

**ERRATA**  
for *Enumerative Combinatorics*, vol. 1, 2nd ed., 2012

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- page 5, line 9–. Insert “a” after “is”.
- page 23, line 6. Insert “a” after “is”.
- page 24, line 2. Change  $c_i$  to  $c_1$ .
- page 34, line 15. It should be stated that for this second way,  $d + 1$  cannot be inserted at the end even though  $d \notin D(w)$ .
- page 38, line 18. Change “does” to “do”.
- page 40, line 15. The intent of the parenthetical comment was to write the summation as

$$\sum_{g(4) \geq g(6)} \sum_{g(6) \geq g(3)} \cdots \sum_{g(5) \geq 0} q^{g(4)+\cdots+g(5)}.$$

We are actually first summing on  $g(5) \geq 0$ , then  $g(1) \geq g(5)$ , etc.

- page 40, line 4–. Insert  $\sum_{m \geq 0}$  before  $\sum_{w \in \mathfrak{S}_d}$ .
- page 43, line 4. Change “relection” to “reflection”.
- page 43, line 14. Change  $i \geq 0$  to  $i \geq 1$ .
- page 45, line 1. Change  $w$  to  $T(w)$ .
- page 47, line 11. Change  $n \geq 2$  to  $n \geq 1$ .
- page 49, lines 20–22. The two sentence beginning “Figure 1.10 . . .” and “Let  $f(n)$  denote . . .” should be interchanged, since  $f(n)$  is used in the first of these sentences but defined in the second.
- page 50 , line 4. Change “tree” to “trees”.
- page 53, line 1–. Change  $n$  to  $n - 1$ .
- page 54, line 8. Change “number” to “numbers”.

- page 62, equation (1.78). Change  $j \in \mathcal{S}_i$  to  $j \in S_i$ .
- page 62, line 13–. Change  $\mathcal{S}_j$  to  $S_i$ .
- page 65, line 7. Change proposition to Proposition.
- page 66, line 13. Change  $F(0, q)$  to  $F(x, 0)$ .
- page 68, line 17–. Change “ $k$  of the  $\gamma_i$ ’s to “ $k$   $\gamma_i$ ’s”.
- page 71, line 2–. Change “then then” to “then the”.
- page 76, line 2. Change “ $x$  to  $-x$ ” to “ $t$  to  $-x$ ”.
- page 77, line 5–. Change “ $f(0), f(0)$ ” to “ $f(0), f(1)$ ”.
- page 85, Theorem 1.10.4, line 3. Change  $\mathrm{GL}(n, q)$  to  $\mathrm{GL}(m, q)$ .
- page 85, Theorem 1.10.4, line 4. Change  $|\lambda(f)| \cdot \deg(f)$  to  $m = |\lambda(f)| \cdot \deg(f)$
- page 88, line 13–. Change  $v_{ij}$  to  $v_{1j}$ .
- page 98, line 7. Change “in the monograph” to “is the monograph”.
- page 115, Exercise 70(b), line 3. Change  $(1, 0)$  to  $(0, 1)$ , and change “i.e.” to “i.e.,”.
- page 120, Exercise 94, second bullet. Change “Then” to “The”.
- page 121, Exercise 96(c), line 3. Change 4.4.1.1 to 4.1.1.
- page 123, Exercise 116(b), line 2. Change distribuiton to distribution.
- page 126, Exercise 129(a), line 3. Add  $\sum_{k \geq 0}$  after  $\sum_{n \geq 1}$ .
- page 140, Exercise 198(b), last displayed equation. Change  $(q^{2m-1})$  to  $(q^{2m-1} - 1)$  (twice).
- page 166, Exercise 91(d), line 4. Replace this line with

$$1 + \sum_{n \geq 1} (-1)^n (x^{-n} - x^{n+1}) q^{n(n+1)/2}.$$

- page 169, Exercise 109(a), line 4. Change “is bijection” to “is a bijection”.
- page 171, line 4. The index entries for these four names is missing.
- page 173, Exercise 129. Change the parts **a** and **b** to **b** and **c**.
- page 173, Exercise 134, line 2. Change the period after Petersen to a comma.
- page 181, Exercise 164, line 1. Change  $x = 0$  to  $y = 0$ .
- page 190, Exercise 1.190(b), line 3. Replace this line with

$$\omega^*(n, q) = q^n - q^m - q^{m-1} - q^{m-2} - \dots - q^{\lfloor n/3 \rfloor} + O(q^{\lfloor n/3 \rfloor - 1}).$$

- page 195, line 9–. Change “example” to “examples”.
- page 196, equation (2.5). Change  $Y \supseteq T$  to  $Y \supseteq \emptyset$  or to just  $Y$ .
- page 198, line 2. This line should read:

function  $f_-$  satisfies  $f_-(T) = f_-(T')$  whenever  $\#T = \#T'$ . Thus also  $f_{\geq}(T)$

- page 199, line 11–. Change “ $i$  set” to “ $i$ -set”.
- page 199, line 3–. Change  $S - T$  to  $S_n - T$ .
- page 200, line 8. Change  $j \geq i$  to  $j \leq i$ .
- page 203, line 6. Insert  $)$  before  $\}$ .
- page 203, line 13. Change “nonattacking” to “nonattacking”.
- page 203, line 4–. Change “is” to “in”.
- page 205, line 2–. Change  $n - k - 1$  to  $n - k + 1$ .
- page 206, line 9. Change “suggest” to “suggests”.
- page 207, line 4–. Change  $x - s_1$  to  $x + s_1$ .
- page 208, line 10–. Change “ $a_3$ ’s” to “ $a_3$  3’s”.

- page 210, line 9. Insert “one for 121,” after “one for 112.”.
- page 210, line 9–. Insert  $=$  between  $d(n)$  and  $\#D_n$ .
- page 212, line 9–. Change  $T \subseteq S$  to  $Y \subseteq S$ .
- page 216, line 5–. Insert  $)$  after  $x_{\gamma_i}$ .
- page 222, Exercise 10(b), lines 1 and 2. Change  $E(n)/n!$  to  $E(n)/n^n$  (twice).
- page 227, line 3–. On the left-hand side of the formula, remove one  $\sum_{i \geq 0}$  and change  $y^i$  to  $t^i$ .
- page 229, Exercise 29(a), line 4. Change “partitions” to “compositions”.
- page 235, Exercise 10(b), line 9. Change  $E(n)/n!$  to  $E(n)/n^n$ .
- page 237, Exercise 19. Change  $\binom{2n-k}{k}$  to  $\binom{2n}{2n-k} \binom{2n-k}{k}$ .
- page 237, line 2–. Change second  $a_{n-k+1}$  to  $a_{n-k+2}$ .
- page 248, line 5–. Change “an” to “a”.
- page 249, Proposition 3.3.2, line 1. Change “condtions” to “condtions”.
- page 252, line 3. Insert “simple” before “matroids”.
- page 277, line 12–. Change  $\dim(W \cup W')$  to  $\dim(W + W')$ .
- page 283, lines 8– to 6–. Delete the sentence “Let  $\Lambda_t = \{s \in L(\mathcal{A}) : s \leq t\}$ , the principal order ideal generated by  $t$ .”
- page 284, line 3–. Delete “real” at the end of the line.
- page 284, line 2–. Insert “over  $K$ ” after “arrangements”.
- page 285, line 11. Under the second  $\Sigma$ , change  $\mathcal{B}_1 \in \mathcal{A}''$  to  $\mathcal{B}_1 \subseteq \mathcal{A}''$
- page 291, line 10–. Change “sketch that” to “reference for”.

- page 303, Theorem 3.15.8. To be completely accurate, one should assume that  $P \neq \emptyset$ .
- page 308, line 9. Change “an” to “and”.
- page 317, after (3.80). The phrase “(since intervals of Eulerian posets are Eulerian)” is unnecessary since the formulas under consideration hold for any graded poset with  $\hat{0}$  and  $\hat{1}$ .
- page 319, line 12–. Change  $Q_1 * Q_2 * \dots * Q_r$  to  $R_1 * R_2 * \dots * R_r$  (since  $Q_i$  already has been given another meaning).
- page 319, line 11–. Change the first  $Q_i$  to  $R_i$ .
- page 332, line 1–. Change  $\gamma_{j-1}$  to  $\gamma_{j-1}^2$ .
- page 332, bottom of page. Add the following paragraph:

The proof that  $(\gamma_j^*)^2 = 1$  is completely analogous. It also follows from the fact that  $\gamma_j^2 = 1$ , since we can assume without loss of generality that  $j = p - 1$  and then apply the automorphism of  $G$  that sends each  $\tau_k$  to  $\tau_{p-k}$ .

- page 334, line 4. Change  $z\delta$  to  $z\delta_{p-1}$ .
- page 336, line 11. Change  $\varphi: \widehat{KP} \rightarrow \widehat{KP}$  to  $\varphi: KP \rightarrow \widehat{KP}$ .
- page 337, lines 14– to 11–. The sentence “For the algebraically minded ... formal power series.” is not correct. We first need to consider non-commutative *polynomials* (not power series) and then pass to suitable completions.
- page 345, line 4. Change  $p_{s-1} + p_s$  to  $p_{j-1} + p_j$ .
- page 345, line 13. Change  $A$  to  $\mathbf{A}$  (boldface).
- page 360, Exercise 41(c,d). It is assumed that  $L$  is distributive.
- page 364, Exercise 55(b). The rating should be changed to [3–]. An exceptionally elegant proof was given by G. Stachowiak, *Order* 5 (1988), 257–259.

- page 378, Exercise 114(a). The answer should be

$$(x-1)(x-2)\cdots(x-n).$$

- page 379, Exercise 115(c), line 1. Change “0,1” to 0. (There are  $\binom{n}{2}$  hyperplanes.)
- page 379, Exercise 116. The subscripts should not be in boldface.
- page 390, Exercise 158(a), line 4. Change **a.** at beginning of line to **i..**
- page 390, Exercise 158(a), line 5. Change **b.** at beginning of line to **ii..**
- page 390, Exercise 158(c). Delete one of the periods at the end of the line.
- page 390, Exercise 158(d), line 2. Change “thats” to “that”.
- page 405, line 8–. The notation  $f_{00}$  is not defined until the next sentence.
- page 407, Exercise 205(b), line 2. Change 44605 to 44606 (private communication from Patrick Byrnes, 21 February 2012). Byrnes originally assumed that a vertex  $v$  could be covered by at most one singleton (element covering only  $v$ ), but there is exactly one example up to rank 9 where this property need not hold. Byrnes also computes that there are 29,199,636 1-differential posets up to rank 10.
- page 431, line 2–. Change **23** to **33**.
- page 449, Exercise 163(a), line 3. Change  $2e_P(p-1) - (p-1)e(p)$  to  $(2e_P(p-1) - (p-1)e(P))/p!$ .
- page 459, line 5–. Should be  $\beta_P(4, 5, 6) = -1$ .
- page 469, line 6–. Change  $\sum_{n \geq 0} f(n)$  to  $\sum_{n \geq 0} f(n)x^n$ .
- page 528, Exercise 4.2, line 3. Change “over” to “in”.
- page 530, Exercise 4.12. Change 0.00010203050813213455… to 0.0001010203050813213455…, and change 1, 2, 3 to 1, 1, 2, 3.
- page 539, Exercise 47, line 1–. Change 1.1.8.6 to 1.8.6.

- page 542, line 10. Delete  $)$  after  $u_6$ .
- page 548, Exercise 2(a), line 6. The assertion “Clearly, we can write  $f(x) = P(x)/Q(x)$  for some relatively prime integer polynomials  $P$  and  $Q$ .” is not so clear. One must show that if  $F(x) \in \mathbb{Q}[[x]]$  and  $F(x) = R(x)/S(x)$  where  $R, S \in \mathbb{C}[x]$ , then one can write  $F(x) = P(x)/Q(x)$  where  $P, Q \in \mathbb{Q}[x]$ . This statement does have a fairly simple proof, which we leave as an exercise.
- page 549, line 1–. Change  $x^{m^2}$  to  $x^{n^2}$ .
- page 552, Exercise 14. The smallest known pair  $(a, b)$  seems to be
$$\begin{aligned} a &= 106276436867 = 31 \cdot 3128272157 \\ b &= 35256392432 = 2^4 \cdot 2203524527 \end{aligned}$$

due to M. Vsemirnov, *J. Integer Seq.* **7** (2004), article 04.3.7.
- page 558, line 1. Delete comma after *Wochenschrift*.
- page 558, Exercise 43. The sequence  $t(3), t(4), \dots$  is known as *Alcuin’s sequence*, after Alcuin of York (730s or 740s – 19 May 804). For a survey see D. J. Bindner and M. Erickson, *Amer. Math. Monthly* **119** (2012), 115–121.
- page 560, Exercise 46(b), line 1. Delete the first “many”.
- page 560, Exercise 46(b), line 2. Change  $f(n+1), f(n+2), \dots, f(n+d)$  to  $“(f(n+1), f(n+2), \dots, f(n+d))$  for fixed  $d”$ .
- page 564, Exercise 58(f), line 1. Change “order polynomials” to “Ehrhart polynomials”.
- page 567, Exercise 75(c), line 1. Delete “directed”.
- page 569, Exercise 80, displayed equation, line 1. Change  $v'_i y$  to  $v_i y$ .
- page 571, line 3. Change “chose” to “chosen”.
- page 579. The following two items are missing: First edition—Supplementary Exercise 3.19 = Second edition—Exercise 3.44; and First edition—Supplementary Exercise 3.10 = Second edition—Exercise 3.63.