-OR grindar.)
- b) Realisera majoritetsgrinden med en 8:1 MUX.
- c) Använd Shannon dekomposition och realisera majoritetsgrinden med en 2:1 MUX och grindar.
- d) Realisera majorotetsgrinden med bara 2:1 MUXar.

(8.7a)

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Med AND OR grindar

$\bar{a}bc$

$a\bar{b}c$

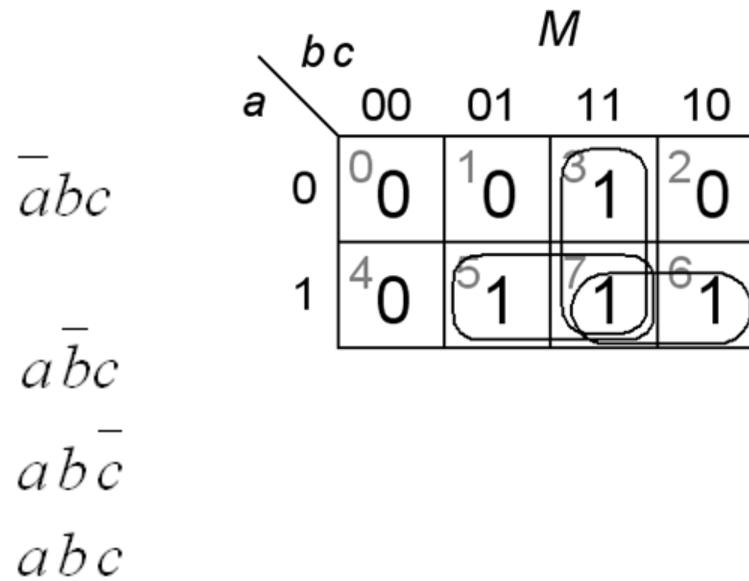
$a\bar{b}\bar{c}$

$a\bar{b}c$

(8.7a)

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

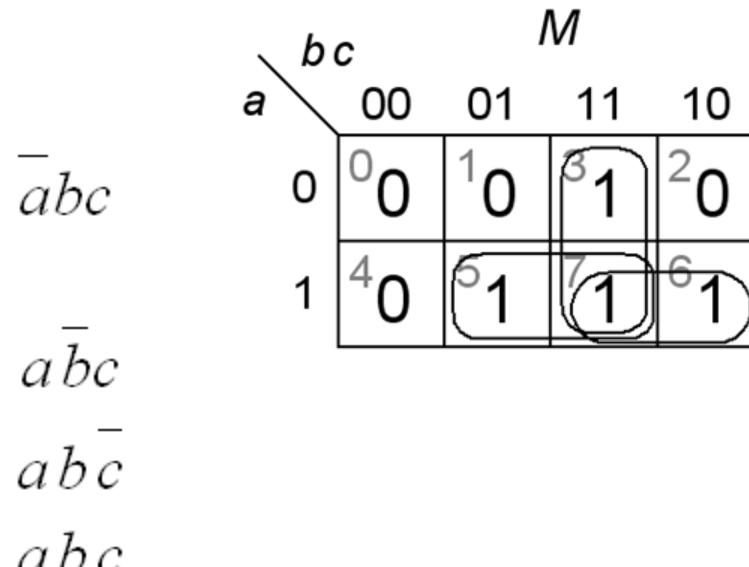
Med AND OR grindar



(8.7a)

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Med AND OR grindar

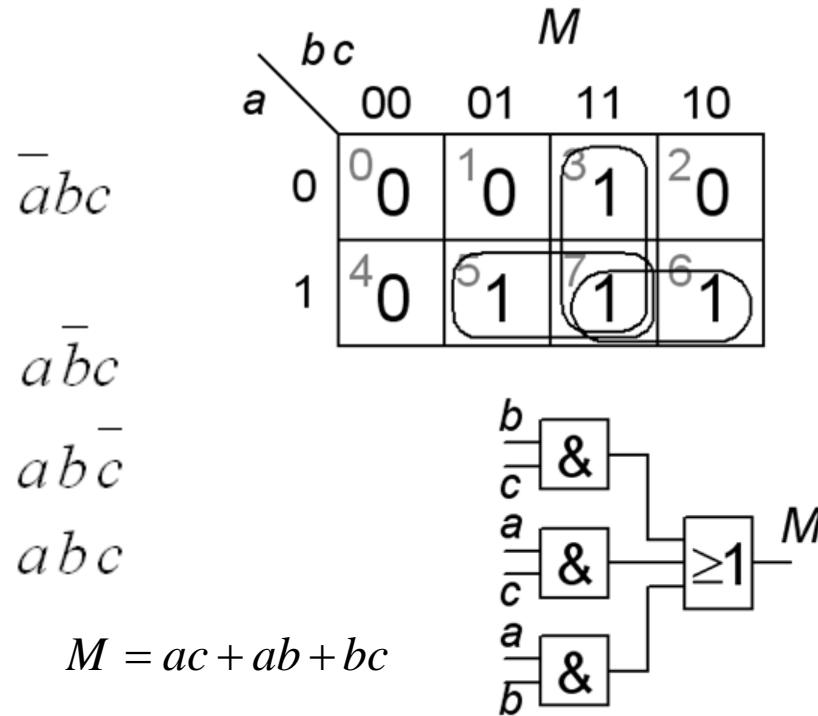


$$M = ac + ab + bc$$

(8.7a)

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Med AND OR grindar



8.7b

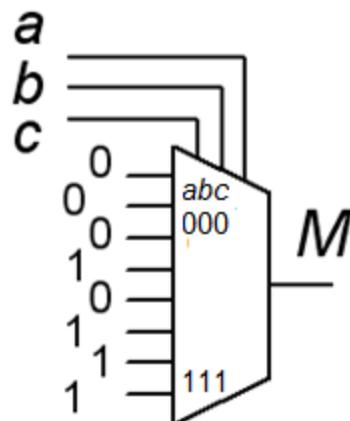
	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Med 8-to-1 mux ...

8.7b

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Med 8-to-1 mux ...



8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

*Shannon dekomposition. 2-to-1 mux
och grindar.*

$\bar{a}bc$

$a\bar{b}c$

$ab\bar{c}$

abc

8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. 2-to-1 mux och grindar.

$\bar{a}bc$

$a\bar{b}c$

$a b \bar{c}$

$a b c$

$$\begin{aligned}M &= \bar{a}bc + a\bar{b}c + a b \bar{c} + abc = \\&= \bar{a}(bc) + a(\bar{b}c + b\bar{c} + bc) =\end{aligned}$$

8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. 2-to-1 mux och grindar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$

$$\begin{aligned} M &= \bar{a}bc + a\bar{b}c + ab\bar{c} + abc = \\ &= \bar{a}(bc) + a(\bar{b}c + b\bar{c} + bc) = \end{aligned}$$

	b	c	
0	0	0	0
0	1	1	$\bar{b}c$
1	0	1	$b\bar{c}$
1	1	1	bc

8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. 2-to-1 mux och grindar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$

$$\begin{aligned} M &= \bar{a}bc + a\bar{b}c + ab\bar{c} + abc = \\ &= \bar{a}(bc) + a(\bar{b}c + b\bar{c} + bc) = \end{aligned}$$

	b	c	
0	0	0	0
0	1	1	$\bar{b}c$
1	0	1	$b\bar{c}$
1	1	1	bc

OR

8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. 2-to-1 mux och grindar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$

$$\begin{aligned}
 M &= \bar{a}bc + a\bar{b}c + ab\bar{c} + abc = \\
 &= \bar{a}(bc) + a(\bar{b}c + b\bar{c} + bc) = \\
 &= \bar{a}(bc) + a(b + c)
 \end{aligned}$$

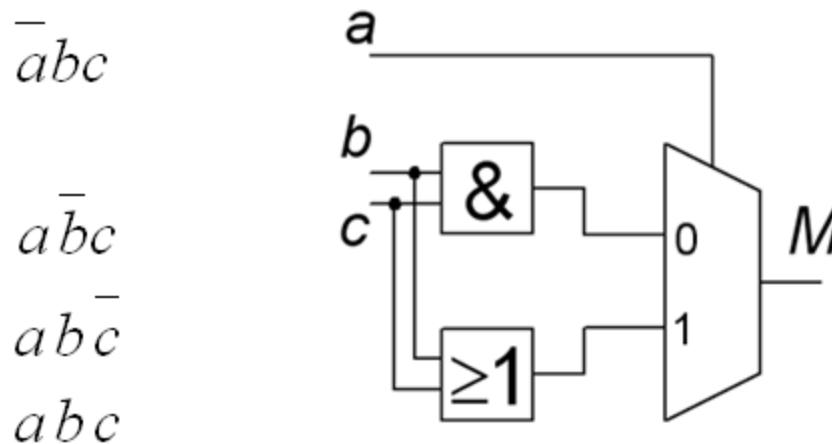
	b	c	
0	0	0	0
0	1	1	$\bar{b}c$
1	0	1	$b\bar{c}$
1	1	1	bc

OR

8.7c

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. 2-to-1 mux och grindar.



$$\begin{aligned}
 M &= \bar{a}bc + a\bar{b}c + ab\bar{c} + abc = \\
 &= \bar{a}(bc) + a(\bar{b}c + b\bar{c} + bc) = \\
 &= \bar{a}(bc) + a(b + c)
 \end{aligned}$$

b	c	M
0	0	0
0	1	1
1	0	1
1	1	1

OR

8.7d

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. Enbart 2-to-1 muxar.

$\bar{a}bc$

$a\bar{b}c$

$ab\bar{c}$

abc

8.7d

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

Shannon dekomposition. Enbart 2-to-1 muxar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$

$$M = \bar{a}(bc) + a(b+c) \quad g = bc \quad h = b+c$$

$$g = \bar{b}(0) + b(c) = \bar{b} \cdot 0 + b \cdot c$$

$$h = b+c = b + (b+\bar{b})c = \bar{b}c + b + bc = \bar{b}c + b(1+c) = \bar{b} \cdot c + b \cdot 1$$

8.7d

a	b	c	M
0	0	0	0
1	0	0	1
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0
7	1	1	1

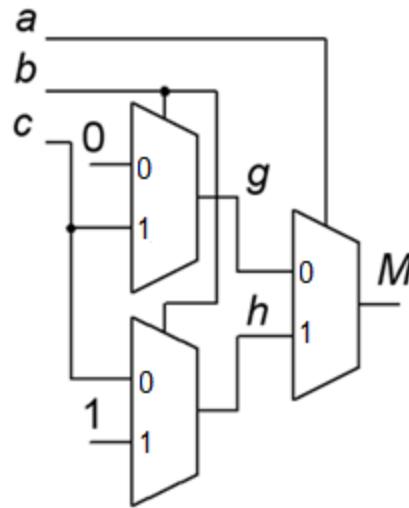
Shannon dekomposition. Enbart 2-to-1 muxar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$



$$M = \bar{a}(bc) + a(b+c) \quad g = bc \quad h = b+c$$

$$g = \bar{b}(0) + b(c) = \bar{b} \cdot 0 + b \cdot c$$

$$h = b+c = b + (b+\bar{b})c = \bar{b}c + b + bc = \bar{b}c + b(1+c) = \bar{b} \cdot c + b \cdot 1$$

8.7d

	a	b	c	M
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	1
7	1	1	1	1

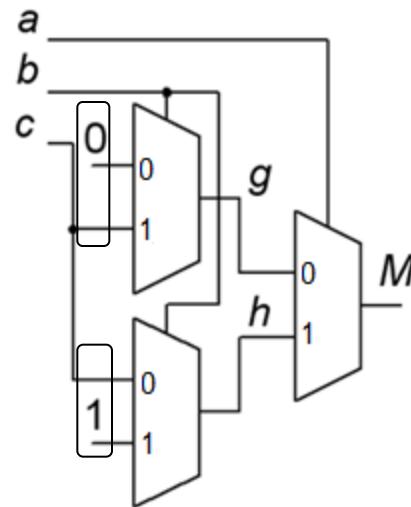
Shannon dekomposition. Enbart 2-to-1 muxar.

$$\bar{a}bc$$

$$a\bar{b}c$$

$$ab\bar{c}$$

$$abc$$



$$M = \bar{a}(bc) + a(b+c) \quad g = bc \quad h = b+c$$

$$g = \bar{b}(0) + b(c) = \bar{b}[0] + b[c]$$

$$h = b+c = b + (b+\bar{b})c = \bar{b}c + b + bc = \bar{b}c + b(1+c) = \bar{b}[c] + b[1]$$

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BV 6.5

For the function

$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 6)$$

use Shannon's expansion to derive an implementation using a 2-to-1 multiplexer and any necessary gates.

BV 6.5

For the function

$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 6)$$

use Shannon's expansion to derive an implementation using a 2-to-1 multiplexer and any necessary gates.

$$\begin{aligned} f(w_1, w_2, w_3) &= \sum m(000, 010, 011, 110) = \\ &= \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} w_2 \overline{w_3} + w_1 \overline{w_2} \overline{w_3} = \\ &= \overline{w_1} (\overline{w_2} \overline{w_3} + w_2 \overline{w_3} + w_2 w_3) + w_1 (w_2 \overline{w_3}) = \\ &= \overline{w_1} (w_2 + \overline{w_3}) + w_1 (w_2 \overline{w_3}) \end{aligned}$$

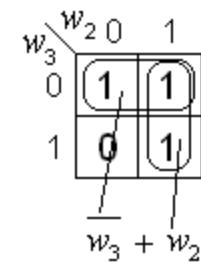
BV 6.5

For the function

$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 6)$$

use Shannon's expansion to derive an implementation using a 2-to-1 multiplexer and any necessary gates.

$$\begin{aligned} f(w_1, w_2, w_3) &= \sum m(000, 010, 011, 110) = \\ &= \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} w_2 \overline{w_3} + w_1 \overline{w_2} \overline{w_3} = \\ &= \overline{w_1} (\overline{w_2} \overline{w_3} + w_2 \overline{w_3} + w_2 w_3) + w_1 (w_2 \overline{w_3}) = (\overline{w_2} \overline{w_3} + w_2 \overline{w_3} + w_2 w_3) \\ &= \overline{w_1} (w_2 + \overline{w_3}) + w_1 (w_2 \overline{w_3}) \end{aligned}$$



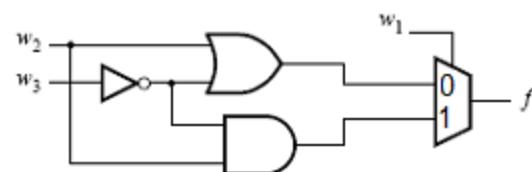
BV 6.5

For the function

$$f(w_1, w_2, w_3) = \sum m(0, 2, 3, 6)$$

use Shannon's expansion to derive an implementation using a 2-to-1 multiplexer and any necessary gates.

$$\begin{aligned} f(w_1, w_2, w_3) &= \sum m(000, 010, 011, 110) = \\ &= \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} \overline{w_2} \overline{w_3} + \overline{w_1} w_2 \overline{w_3} + w_1 \overline{w_2} \overline{w_3} = \\ &= \overline{w_1} (\overline{w_2} \overline{w_3} + w_2 \overline{w_3} + w_2 w_3) + w_1 (w_2 \overline{w_3}) = (\overline{w_2} \overline{w_3} + w_2 \overline{w_3} + w_2 w_3) \\ &= \overline{w_1} (w_2 + \overline{w_3}) + w_1 (w_2 \overline{w_3}) \end{aligned}$$

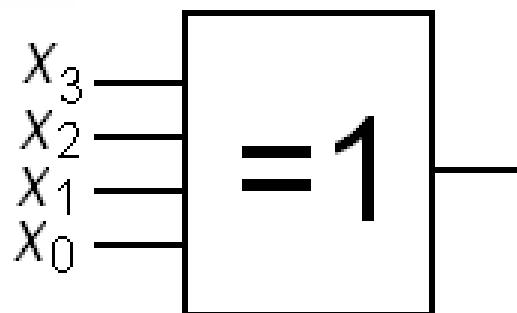


w ₃	w ₂	0	1
0	1	1	
1	0		1

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(ÖH 8.9)



Visa hur en 4 ingångars exorgrind (XOR, udda paritetsfunktion) realiseras i en FPGA-krets. Visa innehållet i SRAM-cellerna (LUT, LookUp Table).

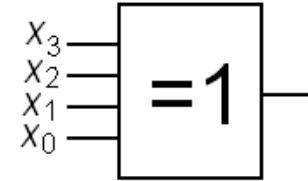
XOR

		x_1	x_0	00	01	11	10
		x_3	x_2	00	11	30	21
		0	0	00	11	30	21
		0	1	41	50	71	60
		1	0	120	131	150	141
		1	1	81	90	111	100
		0	0	00	11	30	21

XOR

	x_1	x_0	00	01	11	10					
x_3	0	0	0	1	1	3	0	2	1		
x_2	0	0	0	4	1	5	0	7	1	6	0
x_1	1	1	1	12	13	15	0	14	1		
x_0	1	0	8	1	9	0	11	1	10		

(8.9)

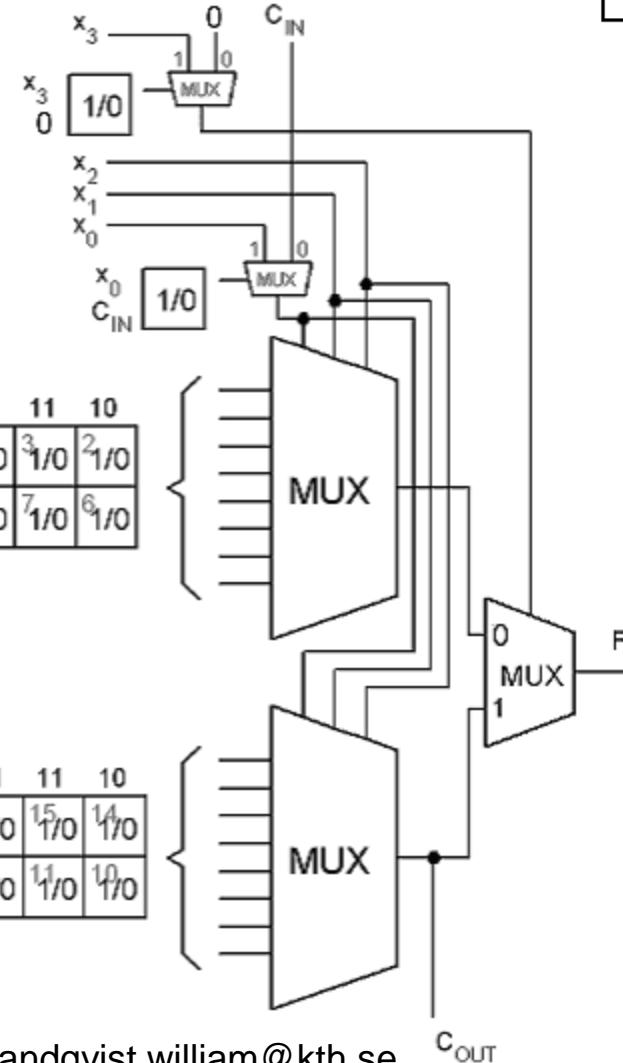


SRAM

	x_1	x_0	00	01	11	10					
x_3	0	0	0	1/0	1/0	3	1/0	2	1/0		
x_2	0	0	0	4	1/0	5	1/0	7	1/0	6	1/0
x_1	1	1	12	13	15	14	1/0				

SRAM

	x_1	x_0	00	01	11	10				
x_3	1	1	12	13	15	14	1/0			
x_2	1	1	8	1/0	9	1/0	11	1/0	10	1/0
x_1	0	0	12	13	15	14	1/0			

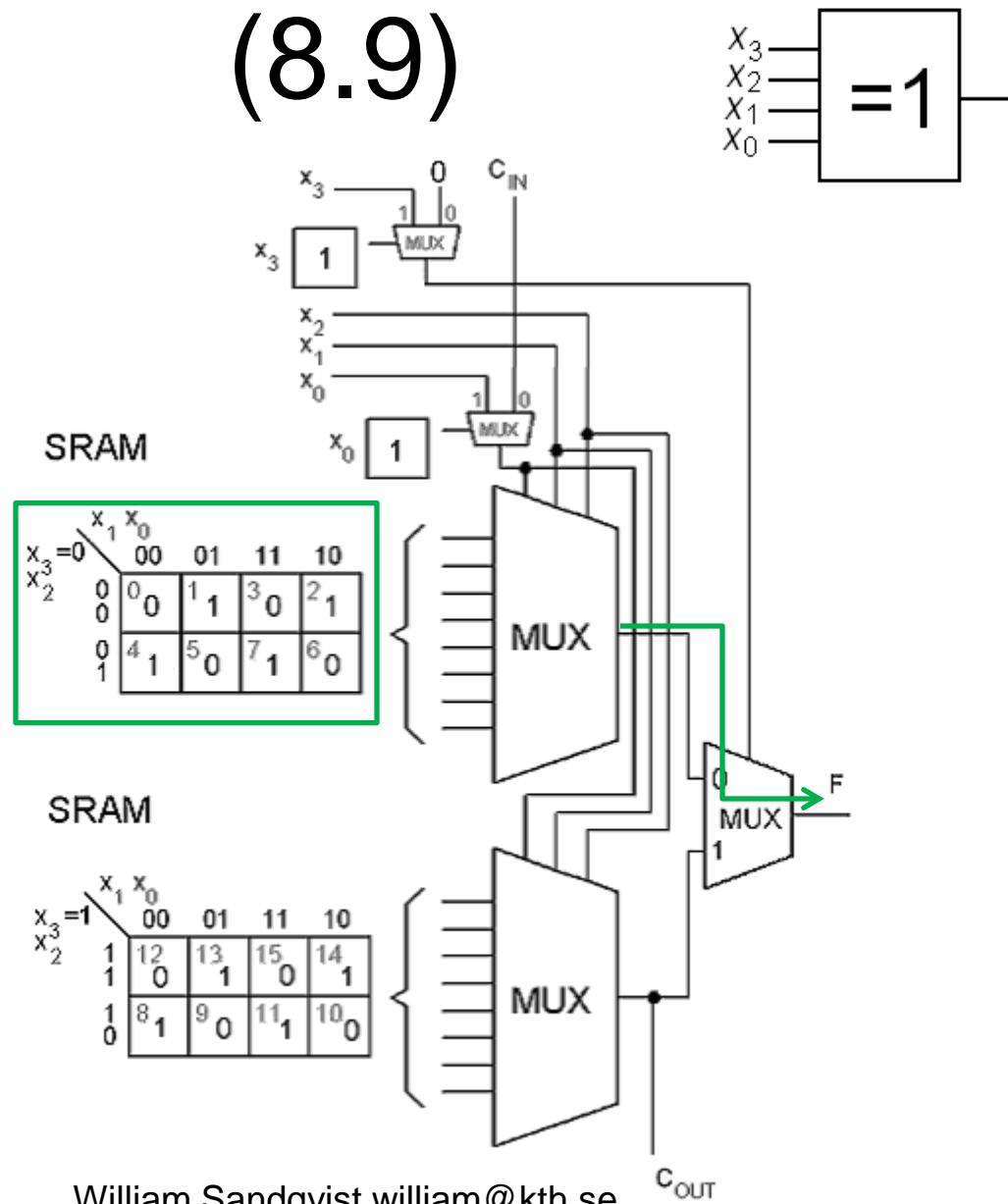


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(8.9)

XOR

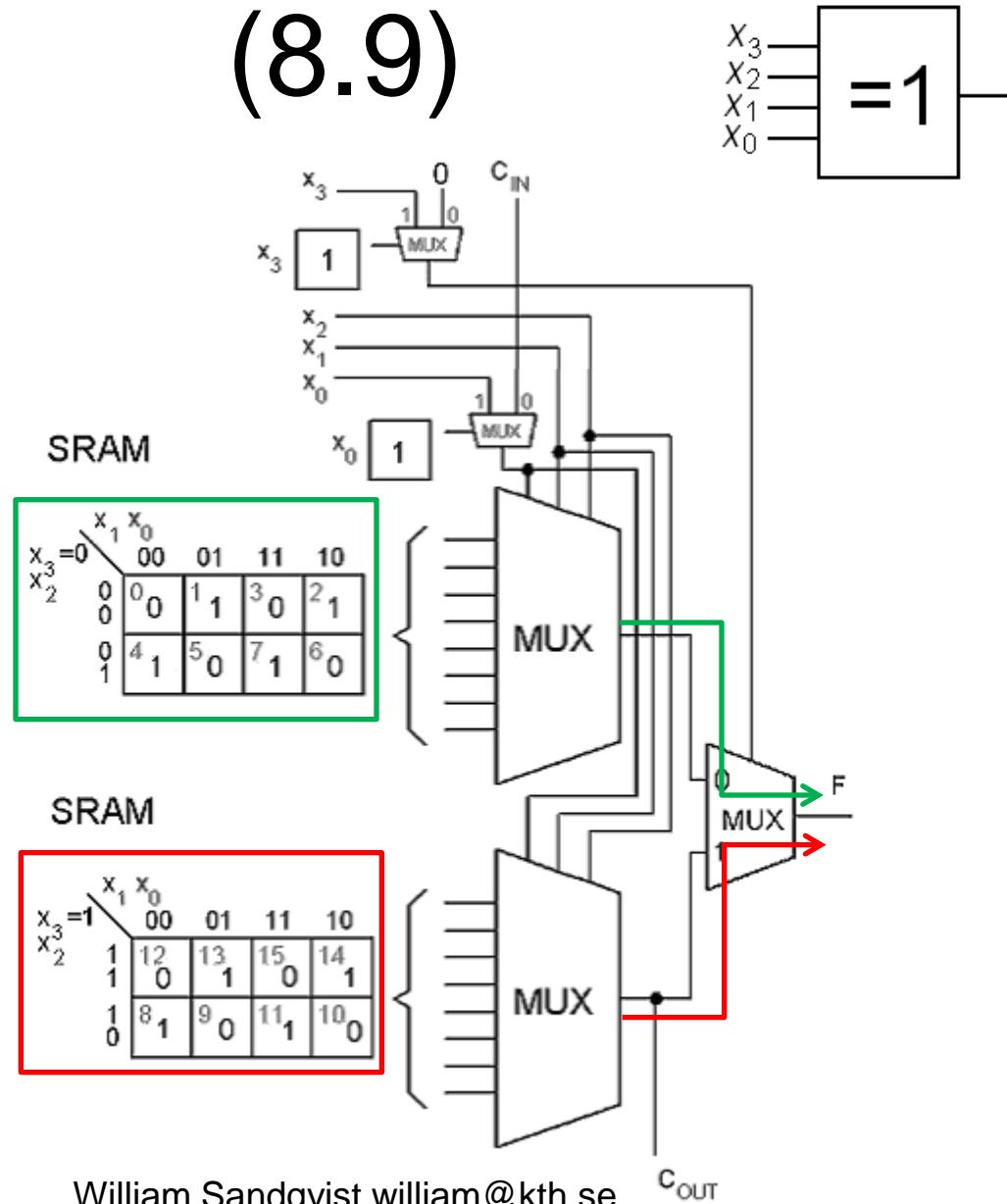
	x_1	x_0	00	01	11	10
x_3	0	0	0	1	0	1
x_2	0	0	0	1	1	0
x_1	0	1	1	0	1	1
x_0	1	0	0	1	0	0



(8.9)

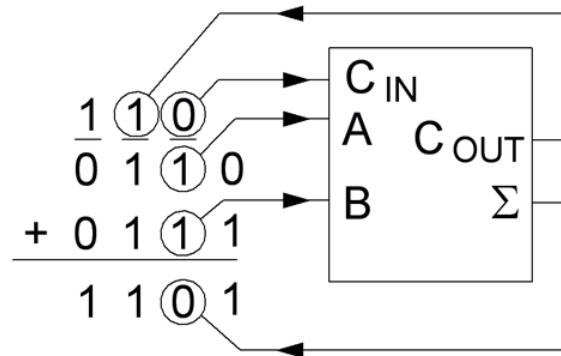
XOR

	x_1	x_0	00	01	11	10
x_3	0	0	0	1	3	2
x_2	0	0	0	1	3	2
x_1	0	1	1	0	1	1
x_0	0	1	0	1	1	0

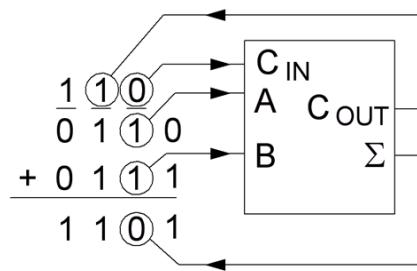


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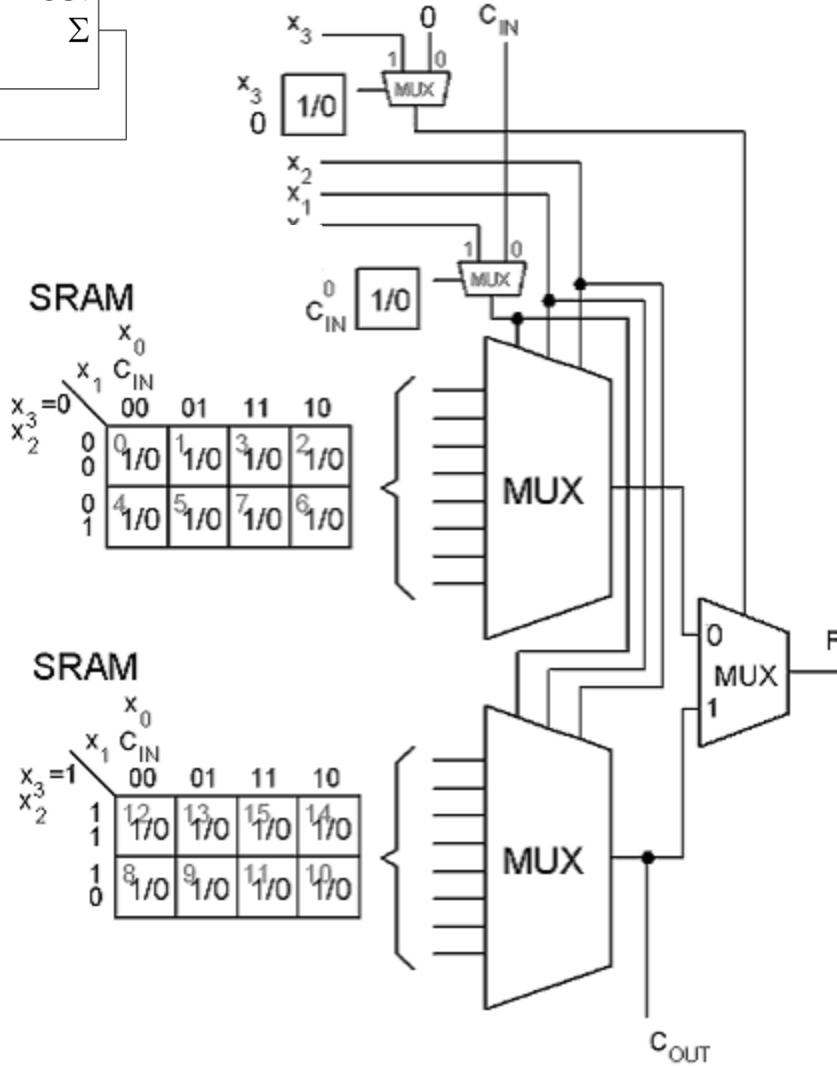
(ÖH 8.8)



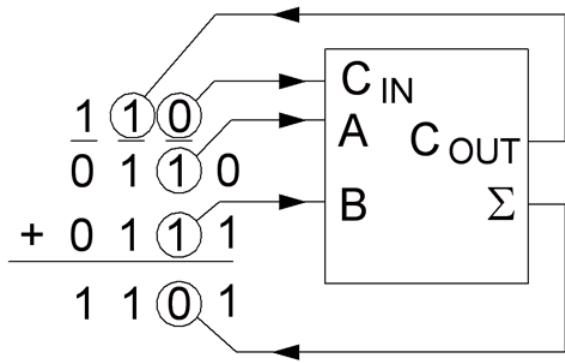
Ställ upp Ställ upp heladderarens sanningstabell. Visa hur en heladderare realiseras i en FPGA-krets. Logikelementen i en FPGA har möjlighet att kaskadkoppla C_{OUT} och C_{IN} mellan "grannarna". Visa innehållet i SRAM-cellerna (LUT, LookUp Table).



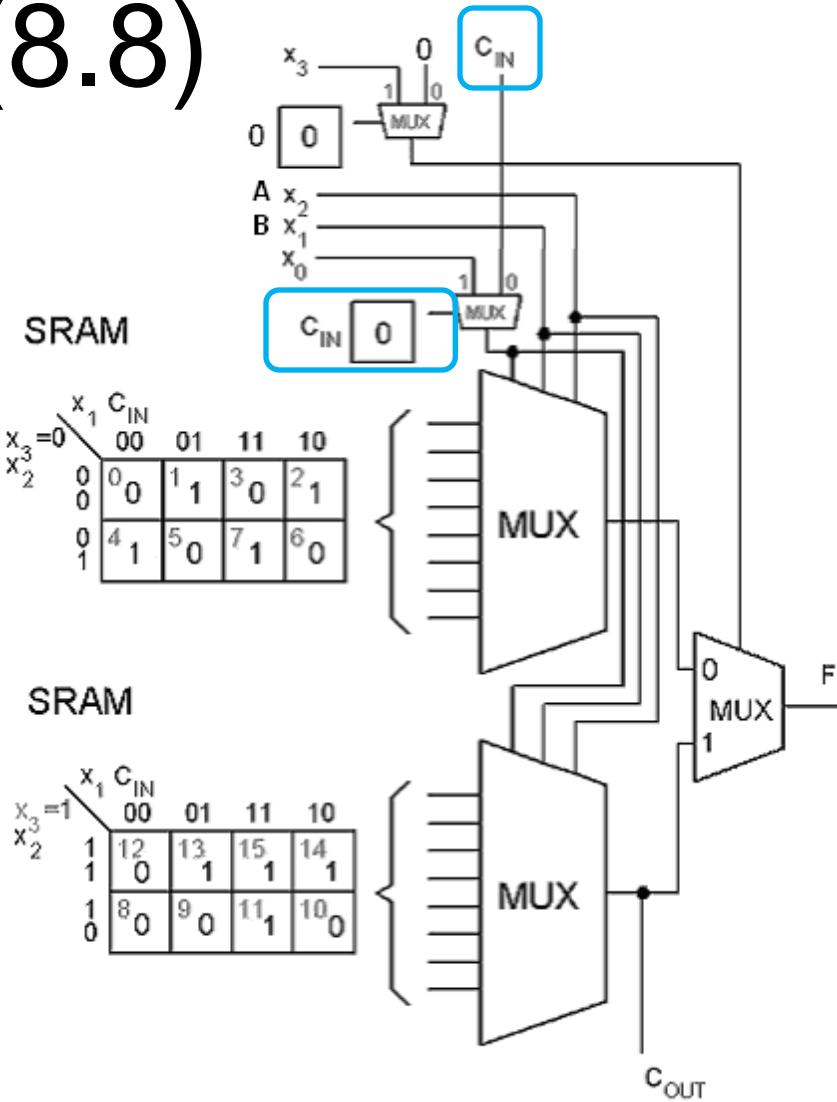
(8.8)

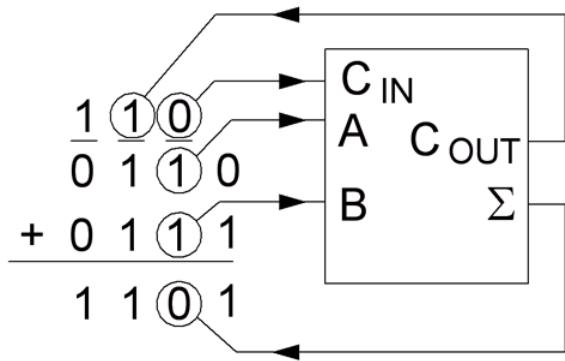


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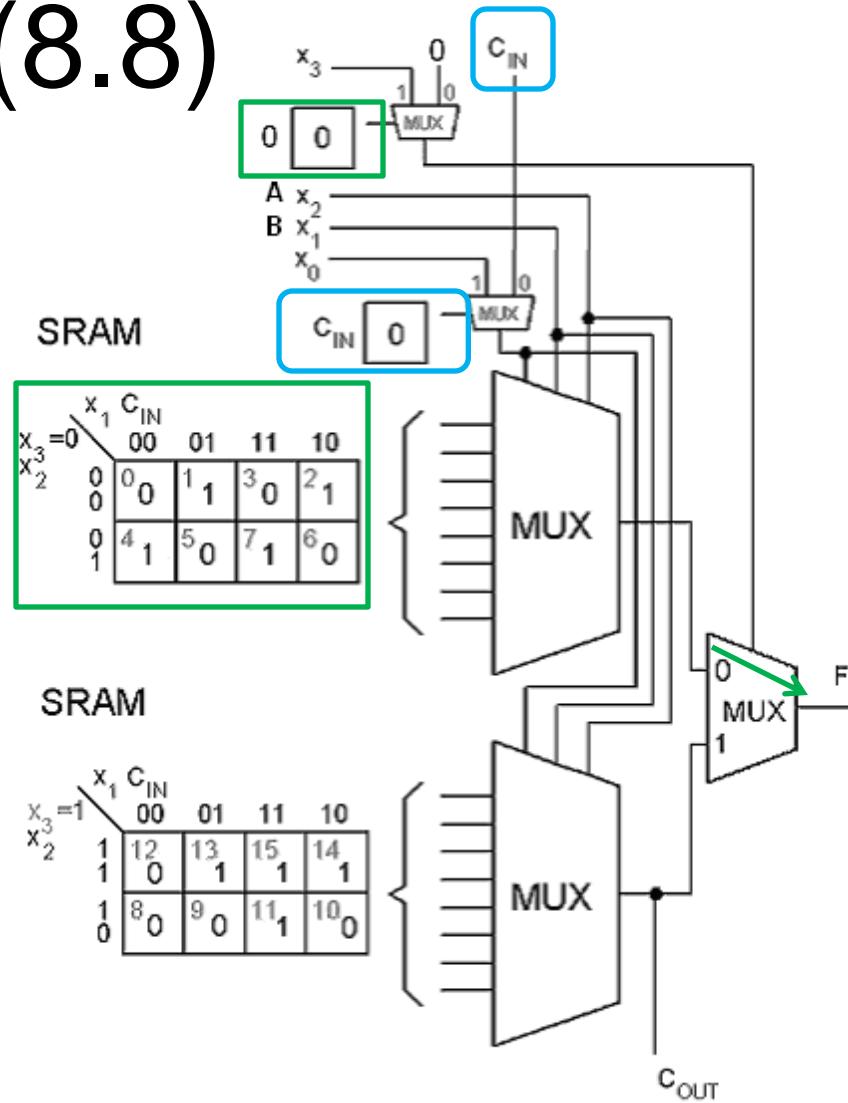


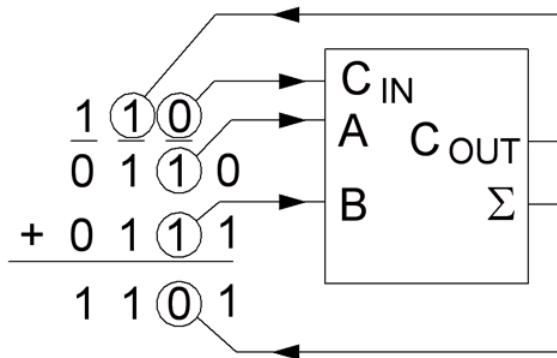
(8.8)



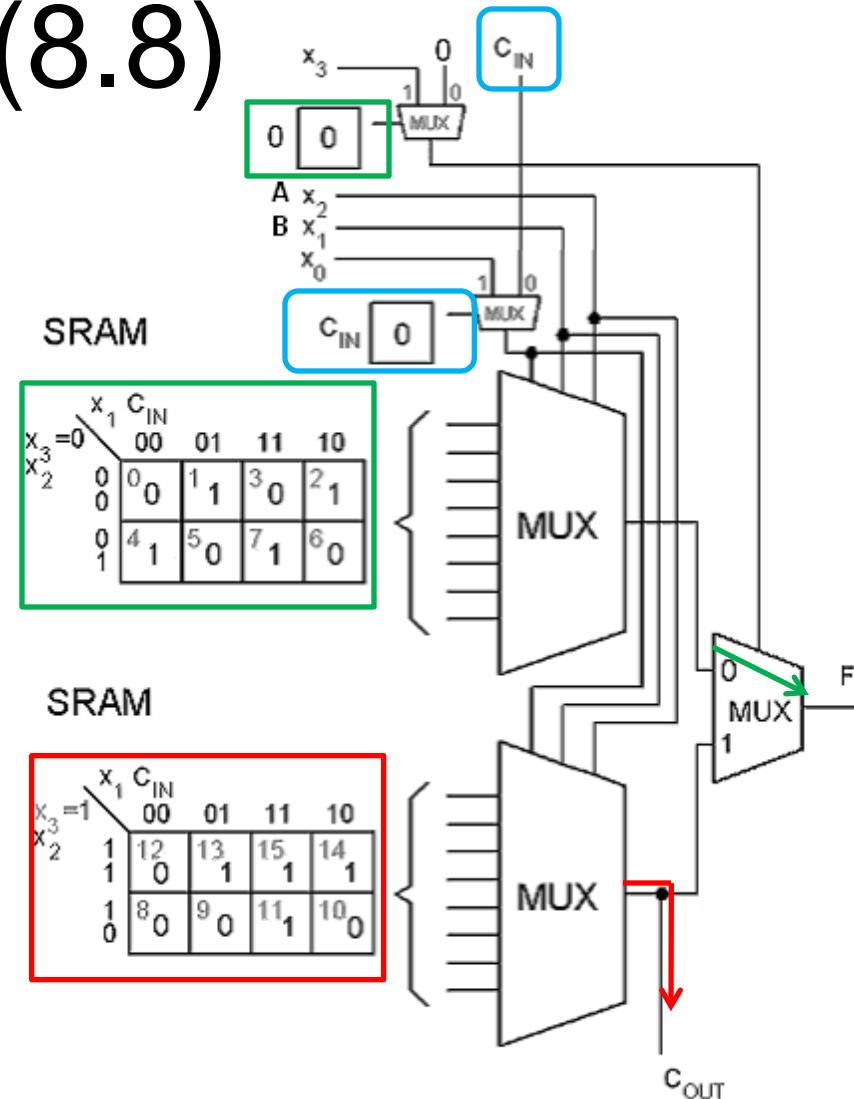


(8.8)





(8.8)

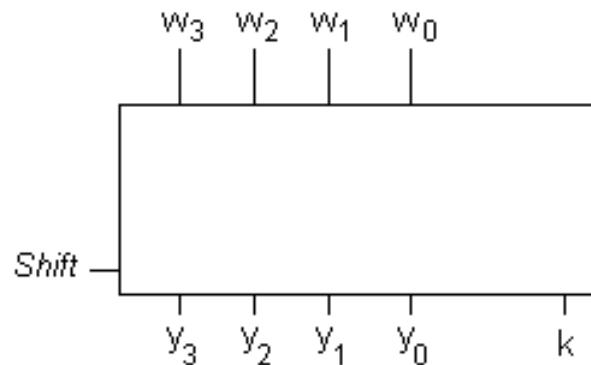


(BV ex 6.31)

In digital systems it is often necessary to have circuits that can shift the bits of a vector one or more bit positions to the left or right.

Design a circuit that can shift a four-bit vector $W = w_3w_2w_1w_0$ one bit position to the right when a control signal $Shift$ is equal to 1.

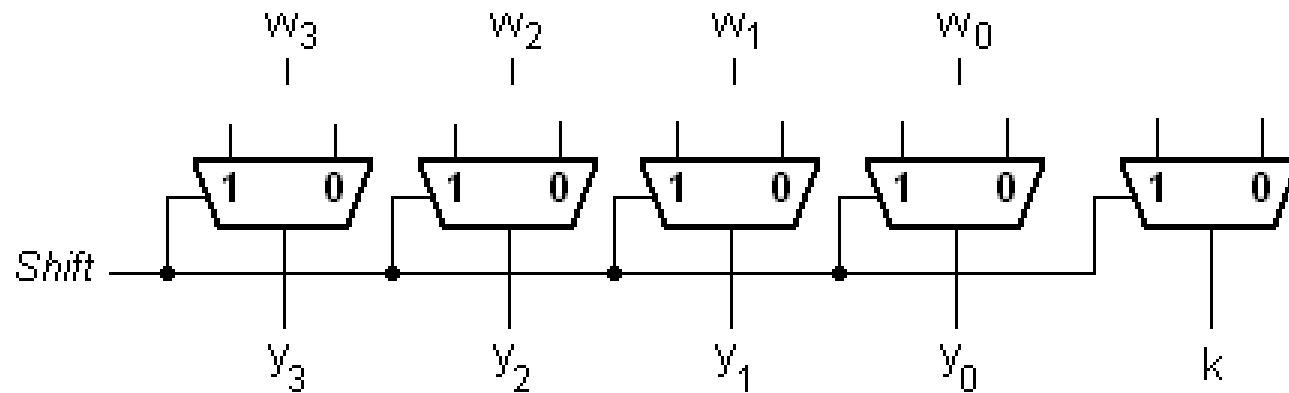
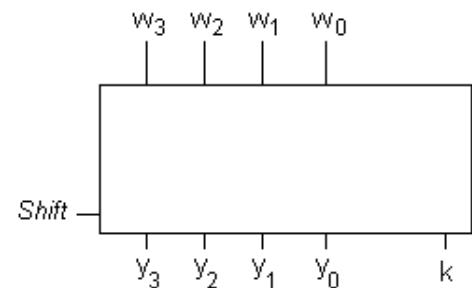
Let the outputs of the circuit be a four-bit vector $Y = y_3y_2y_1y_0$ and a signal k , such that if $Shift = 1$ then $y_3 = 0$, $y_2 = w_3$, $y_1 = w_2$, $y_0 = w_1$, and $k = w_0$. If $Shift = 0$ then $Y = W$ and $k = 0$.



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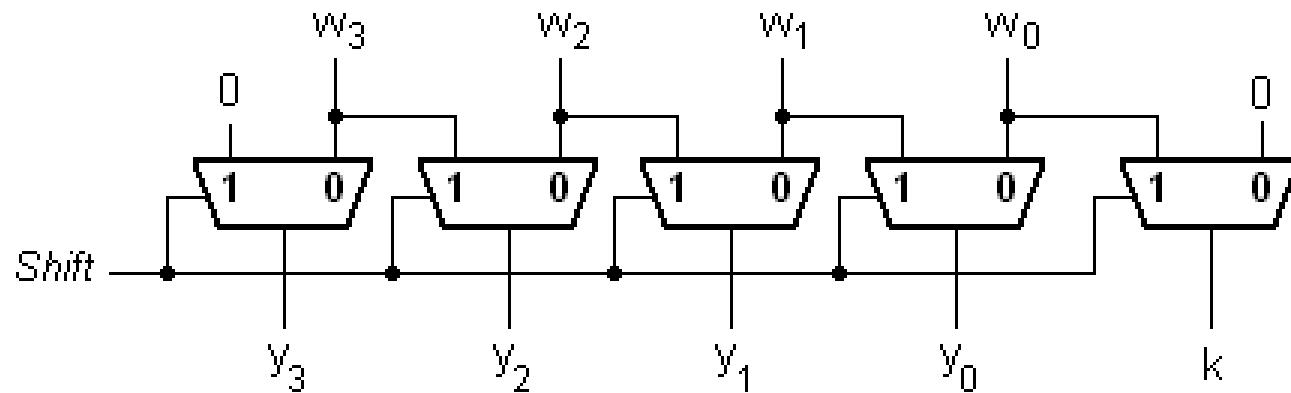
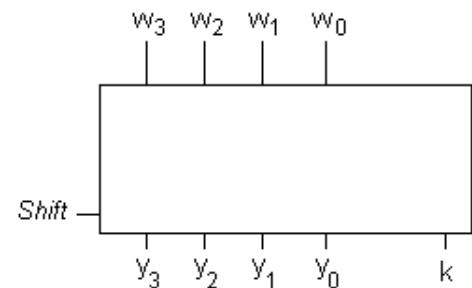
(BV ex 6.31)

Vi använder multiplexorer:



(BV ex 6.31)

Vi använder multiplexorer:



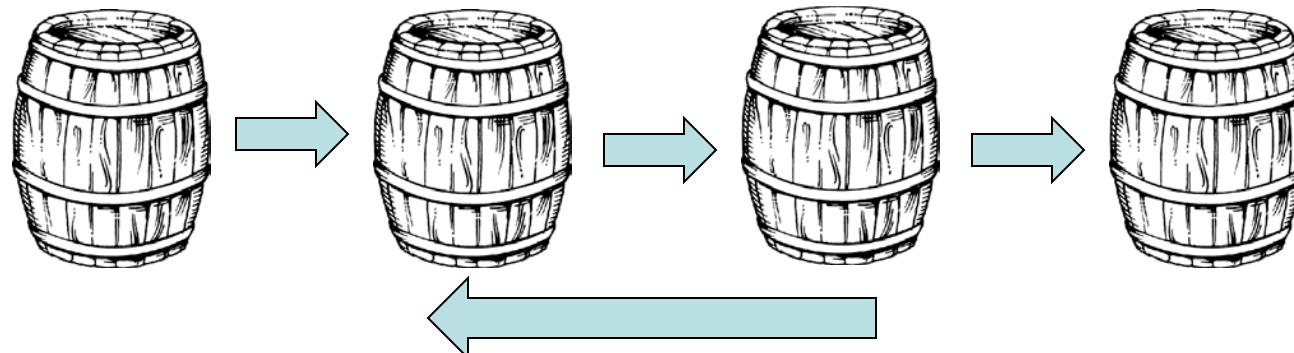
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BV ex. 6.32

Barrel shifter

The shifter in Example 6.31 shifts the bits of an input vector by one bit position to the right. It fills the vacated bit on the left side with 0. If the bits that are shifted out are placed into the vacated position on the left, then the circuit effectively rotates the bits of the input vector by a specified number of bit positions. Such a circuit is called a *barrel shifter*.

Design a four-bit barrel shifter that rotates the bits by 0, 1, 2, or 3 bit positions as determined by the valuation of two control signals s_1 and s_0 .



En barrelshifter används för att snabba upp flyttalsoperationer.

Barrel shifter

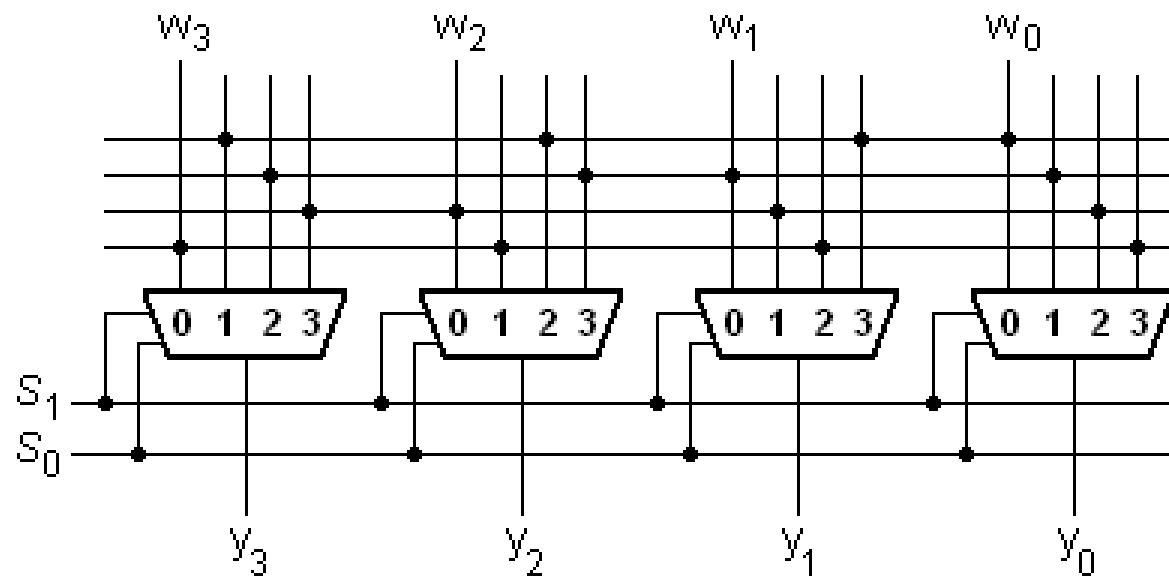
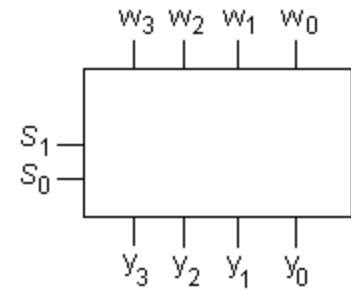


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BV ex. 6.32

Sanningstabell:

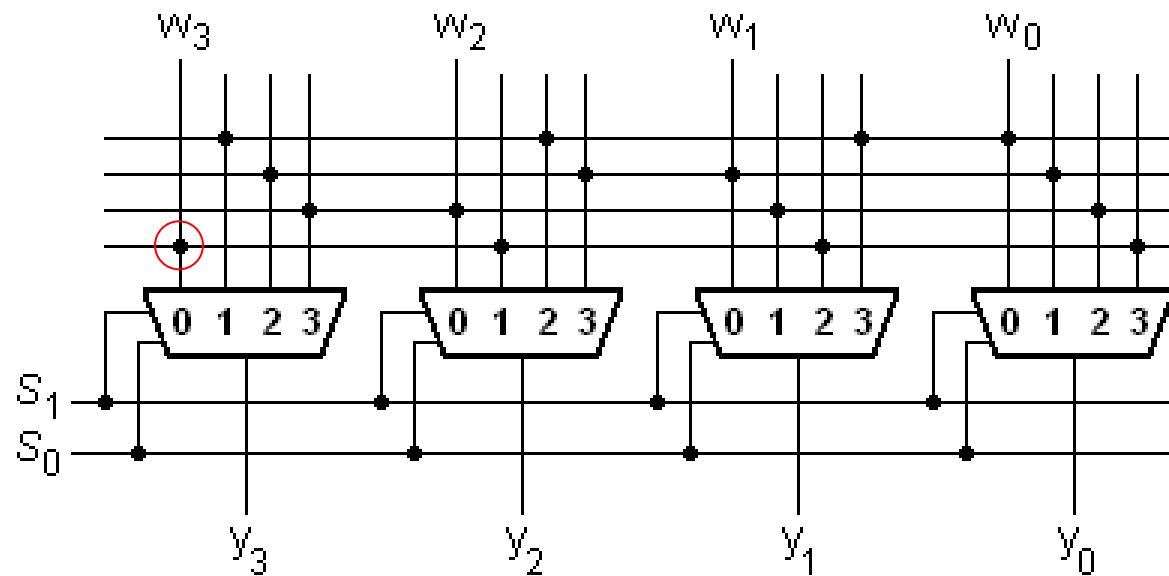
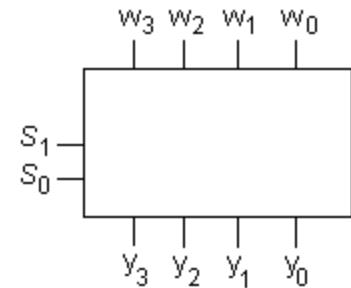
s_1	s_0	y_3	y_2	y_1	y_0
0	0	w ₃	w ₂	w ₁	w ₀
0	1	w ₀	w ₃	w ₂	w ₁
1	0	w ₁	w ₀	w ₃	w ₂
1	1	w ₂	w ₁	w ₀	w ₃



BV ex. 6.32

Sanningstabell:

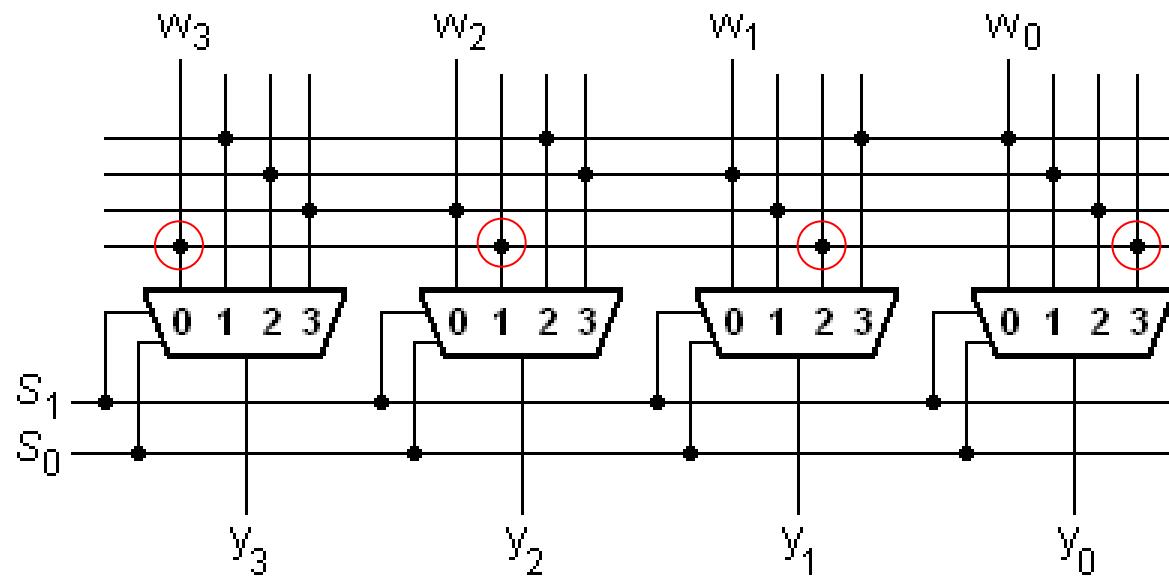
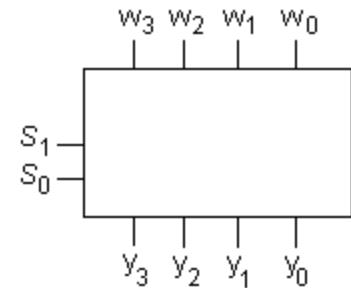
s_1	s_0	y_3	y_2	y_1	y_0
0	0	w ₃	w ₂	w ₁	w ₀
0	1	w ₀	w ₃	w ₂	w ₁
1	0	w ₁	w ₀	w ₃	w ₂
1	1	w ₂	w ₁	w ₀	w ₃



BV ex. 6.32

Sanningstabell:

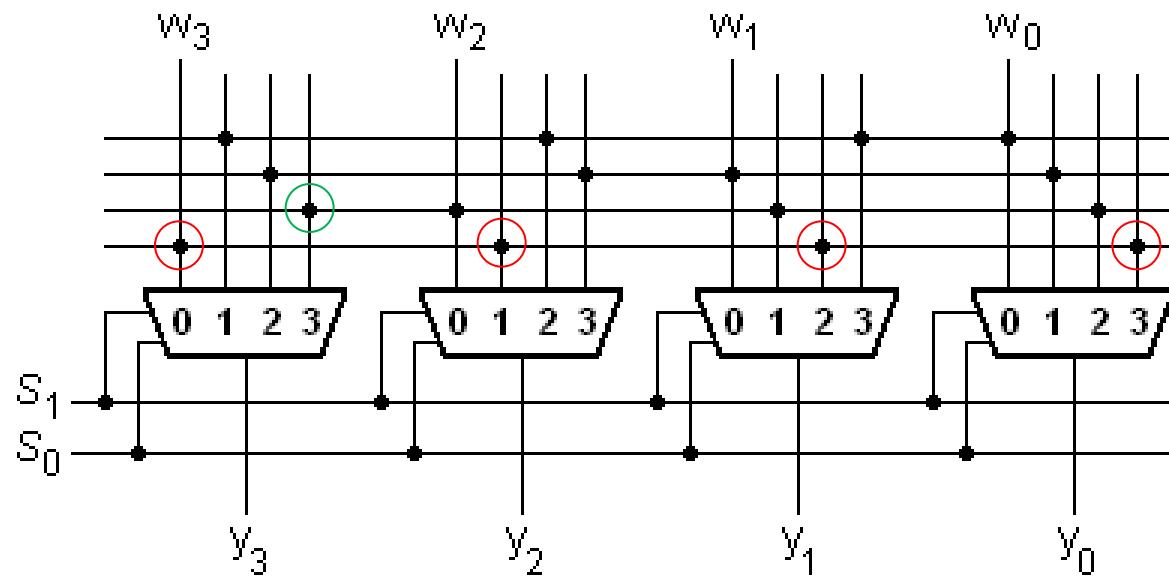
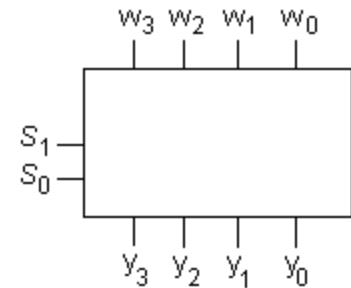
s_1	s_0	y_3	y_2	y_1	y_0
0	0	w ₃	w ₂	w ₁	w ₀
0	1	w ₀	w ₃	w ₂	w ₁
1	0	w ₁	w ₀	w ₃	w ₂
1	1	w ₂	w ₁	w ₀	w ₃



BV ex. 6.32

Sanningstabell:

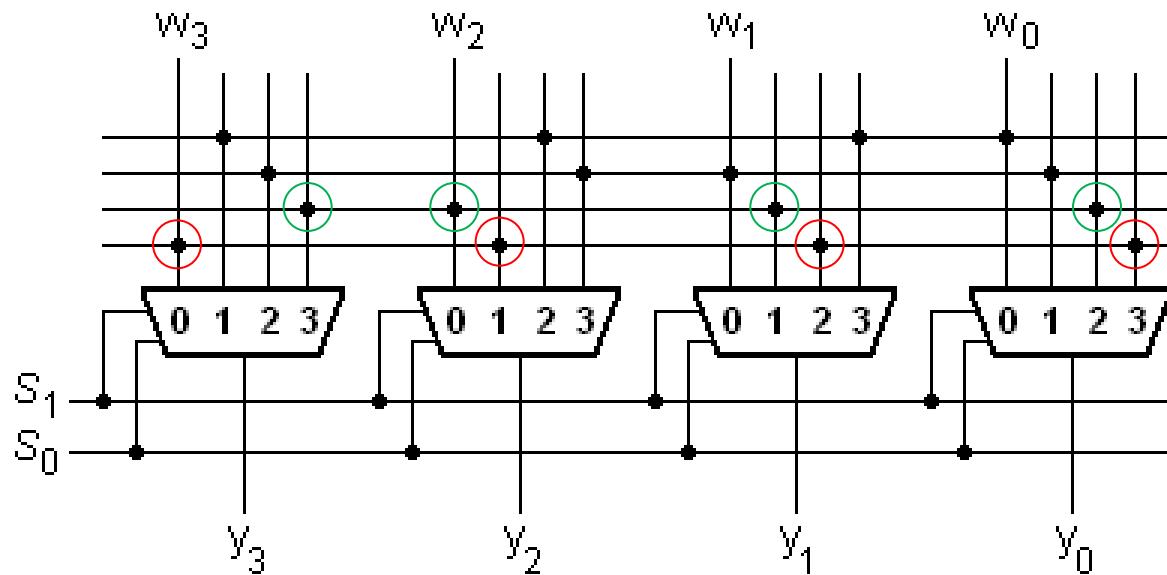
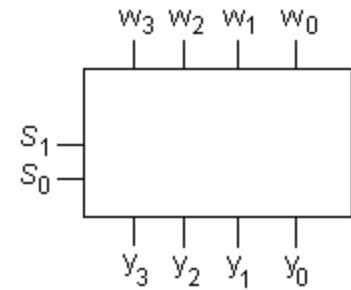
s_1	s_0	y_3	y_2	y_1	y_0
0	0	w ₃	w ₂	w ₁	w ₀
0	1	w ₀	w ₃	w ₂	w ₁
1	0	w ₁	w ₀	w ₃	w ₂
1	1	w ₂	w ₁	w ₀	w ₃



BV ex. 6.32

Sanningstabell:

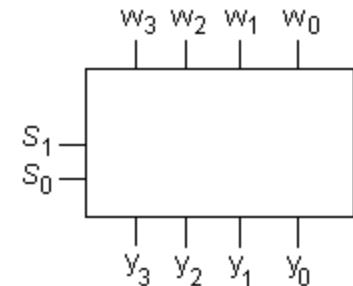
s_1	s_0	y_3	y_2	y_1	y_0
0	0	w ₃	w ₂	w ₁	w ₀
0	1	w ₀	w ₃	w ₂	w ₁
1	0	w ₁	w ₀	w ₃	w ₂
1	1	w ₂	w ₁	w ₀	w ₃



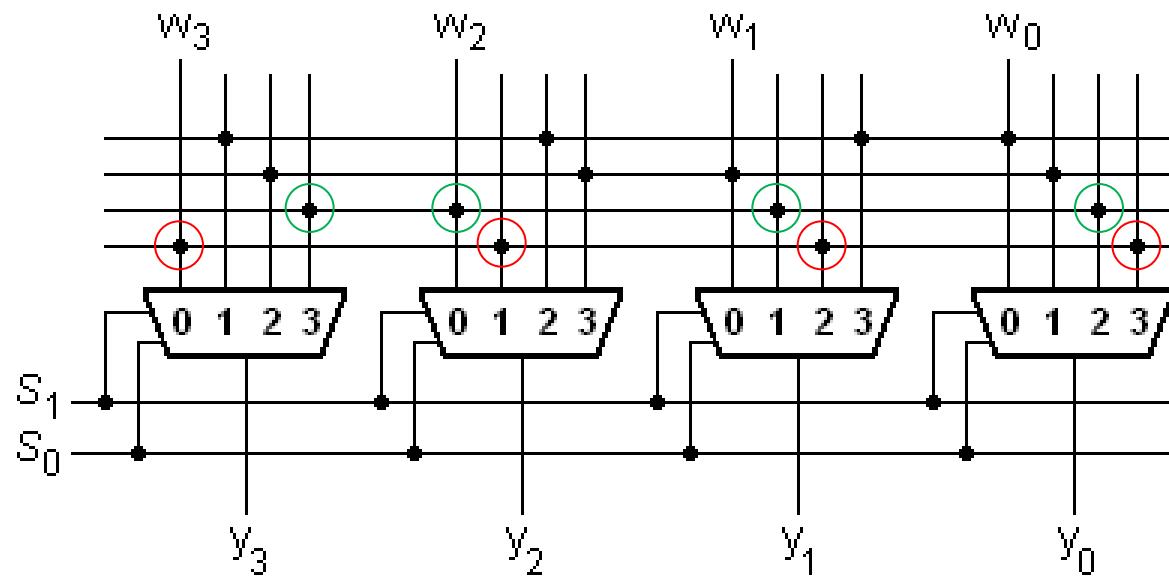
BV ex. 6.32

Sanningstabell:

$s_1 s_0$	y_3	y_2	y_1	y_0
0 0	w ₃	w ₂	w ₁	w ₀
0 1	w ₀	w ₃	w ₂	w ₁
1 0	w ₁	w ₀	w ₃	w ₂
1 1	w ₂	w ₁	w ₀	w ₃



Och så vidare ...



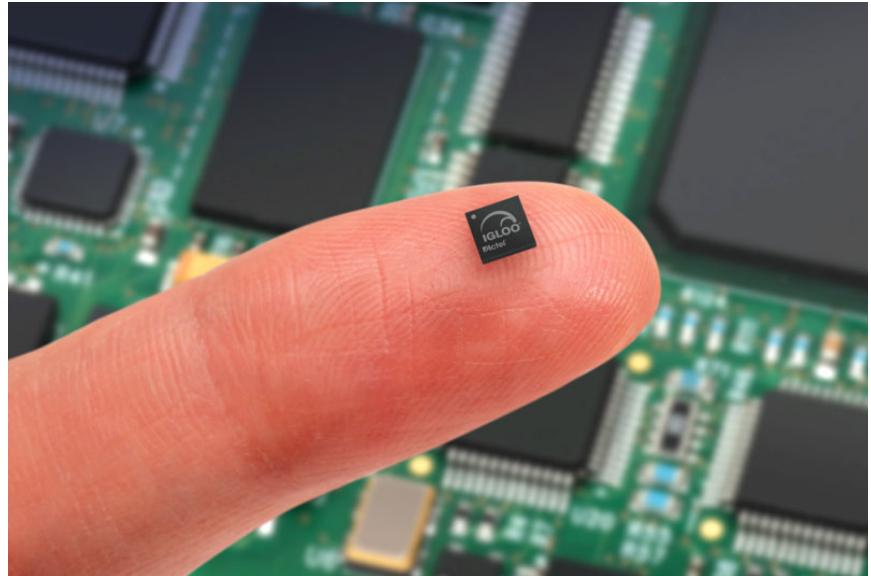
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= Lågpris FPGA

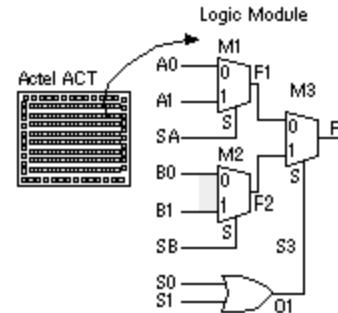


Key Benefits

- Lowest FPGA unit cost starting at **\$0.49**
- Ultra-low power in Flash*Freeze mode, as low as 2 µW
- Nonvolatile FPGA eliminates unnecessary parts from BOM
- Single-chip and ultra-low-power products simplify board design
- Variety of cost-optimized packages reduce assembly costs
- Low-power FPGAs reduce thermal management and cooling needs



BV 6.16



Actel Corporation manufactures an FPGA family called Act 1, which uses multiplexer based logic blocks. Show how the function

$$f = w_2 \overline{w_3} + w_1 w_3 + \overline{w_2} w_3$$

can be implemented using only ACT 1 logic blocks.

BV 6.16

$$f = w_2 \overline{w_3} + w_1 w_3 + \overline{w_2} w_3$$

BV 6.16

$$f = w_2 \overline{w_3} + w_1 w_3 + \overline{w_2} w_3$$

$$f = \overline{w_3}(w_2) + w_3(w_1 + \overline{w_2})$$

$$\overline{w_3}(w_2) = \overline{w_3}(\overline{w_2} \cdot 0 + w_2 \cdot 1)$$

$$w_3(w_1 + \overline{w_2}) = w_3\left(w_1(w_2 + \overline{w_2}) + \overline{w_2}\right) = w_3\left(w_2 w_1 + \overline{w_2} w_1 + \overline{w_2}\right) =$$

$$= w_3\left(w_2 w_1 + \overline{w_2}(w_1 + 1)\right) = w_3\left(\overline{w_2} \cdot 1 + w_2 \cdot w_1\right)$$

$$f = \overline{w_3}(\overline{w_2} \cdot 0 + w_2 \cdot 1) + w_3\left(\overline{w_2} \cdot 1 + w_2 \cdot w_1\right)$$

BV 6.16

$$f = w_2 \overline{w_3} + w_1 w_3 + \overline{w_2} w_3$$

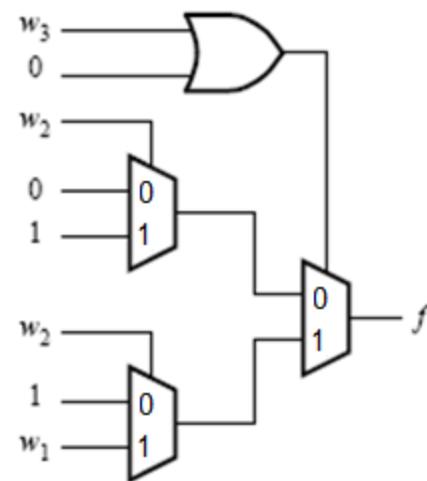
$$f = \overline{w_3}(w_2) + w_3(w_1 + \overline{w_2})$$

$$\overline{w_3}(w_2) = \overline{w_3}(\overline{w_2} \cdot 0 + w_2 \cdot 1)$$

$$w_3(w_1 + \overline{w_2}) = w_3\left(w_1(w_2 + \overline{w_2}) + \overline{w_2}\right) = w_3\left(w_2 w_1 + \overline{w_2} w_1 + \overline{w_2}\right) =$$

$$= w_3\left(w_2 w_1 + \overline{w_2}(w_1 + 1)\right) = w_3\left(\overline{w_2} \cdot 1 + w_2 \cdot w_1\right)$$

$$f = \overline{w_3}(\overline{w_2} \cdot 0 + w_2 \cdot 1) + w_3\left(\overline{w_2} \cdot 1 + w_2 \cdot w_1\right)$$



BV 6.16

$$f = w_2 \overline{w_3} + w_1 w_3 + \overline{w_2} w_3$$

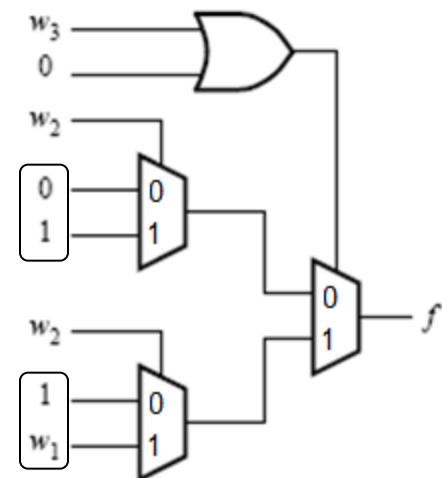
$$f = \overline{w_3}(w_2) + w_3(w_1 + \overline{w_2})$$

$$\overline{w_3}(w_2) = \overline{w_3}(\overline{w_2} \cdot 0 + w_2 \cdot 1)$$

$$w_3(w_1 + \overline{w_2}) = w_3(w_1(w_2 + \overline{w_2}) + \overline{w_2}) = w_3(w_2 w_1 + \overline{w_2} w_1 + \overline{w_2}) =$$

$$= w_3(w_2 w_1 + \overline{w_2}(w_1 + 1)) = w_3(\overline{w_2} \cdot 1 + w_2 \cdot w_1)$$

$$f = \overline{w_3}(\overline{w_2} \cdot \boxed{0} + w_2 \boxed{1}) + w_3(\overline{w_2} \boxed{1} + w_2 \cdot \boxed{w_1})$$



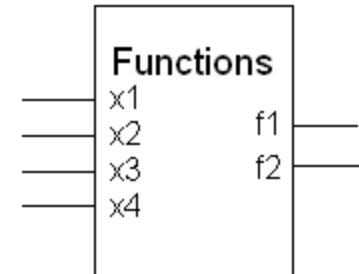
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VHDL BV 2.51a

Write VHDL code to describe the following functions

$$f_1 = x_1 \overline{x_3} + x_2 \overline{x_3} + \overline{x_3} \overline{x_4} + x_1 x_2 + x_1 \overline{x_4}$$

$$f_2 = (x_1 + \overline{x_3}) \cdot (x_1 + x_2 + \overline{x_4}) \cdot (x_2 + \overline{x_3} + \overline{x_4})$$



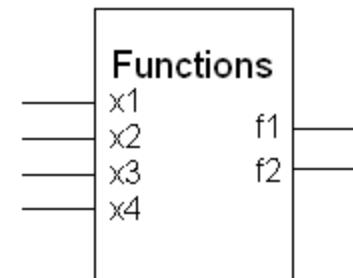
VHDL koden skrivs med en texteditor och sparas i en fil med ändelsen .vhd . Koden består alltid av två avsnitt ENTITY och ARCHITECTURE.

Entity är en beskrivning av hur kretsen ”ser ut utifrån” (gränssnittet), och Architecture hur den ”ser ut inuti.”

VHDL BV 2.51a

$$f_1 = x_1 \overline{x_3} + x_2 \overline{x_3} + \overline{x_3} \overline{x_4} + x_1 x_2 + x_1 \overline{x_4}$$

$$f_2 = (x_1 + \overline{x_3}) \cdot (x_1 + x_2 + \overline{x_4}) \cdot (x_2 + \overline{x_3} + \overline{x_4})$$



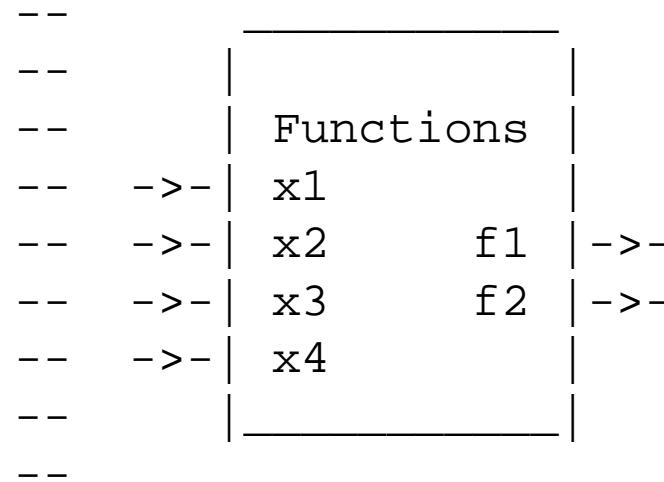
Programkod skrivas med texteditorer. Man kan därför bara göra textkommentarer till koden. Ett typsnitt med fast bredd används (ex. Courier New).

Kommentarer börjar med

--

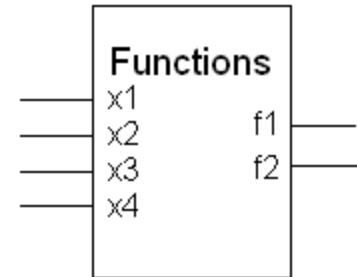
Om man vill, kan man "rita" förtydligande ASCII-grafik inom kommentarraderna.

Man brukar också indentera textblock som hör ihop för ökad tydlighet.



VHDL BV 2.51a

$$f_1 = x_1 \overline{x_3} + x_2 \overline{x_3} + \overline{x_3} \overline{x_4} + x_1 x_2 + x_1 \overline{x_4}$$
$$f_2 = (x_1 + \overline{x_3}) \cdot (x_1 + x_2 + \overline{x_4}) \cdot (x_2 + \overline{x_3} + \overline{x_4})$$



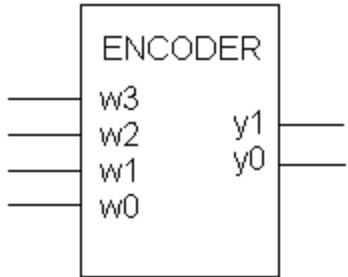
```
ENTITY Functions IS
  PORT(x1, x2, x3, x4 :IN STD_LOGIC;
        f1, f2,           :OUT STD_LOGIC )
```

```
END Functions
```

```
ARCHITECTURE LogicFunc OF Functions IS
BEGIN
  f1 <= (x1 AND NOT x3)OR(x2 AND NOT x3)OR
          (NOT x3 AND NOT x4)OR(x1 AND x2)OR
          (x1 AND NOT x4);
  f2 <= (x1 OR NOT x3)AND(x1 OR x2 OR NOT x4)AND
          (x2 OR NOT x3 OR NOT x4);
END LogicFunc ;
```

VHDL BV 6.21

Using a **selected** signal assignement, write VHDL code for a 4-to-2 binary encoder. Only one of w0 ...w3 is "1" at a time.

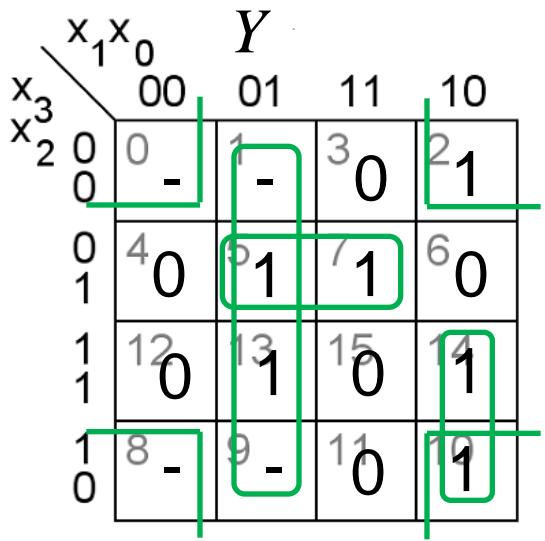


```
LIBRARY ieee;
USE IEEE.std_logic_1164.all;
ENTITY ENCODER IS
    PORT( w :IN STD_LOGIC_VECTOR( 3 DOWNTO 0 ) ;
          y :OUT STD_LOGIC_VECTOR( 1 DOWNTO 0 ) );
END ENCODER
ARCHITECTURE Behavior OF ENCODER IS
BEGIN
    WITH w SELECT
        y <= "00" WHEN "0001",
                    "01" WHEN "0010",
                    "10" WHEN "0100",
                    "11" WHEN OTHERS;
END Behavior ;
```

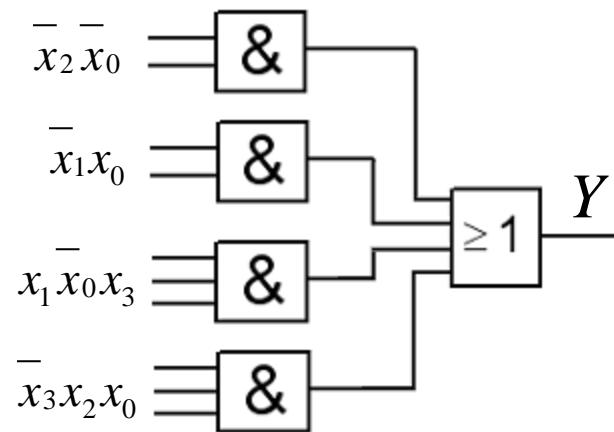
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(8.10) Extrauppgift

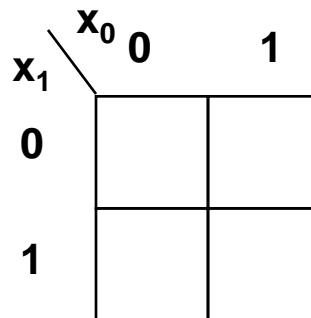
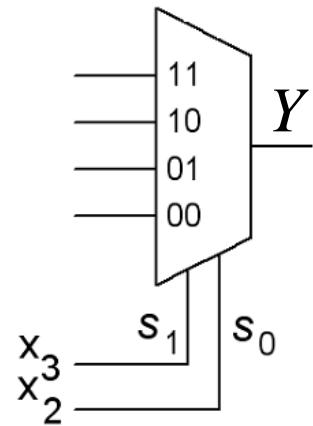
		Y			
		00	01	11	10
		00	01	11	10
x_3	0	0	1	3	2
	0	-	-	0	1
	1	4	5	7	6
	1	0	1	1	0
x_2	1	12	13	15	14
	0	0	1	0	1
x_1	0	8	9	11	10
	1	-	-	0	1



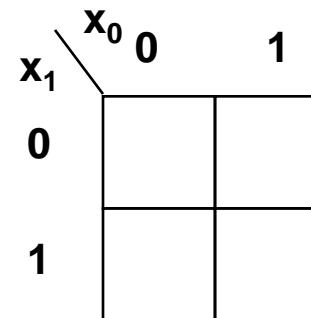
$$Y = \overline{x_2} \overline{x_0} + \overline{x_1} x_0 + x_1 \overline{x_0} x_3 + \overline{x_3} x_2 x_0$$



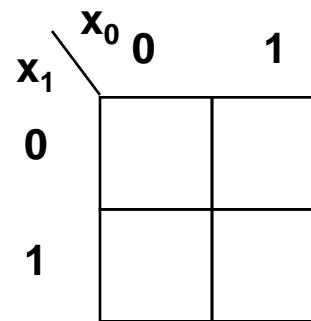
x_1	x_0	Y			
x_3	x_2	00	01	11	10
0	0	0	-	3	2
0	1	1	-	0	1
1	0	0	1	7	6
1	1	12	13	15	14
1	0	0	1	0	1
0	1	8	-	9	-
0	0	-	-	11	10



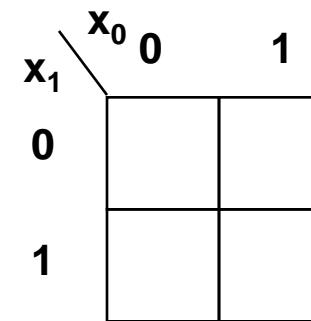
$$x_3x_2(0,0) \Rightarrow$$



$$x_3x_2(0,1) \Rightarrow$$

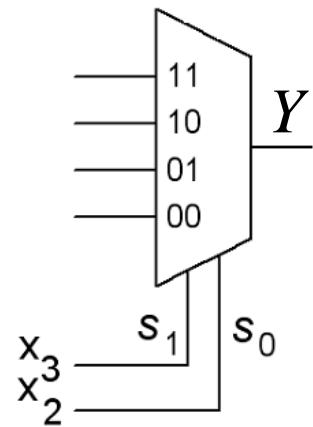


$$x_3x_2(1,1) \Rightarrow$$



$$x_3x_2(1,0) \Rightarrow$$

x_1	x_0	Y			
x_3	x_2	00	01	11	10
0	0	0	-	3	2
0	1	1	-	0	1
1	0	0	1	7	6
1	1	1	0	15	14
1	0	0	-	13	10
0	1	1	0	9	-
1	1	0	1	11	0
0	0	1	0	-	8



x_1	x_0	0	1
0	-	-	
1	1	0	

$$x_3 x_2(0,0) \Rightarrow$$

x_1	x_0	0	1
0	0	1	
1	0	1	

$$x_3 x_2(0,1) \Rightarrow$$

x_1	x_0	0	1
0	0	1	
1	1	0	

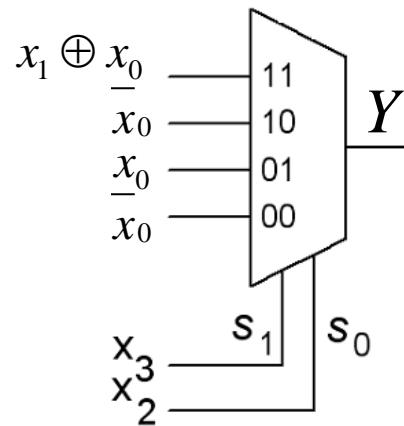
$$x_3 x_2(1,1) \Rightarrow$$

x_1	x_0	0	1
0	-	-	
1	1	0	

$$x_3 x_2(1,0) \Rightarrow$$

x_3	x_2	x_1	x_0	Y
0	00	01	11	10
1	-	-	3	2
0	4	5	7	6
1	12	13	15	14
0	8	9	11	10

$$Y = \overline{x_2} \overline{x_0} + \overline{x_1} x_0 + x_1 \overline{x_0} x_3 + \overline{x_3} x_2 x_0$$



x_1	x_0	1
0	-	-
1	1	0

$$x_3 x_2(0,0) \Rightarrow \\ Y = \overline{x_0}$$

x_1	x_0	1
0	0	1
1	0	1

$$x_3 x_2(0,1) \Rightarrow \\ Y = x_0$$

x_1	x_0	1
0	0	1
1	1	0

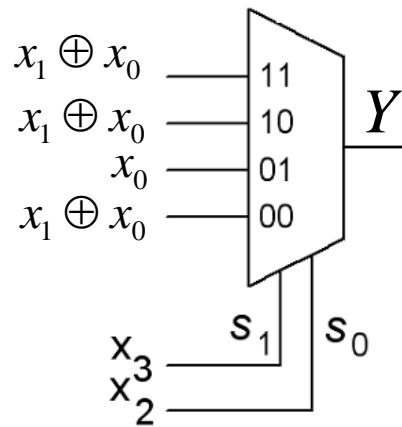
$$x_3 x_2(1,1) \Rightarrow \\ Y = x_1 \oplus x_0$$

x_1	x_0	1
0	-	-
1	1	0

$$x_3 x_2(1,0) \Rightarrow \\ Y = \overline{x_0}$$

x_3	x_2	x_1	x_0	Y
0	0	0	0	0
0	0	0	1	1
0	0	1	0	3
0	0	1	1	2
0	1	0	0	4
0	1	0	1	5
0	1	1	-	7
0	1	1	-	6
1	1	0	-	12
1	1	0	-	13
1	1	1	-	15
1	1	1	-	14
1	0	0	-	8
1	0	0	-	9
1	0	1	-	11
1	0	1	-	10

$$Y = \overline{x_2}x_0 + \overline{x_1}x_0 + x_1\overline{x_0}x_3 + \overline{x_3}x_2x_0$$



Eller ...

x_1	x_0	0	1
0	-	-	-
1	1	0	-

$$x_3x_2(0,0) \Rightarrow \\ Y = x_1 \oplus x_0$$

x_1	x_0	0	1
0	0	1	-
1	0	1	-

$$x_3x_2(0,1) \Rightarrow \\ Y = x_0$$

x_1	x_0	0	1
0	0	1	-
1	1	0	-

$$x_3x_2(1,1) \Rightarrow \\ Y = x_1 \oplus x_0$$

x_1	x_0	0	1
0	-	-	-
1	1	0	-

$$x_3x_2(1,0) \Rightarrow \\ Y = x_1 \oplus x_0$$

Eller om det är svårt att få tag i x_0 inverterad ...

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