

ERRATA

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- page 5, line 9–. Insert “a” after “is”.
- page 23, line 6. Insert “a” after “is”.
- page 24, line 2. Change c_i to c_1 .
- page 34, line 15. It should be stated that for this second way, $d + 1$ cannot be inserted at the end even though $d \notin D(w)$.
- page 38, line 18. Change “does” to “do”.
- page 40, line 15. The intent of the parenthetical comment was to write the summation as

$$\sum_{g(4) \geq g(6)} \sum_{g(6) \geq g(3)} \cdots \sum_{g(5) \geq 0} q^{g(4) + \cdots + g(5)}.$$

We are actually first summing on $g(5) \geq 0$, then $g(1) \geq g(5)$, etc.

- page 40, line 4–. Insert $\sum_{m \geq 0}$ before $\sum_{w \in \mathfrak{S}_d}$.
- page 43, line 4. Change “relection” to “reflection”.
- page 43, line 14. Change $i \geq 0$ to $i \geq 1$.
- page 45, line 1. Change w to $T(w)$.
- page 47, line 11. Change $n \geq 2$ to $n \geq 1$.
- page 49, lines 20–22. The two sentence beginning “Figure 1.10 ...” and “Let $f(n)$ denote ...” should be interchanged, since $f(n)$ is used in the first of these sentences but defined in the second.
- page 50 , line 4. Change “tree” to “trees”.
- page 53, line 1–. Change n to $n - 1$.
- page 54, line 8. Change “number” to “numbers”.

- page 62, equation (1.78). Change $j \in \mathcal{S}_i$ to $j \in S_i$.
- page 62, line 13–. Change \mathcal{S}_j to S_i .
- page 65, line 7. Change proposition to Proposition.
- page 66, line 13. Change $F(0, q)$ to $F(x, 0)$.
- page 68, line 17–. Change “ k of the γ_i ’s” to “ k γ_i ’s”.
- page 71, line 2–. Change “then then” to “then the”.
- page 76, line 2. Change “ x to $-x$ ” to “ t to $-x$ ”.
- page 77, line 5–. Change “ $f(0), f(0)$ ” to “ $f(0), f(1)$ ”.
- page 85, Theorem 1.10.4, line 3. Change $\text{GL}(n, q)$ to $\text{GL}(m, q)$.
- page 85, Theorem 1.10.4, line 4. Change $|\lambda(f)| \cdot \deg(f)$ to $m = |\lambda(f)| \cdot \deg(f)$.
- page 88, line 13–. Change v_{ij} to v_{1j} .
- page 98, line 7. Change “in the monograph” to “is the monograph”.
- page 115, Exercise 70(b), line 3. Change $(1, 0)$ to $(0, 1)$, and change “i.e.” to “i.e.,”.
- page 120, Exercise 94, second bullet. Change “Then” to “The”.
- page 121, Exercise 96(c), line 3. Change 4.4.1.1 to 4.1.1.
- page 123, Exercise 116(b), line 2. Change distribuiton to distribution.
- page 126, Exercise 129(a), line 3. Add $\sum_{k \geq 0}$ after $\sum_{n \geq 1}$.
- page 140, Exercise 198(b), last displayed equation. Change (q^{2m-1}) to $(q^{2m-1} - 1)$ (twice).
- page 166, Exercise 91(d), line 4. Replace this line with

$$1 + \sum_{n \geq 1} (-1)^n (x^{-n} - x^{n+1}) q^{n(n+1)/2}.$$

- page 169, Exercise 109(a), line 4. Change “is bijection” to “is a bijection”.
- page 171, line 4. The index entries for these four names is missing.
- page 173, Exercise 129. Change the parts **a** and **b** to **b** and **c**.
- page 173, Exercise 134, line 2. Change the period after Petersen to a comma.
- page 181, Exercise 164, line 1. Change $x = 0$ to $y = 0$.
- page 190, Exercise 1.190(b), line 3. Replace this line with

$$\omega^*(n, q) = q^n - q^m - q^{m-1} - q^{m-2} - \dots - q^{\lfloor n/3 \rfloor} + O(q^{\lfloor n/3 \rfloor - 1}).$$

- page 195, line 9–. Change “example” to “examples”.
- page 196, equation (2.5). Change $Y \supseteq T$ to $Y \supseteq \emptyset$ or to just Y .
- page 198, line 2. This line should read:
function $f_{=}$ satisfies $f_{=}(T) = f_{=}(T')$ whenever $\#T = \#T'$. Thus also $f_{\geq}(T)$
- page 199, line 11–. Change “ i set” to “ i -set”.
- page 199, line 3–. Change $S - T$ to $S_n - T$.
- page 200, line 8. Change $j \geq i$ to $j \leq i$.
- page 203, line 6. Insert $)$ before $\}$.
- page 203, line 13. Change “nonattacking” to “nonattacking”.
- page 203, line 4–. Change “is” to “in”.
- page 205, line 2–. Change $n - k - 1$ to $n - k + 1$.
- page 206, line 9. Change “suggest” to “suggests”.
- page 207, line 4–. Change $x - s_1$ to $x + s_1$.
- page 208, line 10–. Change “ a_3 ’s” to “ a_3 3’s”.

- page 210, line 9. Insert “one for 121,” after “one for 112,”.
- page 210, line 9–. Insert $=$ between $d(n)$ and $\#D_n$.
- page 212, line 9–. Change $T \subseteq S$ to $Y \subseteq S$.
- page 216, line 5–. Insert $)$ after x_{γ_i} .
- page 222, Exercise 10(b), lines 1 and 2. Change $E(n)/n!$ to $E(n)/n^n$ (twice).
- page 227, line 3–. On the left-hand side of the formula, remove one $\sum_{i \geq 0}$ and change y^i to t^i .
- page 229, Exercise 29(a), line 4. Change “partitions” to “compositions”.
- page 235, Exercise 10(b), line 9. Change $E(n)/n!$ to $E(n)/n^n$.
- page 237, Exercise 19. Change $\binom{2n-k}{k}$ to $\frac{2n}{2n-k} \binom{2n-k}{k}$.
- page 237, line 2–. Change second a_{n-k+1} to a_{n-k+2} .
- page 248, line 5–. Change “an” to “a”.
- page 249, Proposition 3.3.2, line 1. Change “condtions” to “conditions”.
- page 252, line 3. Insert “simple” before “matroids”.
- page 277, line 12–. Change $\dim(W \cup W')$ to $\dim(W + W')$.
- page 283, lines 8– to 6–. Delete the sentence “Let $\Lambda_t = \{s \in L(\mathcal{A}) : s \leq t\}$, the principal order ideal generated by t .”
- page 284, line 3–. Delete “real” at the end of the line.
- page 284, line 2–. Insert “over K ” after “arrangements”.
- page 285, line 11. Under the second Σ , change $\mathcal{B}_1 \in \mathcal{A}''$ to $\mathcal{B}_1 \subseteq \mathcal{A}''$.
- page 291, line 10–. Change “sketch that” to “reference for”.

- page 303, Theorem 3.15.8. To be completely accurate, one should assume that $P \neq \emptyset$.
- page 308, line 9. Change “an” to “and”.
- page 317, after (3.80). The phrase “(since intervals of Eulerian posets are Eulerian)” is unnecessary since the formulas under consideration hold for any graded poset with $\hat{0}$ and $\hat{1}$.
- page 319, line 12–. Change $Q_1 * Q_2 * \cdots * Q_r$ to $R_1 * R_2 * \cdots * R_r$ (since Q_i already has been given another meaning).
- page 319, line 11–. Change the first Q_i to R_i .
- page 332, line 1–. Change γ_{j-1} to γ_{j-1}^2 .
- page 332, bottom of page. Add the following paragraph:
The proof that $(\gamma_j^*)^2 = 1$ is completely analogous. It also follows from the fact that $\gamma_j^2 = 1$, since we can assume without loss of generality that $j = p - 1$ and then apply the automorphism of G that sends each τ_k to τ_{p-k} .
- page 334, line 4. Change $z\delta$ to $z\delta_{p-1}$.
- page 336, line 11. Change $\varphi: \widehat{KP} \rightarrow \widehat{KP}$ to $\varphi: KP \rightarrow \widehat{KP}$.
- page 337, lines 14– to 11–. The sentence “For the algebraically minded . . . formal power series.” is not correct. We first need to consider non-commutative *polynomials* (not power series) and then pass to suitable completions.
- page 345, line 4. Change $p_{s-1} + p_s$ to $p_{j-1} + p_j$.
- page 345, line 13. Change A to **A** (boldface).
- page 360, Exercise 41(c,d). It is assumed that L is distributive.
- page 364, Exercise 55(b). The rating should be changed to [3–]. An exceptionally elegant proof was given by G. Stachowiak, *Order* **5** (1988), 257–259.

- page 378, Exercise 114(a). The answer should be

$$(x-1)(x-2)\cdots(x-n).$$

- page 379, Exercise 115(c), line 1. Change “0,1” to 0. (There are $\binom{n}{2}$ hyperplanes.)
- page 379, Exercise 116. The subscripts should not be in boldface.
- page 390, Exercise 158(a), line 4. Change **a.** at beginning of line to **i.**
- page 390, Exercise 158(a), line 5. Change **b.** at beginning of line to **ii.**
- page 390, Exercise 158(c). Delete one of the periods at the end of the line.
- page 390, Exercise 158(d), line 2. Change “thats” to “that”.
- page 405, line 8–. The notation f_{00} is not defined until the next sentence.
- page 407, Exercise 205(b), line 2. Change 44605 to 44606 (private communication from Patrick Byrnes, 21 February 2012). Byrnes originally assumed that a vertex v could be covered by at most one singleton (element covering only v), but there is exactly one example up to rank 9 where this property need not hold. Byrnes also computes that there are 29,199,636 1-differential posets up to rank 10.
- page 431, line 2–. Change **23** to **33**.
- page 449, Exercise 163(a), line 3. Change $2e_P(p-1) - (p-1)e(p)$ to $(2e_P(p-1) - (p-1)e(P))/p!$.
- page 459, line 5–. Should be $\beta_P(4, 5, 6) = -1$.
- page 469, line 6–. Change $\sum_{n \geq 0} f(n)$ to $\sum_{n \geq 0} f(n)x^n$.
- page 528, Exercise 4.2, line 3. Change “over” to “in”.
- page 530, Exercise 4.12. Change 0.00010203050813213455... to 0.0001010203050813213455..., and change 1, 2, 3 to 1, 1, 2, 3.
- page 539, Exercise 47, line 1–. Change 1.1.8.6 to 1.8.6.

- page 542, line 10. Delete $)$ after u_6 .
- page 548, Exercise 2(a), line 6. The assertion “Clearly, we can write $f(x) = P(x)/Q(x)$ for some relatively prime integer polynomials P and Q .” is not so clear. One must show that if $F(x) \in \mathbb{Q}[[x]]$ and $F(x) = R(x)/S(x)$ where $R, S \in \mathbb{C}[x]$, then one can write $F(x) = P(x)/Q(x)$ where $P, Q \in \mathbb{Q}[x]$. This statement does have a fairly simple proof, which we leave as an exercise.
- page 549, line 1–. Change x^{m^2} to x^{n^2} .
- page 552, Exercise 14. The smallest known pair (a, b) seems to be

$$\begin{aligned} a &= 106276436867 = 31 \cdot 3128272157 \\ b &= 35256392432 = 2^4 \cdot 2203524527 \end{aligned}$$

due to M. Vsemirnov, *J. Integer Seq.* **7** (2004), article 04.3.7.

- page 558, line 1. Delete comma after *Wochenschrift*.
- page 558, Exercise 43. The sequence $t(3), t(4), \dots$ is known as *Alcuin’s sequence*, after Alcuin of York (730s or 740s – 19 May 804). For a survey see D. J. Bindner and M. Erickson, *Amer. Math. Monthly* **119** (2012), 115–121.
- page 560, Exercise 46(b), line 1. Delete the first “many”.
- page 560, Exercise 46(b), line 2. Change $f(n+1), f(n+2), \dots, f(n+d)$ to “ $(f(n+1), f(n+2), \dots, f(n+d))$ for fixed d ”.
- page 564, Exercise 58(f), line 1. Change “order polynomials” to “Ehrhart polynomials”.
- page 567, Exercise 75(c), line 1. Delete “directed”.
- page 569, Exercise 80, displayed equation, line 1. Change v'_iy to v_iy .
- page 571, line 3. Change “chose” to “chosen”.
- page 579. The following two items are missing: First edition—Supplementary Exercise 3.19 = Second edition—Exercise 3.44; and First edition—Supplementary Exercise 3.10 = Second edition—Exercise 3.63.