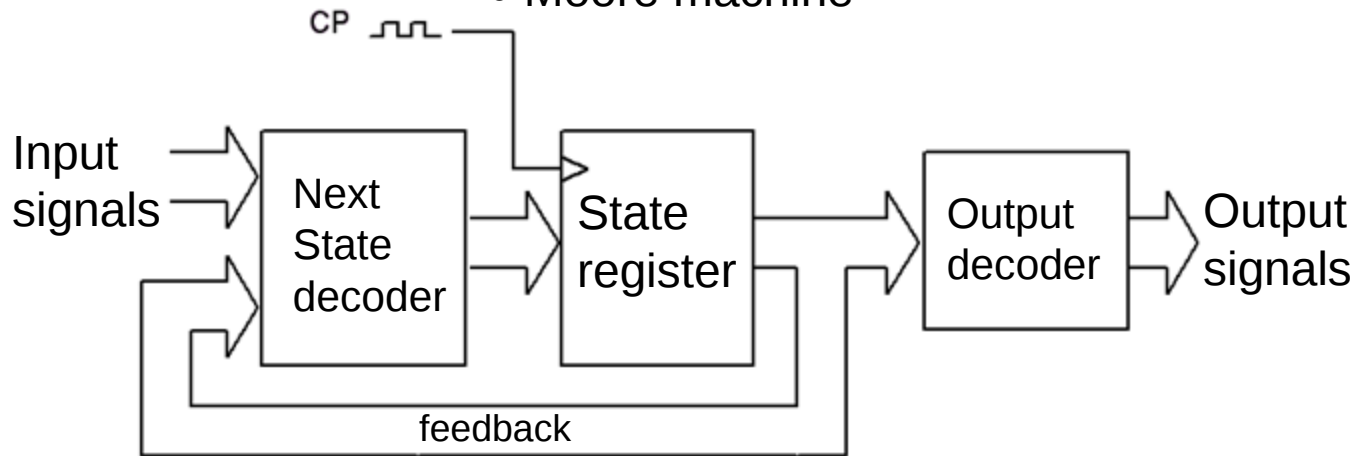
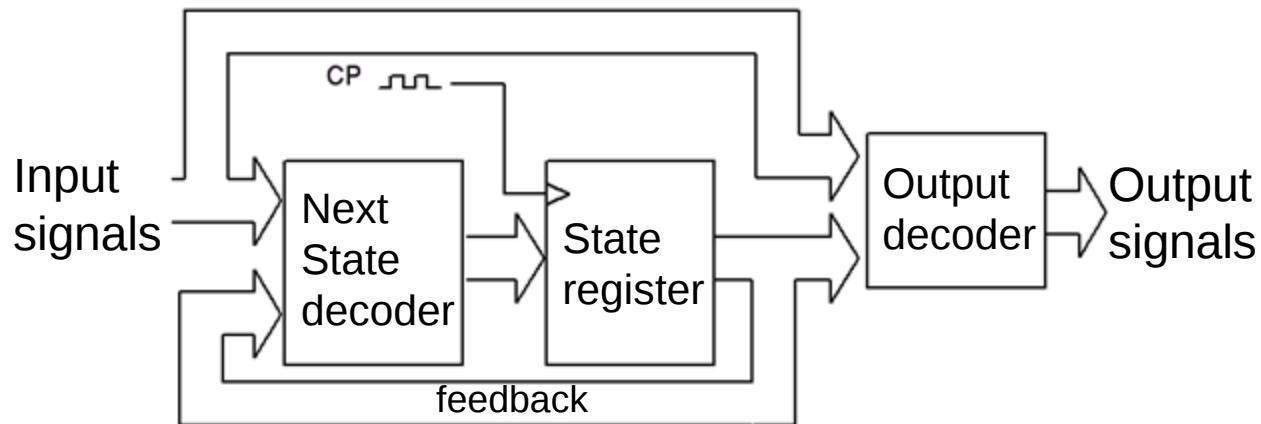


# Statemachines

- Moore machine



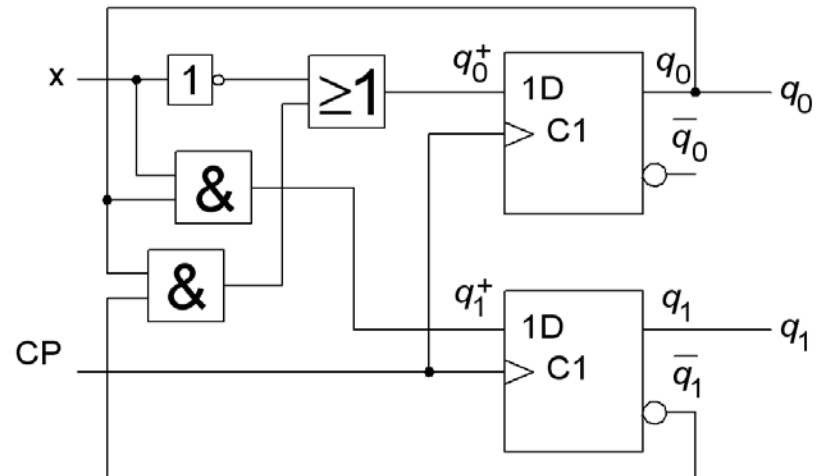
- Mealy machine



# Ex 10.1

Determine the state diagram and state table for the sequential circuit.

Which of the models Mealy or Moore fits the circuit?



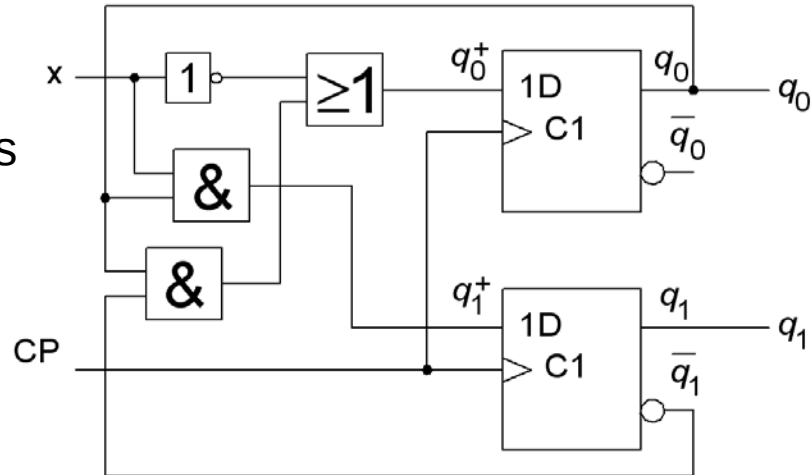
# 10.1

From the schematic, the following equations can be set up:

$q_1$   $q_0$  output signals

$$q_1^+ = x \cdot q_0$$

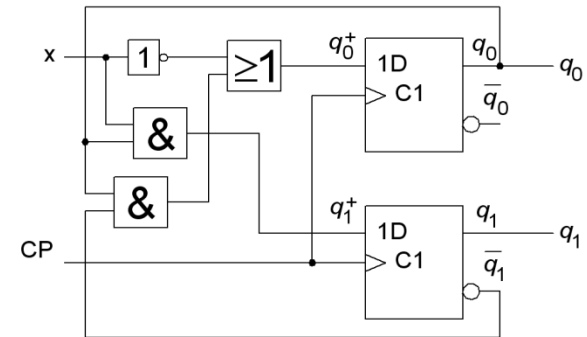
$$q_0^+ = \bar{x} + \bar{q}_1 \cdot q_0$$



No output decoder is used, the state of the flip-flops are used directly as output. **Moore**-model is used.

# 10.1

$$q_1^+ = x \cdot q_0 \quad q_0^+ = \bar{x} + \bar{q}_1 \cdot q_0$$



$q_1^+ = x q_0$ 

|           |    |     |   |
|-----------|----|-----|---|
|           |    | $x$ |   |
|           |    | 0   | 1 |
| $q_1 q_0$ | 00 |     |   |
|           | 01 |     | 1 |
|           | 11 |     | 1 |
|           | 10 |     |   |

$x q_0$  → (points to the 1 in row 01, column 1)

$q_0^+ = \bar{q}_1 q_0 + \bar{x}$ 

|           |    |     |   |
|-----------|----|-----|---|
|           |    | $x$ |   |
|           |    | 0   | 1 |
| $q_1 q_0$ | 00 | 1   |   |
|           | 01 | 1   | 1 |
|           | 11 | 1   |   |
|           | 10 | 1   |   |

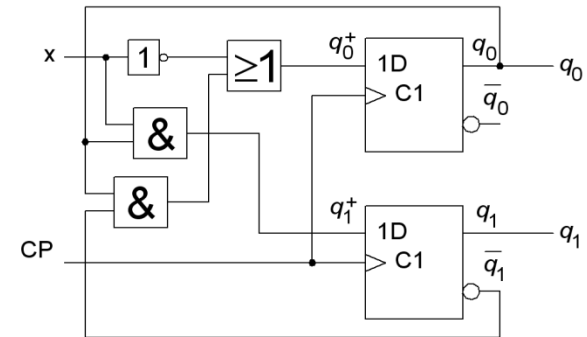
$\bar{x}$  → (points to the 1 in row 11, column 0)

$q_1^+ q_0^+ (q_1 q_0 x)$ 

|           |    |     |   |
|-----------|----|-----|---|
|           |    | $x$ |   |
|           |    | 0   | 1 |
| $q_1 q_0$ | 00 |     |   |
|           | 01 |     |   |
|           | 11 |     |   |
|           | 10 |     |   |

# 10.1

$$q_1^+ = x \cdot q_0 \quad q_0^+ = \bar{x} + \bar{q}_1 \cdot q_0$$



$q_1^+ = x \cdot q_0$

|           |    | $x$ |   |
|-----------|----|-----|---|
|           |    | 0   | 1 |
| $q_1 q_0$ | 00 |     |   |
|           | 01 |     | 1 |
|           | 11 |     | 1 |
|           | 10 |     |   |

$x \cdot q_0$  points to the 1 in the 01 row, 1 column.

$q_0^+ = \bar{q}_1 q_0 + \bar{x}$

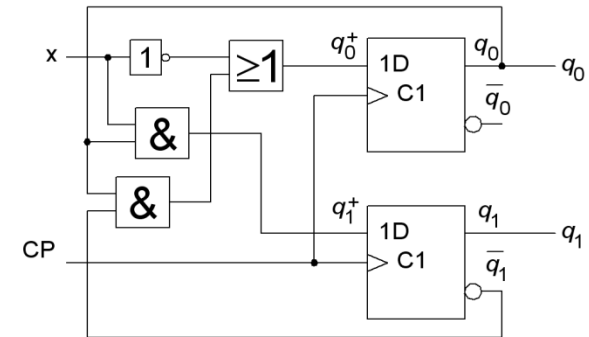
|           |    | $x$ |   |
|-----------|----|-----|---|
|           |    | 0   | 1 |
| $q_1 q_0$ | 00 | 1   |   |
|           | 01 | 1   | 1 |
|           | 11 | 1   |   |
|           | 10 | 1   |   |

$\bar{q}_1 q_0$  points to the 1 in the 00 row, 0 column.  
 $\bar{x}$  points to the 1 in the 11 row, 0 column.

$q_1^+ q_0^+ (q_1 q_0 x)$

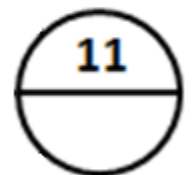
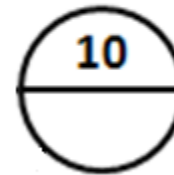
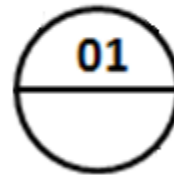
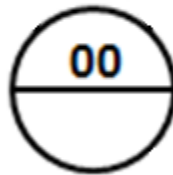
|           |    | $x$ |    |
|-----------|----|-----|----|
|           |    | 0   | 1  |
| $q_1 q_0$ | 00 | 01  | 00 |
|           | 01 | 01  | 11 |
|           | 11 | 01  | 10 |
|           | 10 | 01  | 00 |

# 10.1

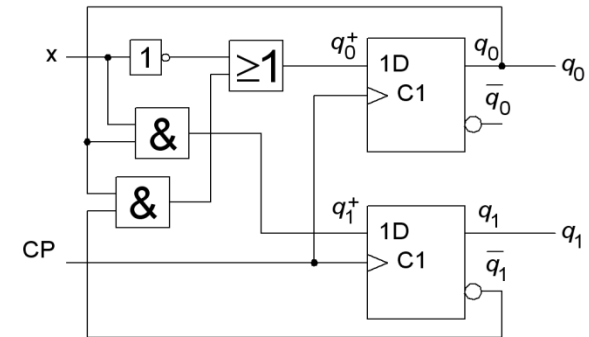


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

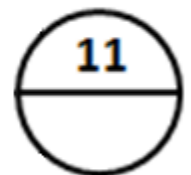
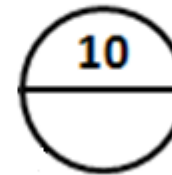
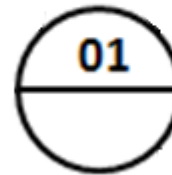
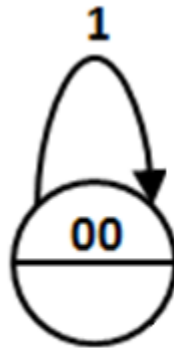


# 10.1

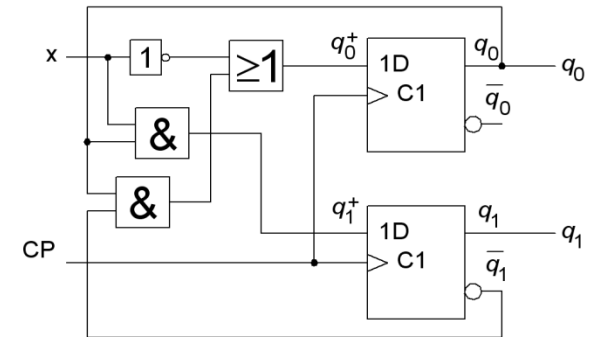


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

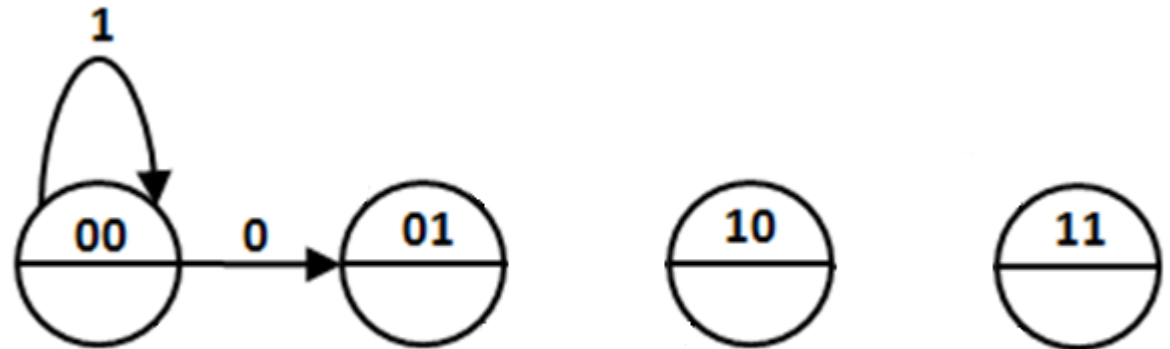


# 10.1

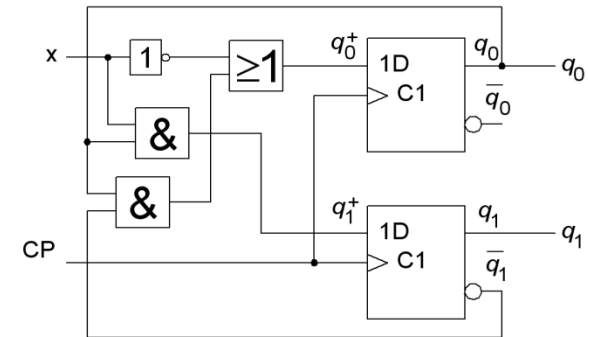


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

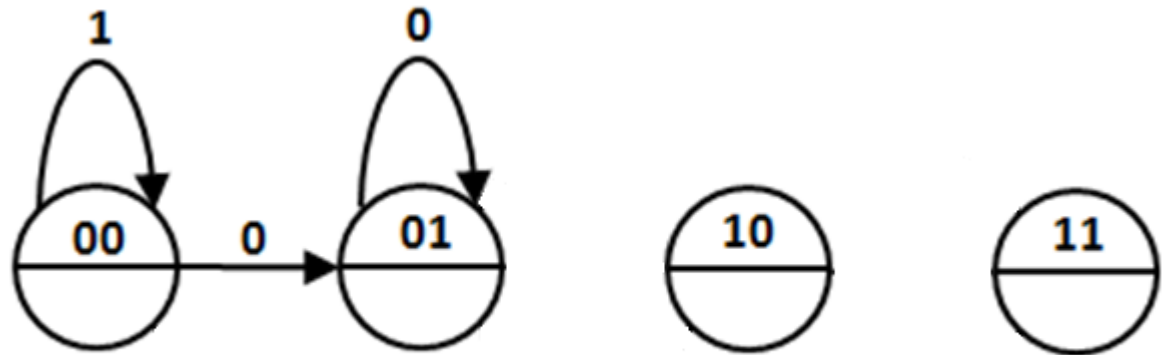


# 10.1

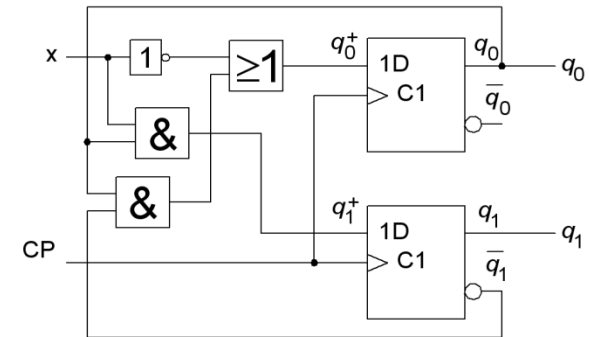


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

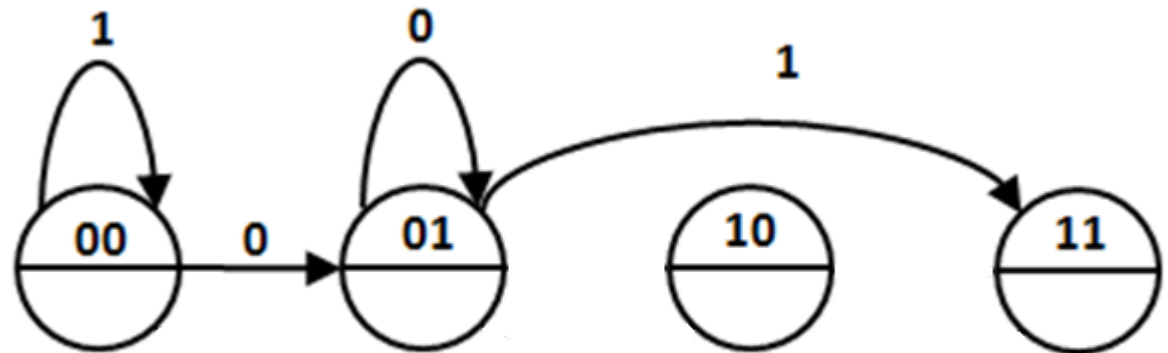


# 10.1

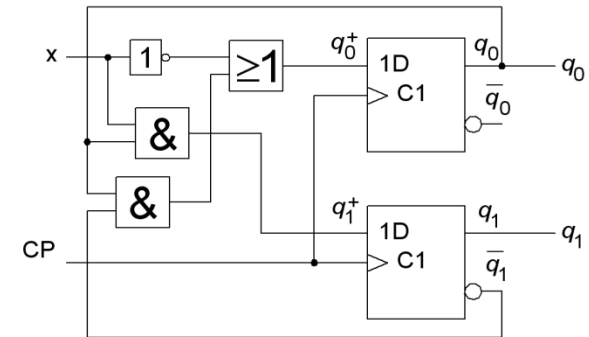


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

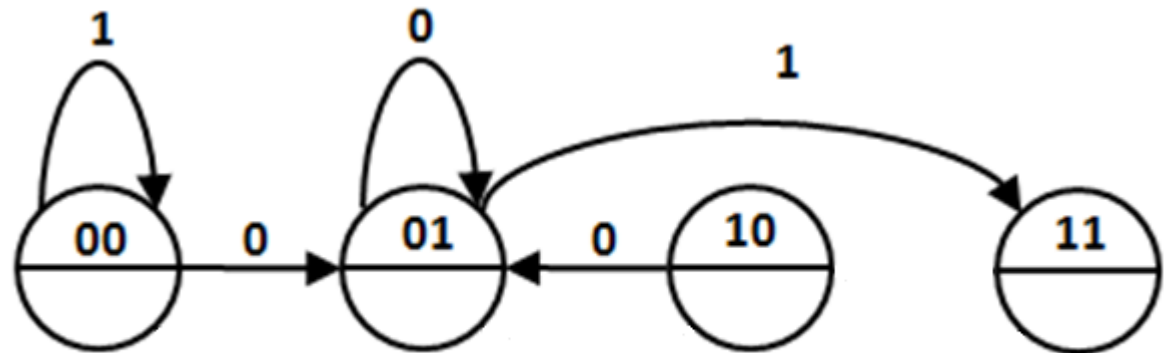


# 10.1

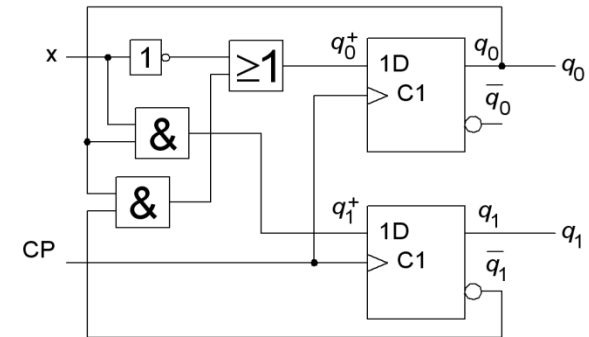


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

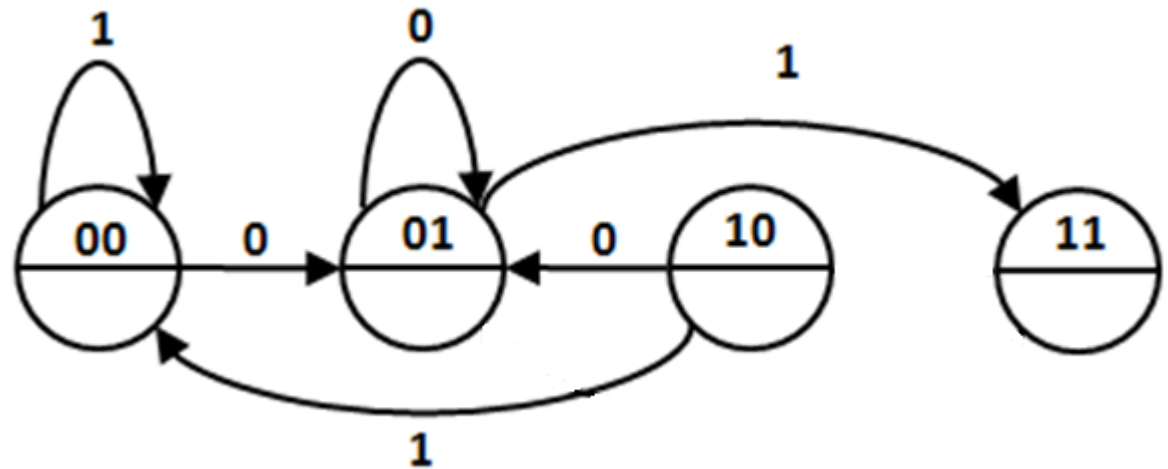


# 10.1

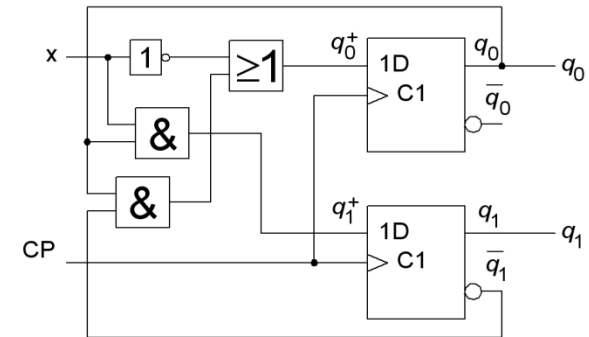


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

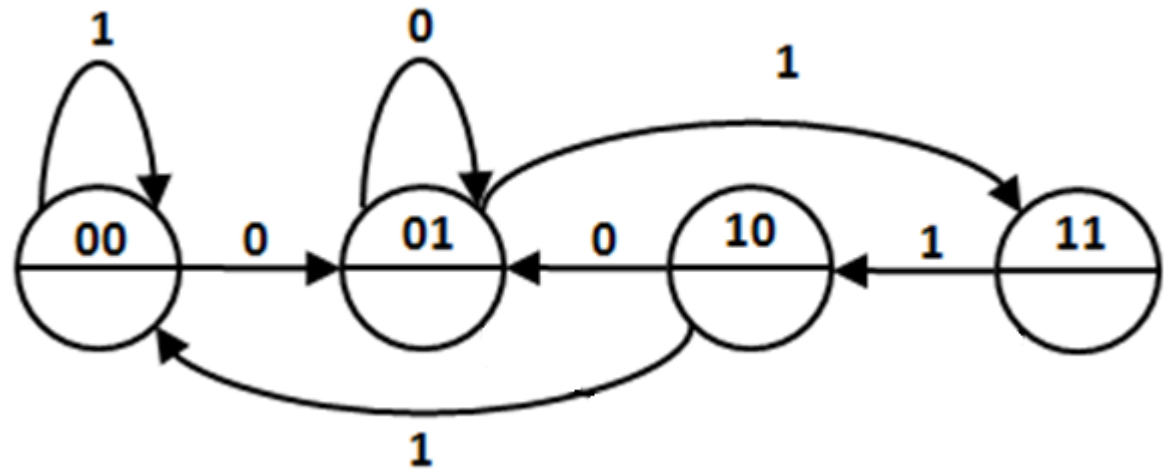


# 10.1

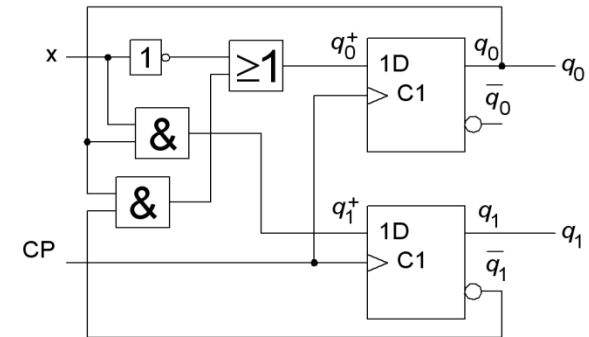


$q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |

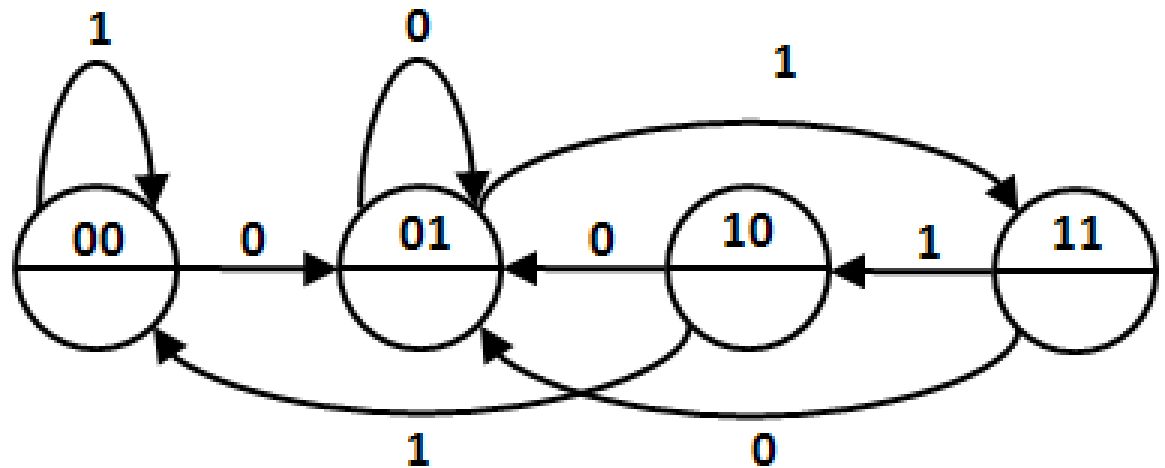


# 10.1

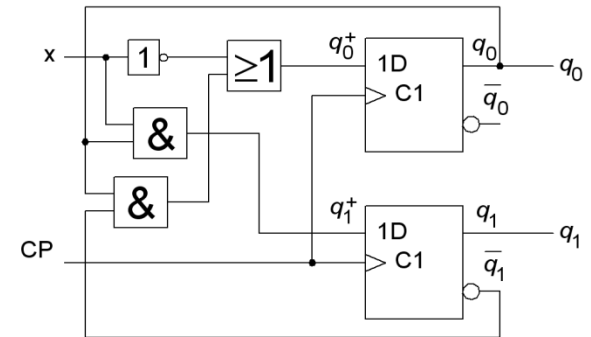


$q_1^+ q_0^+ (q_1 q_0 x)$

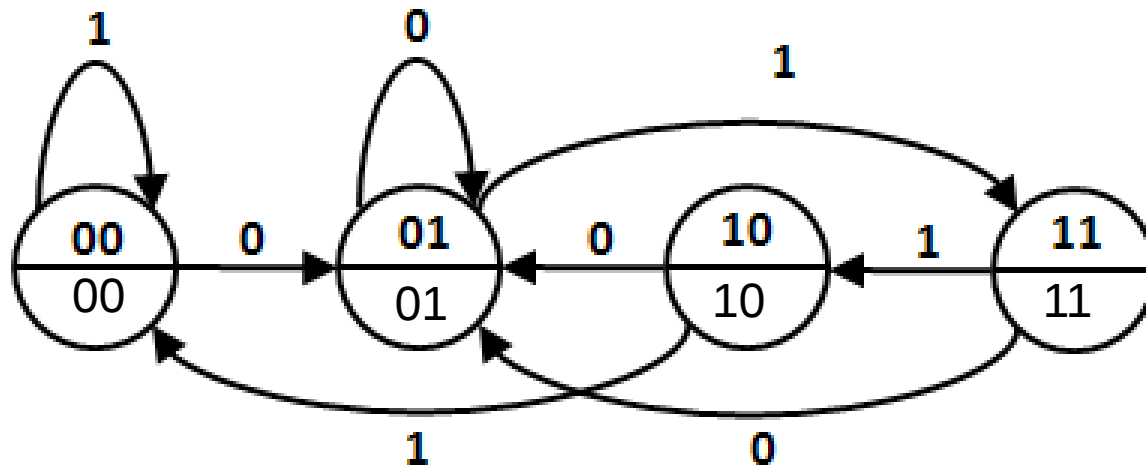
| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| 00                     | 01 | 00 |
| 01                     | 01 | 11 |
| 11                     | 01 | 10 |
| 10                     | 01 | 00 |



# 10.1

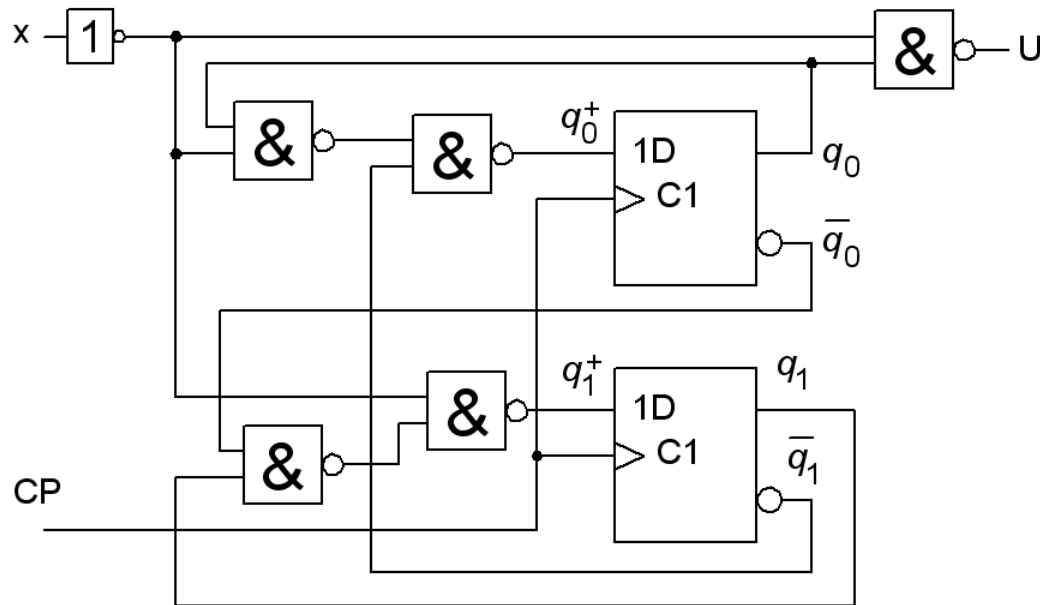


Output is the same as flip-flop state.

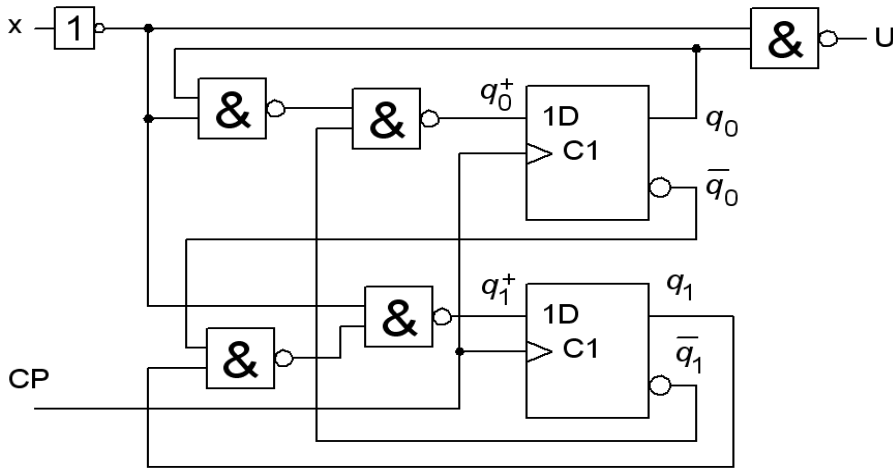


# Ex 10.2

Determine the state diagram and state table for the sequence circuit.  
Which of the models Mealy or Moore fits on the circuit?



# 10.2



Because  $U$  is directly depended of  $x$  so must the Mealy model be used.

NAND-gates:

$$U = \overline{\overline{x} \cdot q_0} = \{dM\} = x + \overline{q_0}$$

$$q_0^+ = \overline{\overline{q_1} \cdot (\overline{q_0} \cdot \overline{x})} = \{dM\} = \\ = q_1 + q_0 \overline{x}$$

$$q_1^+ = \overline{\overline{(q_1 \cdot q_0)} \cdot \overline{x}} = \{dM\} = \\ = x + \overline{q_1 q_0}$$

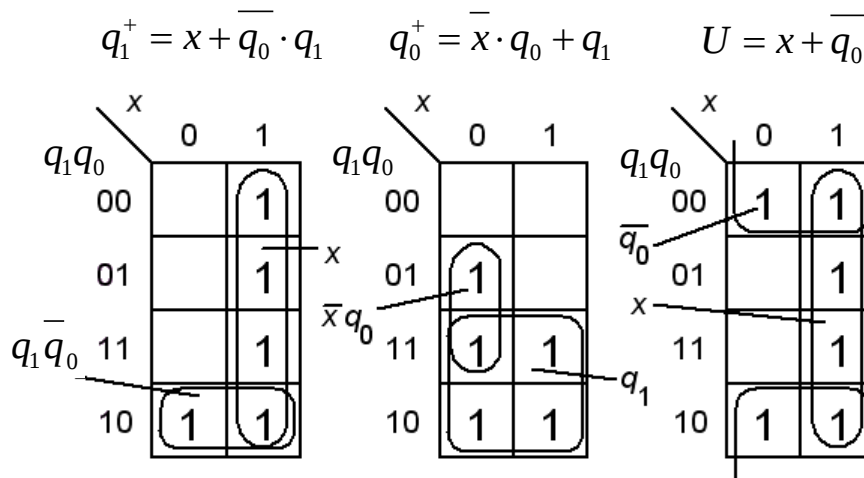
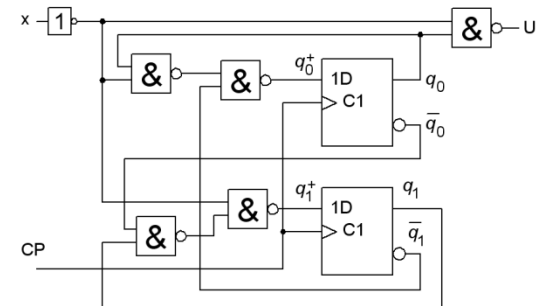
De Morgans law gives us the SP form.

# 10.2

$$U = x + \overline{q_0}$$

$$q_1^+ = x + \overline{q_0} \cdot q_1$$

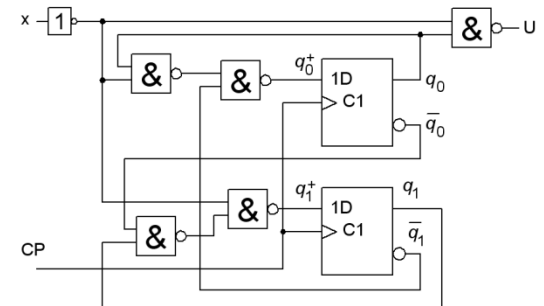
$$q_0^+ = \overline{x} \cdot q_0 + q_1$$



$$q_0^+ q_1^+ / U = f(q_0, q_1, x)$$

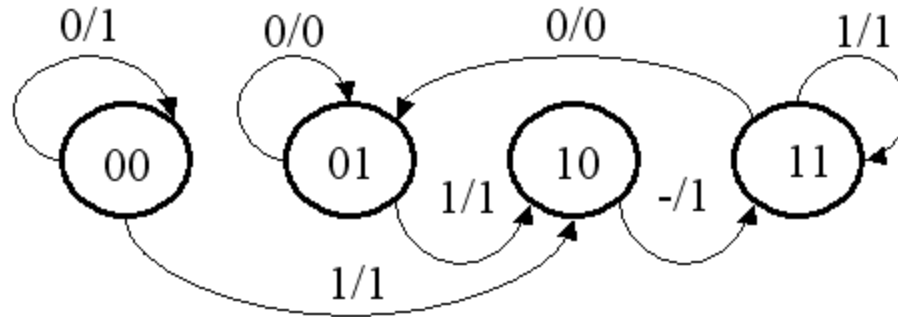
|           | x  |           |
|-----------|----|-----------|
|           | 0  | 1         |
| $q_1 q_0$ | 00 | 00/1 10/1 |
|           | 01 | 01/0 10/1 |
|           | 11 | 01/0 11/1 |
|           | 10 | 11/1 11/1 |

# 10.2



$$q_0^+ q_1^+ / U = f(q_0, q_1, x)$$

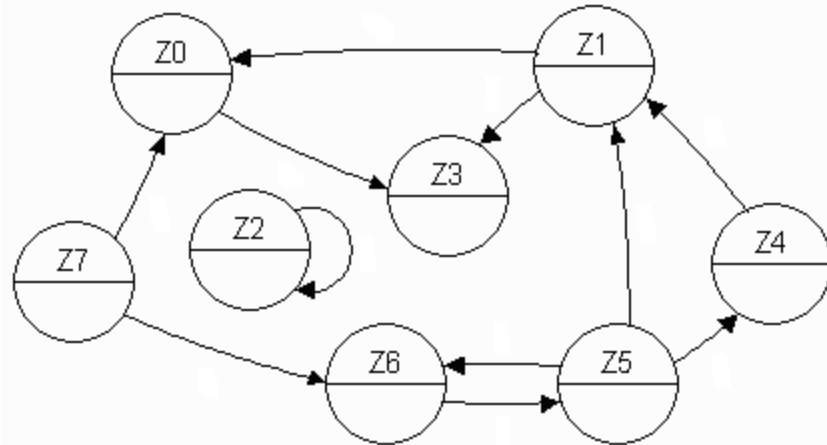
|           |    | x    |      |
|-----------|----|------|------|
|           |    | 0    | 1    |
| $q_0 q_1$ | 00 | 00/1 | 10/1 |
|           | 01 | 01/0 | 10/1 |
|           | 11 | 01/0 | 11/1 |
|           | 10 | 11/1 | 11/1 |



# ( Ex 10.4 )

Is there any stopping condition, loss condition or isolated states in the state diagram?

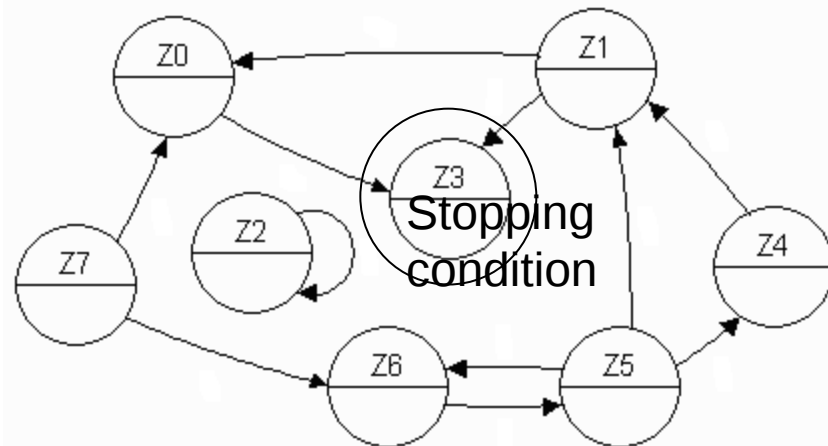
- Stopping condition:
- Loss condition:
- Isolated states:



# ( Ex 10.4 )

Is there any stopping condition, loss condition or isolated states in the state diagram?

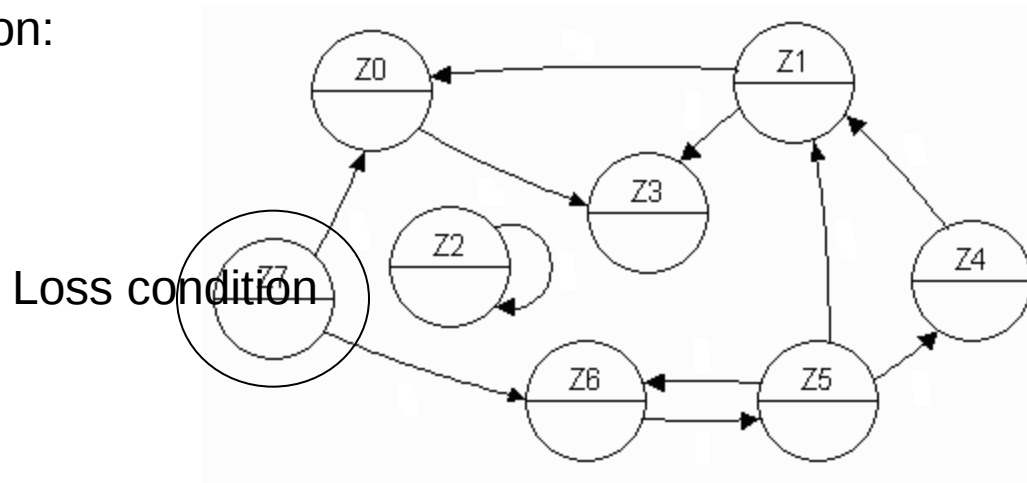
- Stopping condition:
- Loss condition:
- Isolated states:



# ( Ex 10.4 )

Is there any stopping condition, loss condition or isolated states in the state diagram?

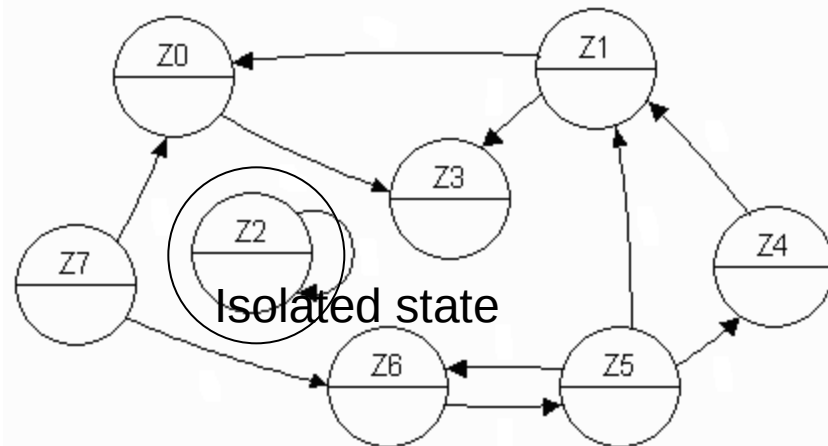
- Stopping condition:
- Loss condition:
- Isolated states:



# ( Ex 10.4 )

Is there any stopping condition, loss condition or isolated states in the state diagram?

- Stopping condition:
- Loss condition:
- Isolated states:

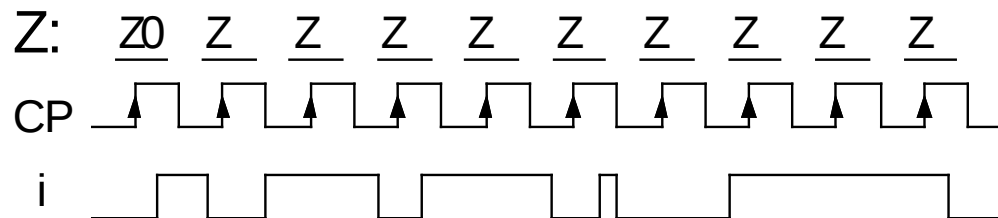
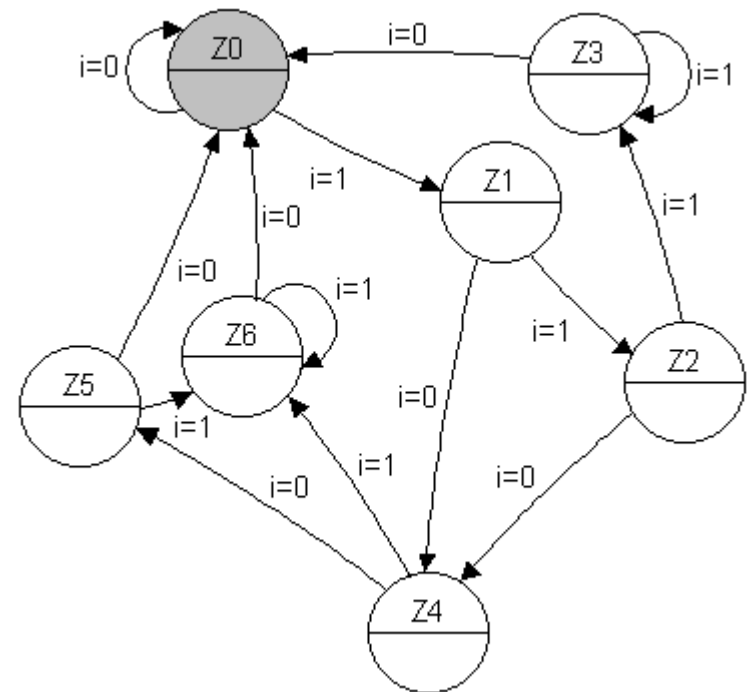


# Ex 10.5

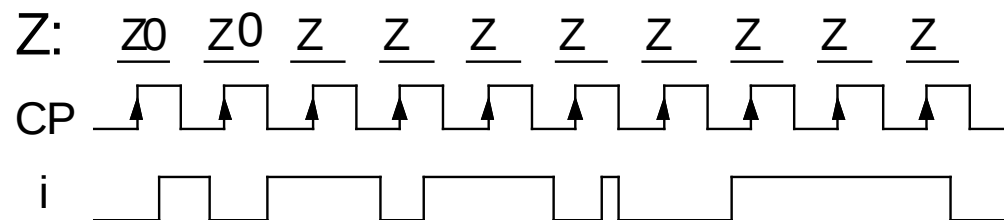
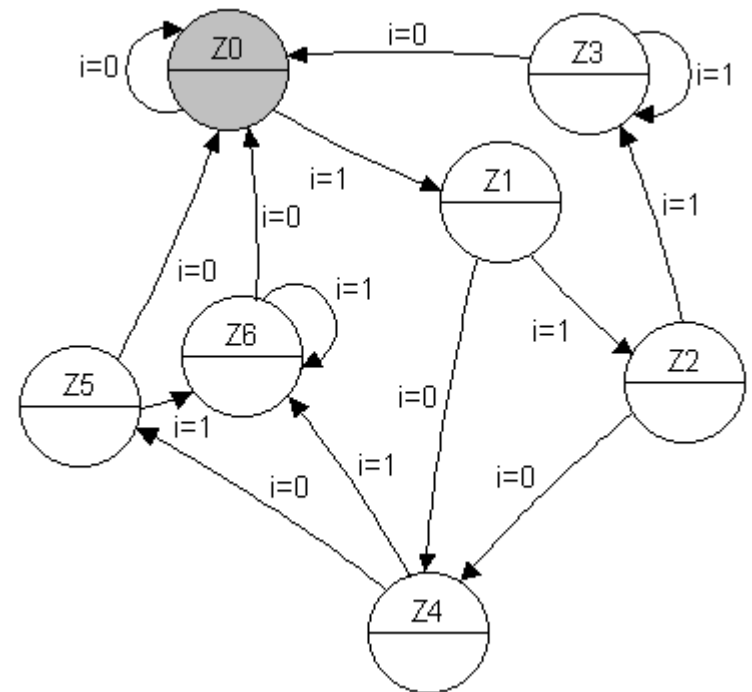
To the right is a state diagram for a Moore machine.  
(it will detect a double tap).

A monkey accidentally get hold of the push-button input signal, and then presses according to the timing diagram below.

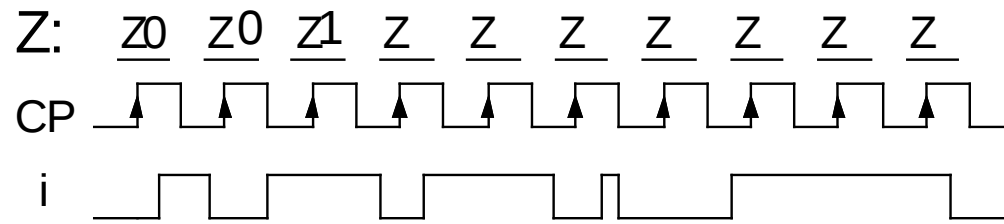
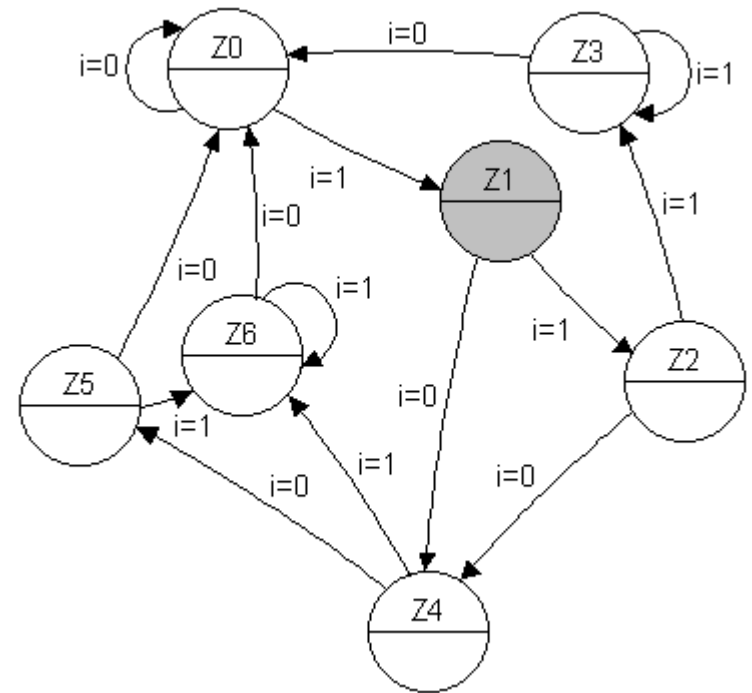
The Moore-machine has flip-flops that are triggered by the positive edge of the clock. Suppose that the initial state is Z0.



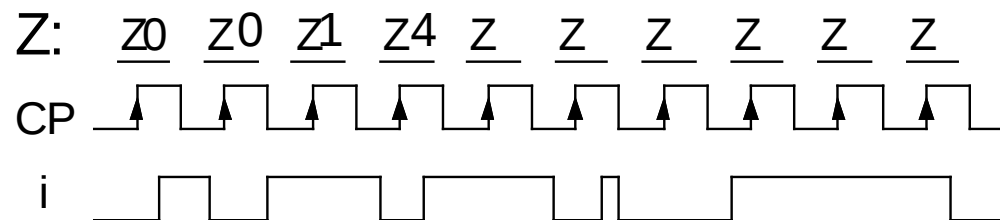
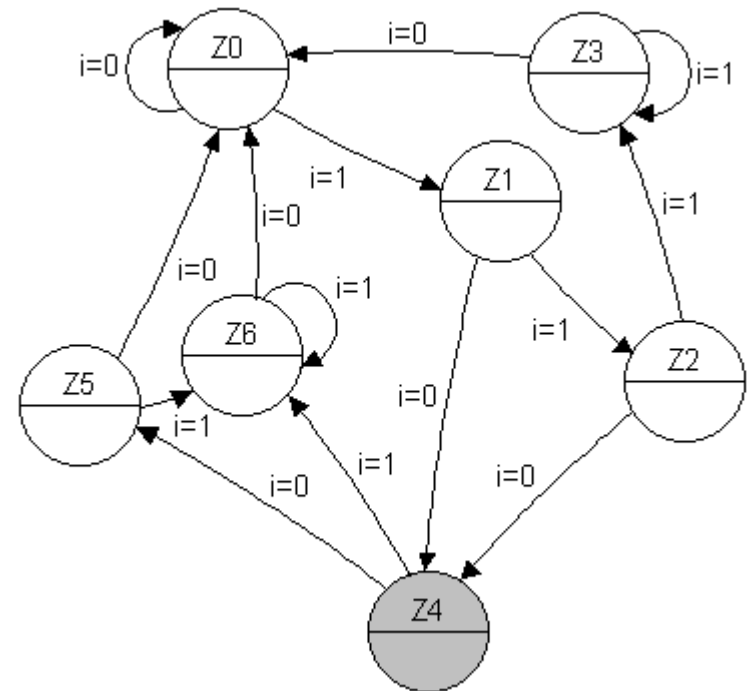
# Ex 10.5



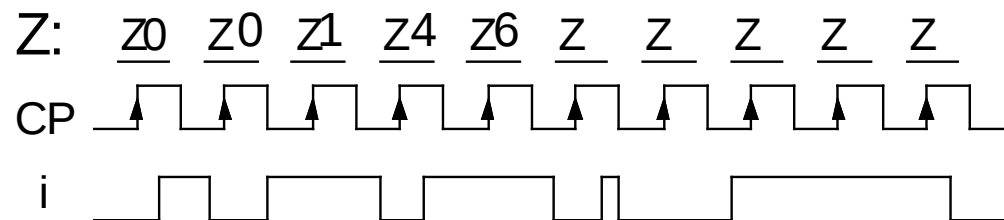
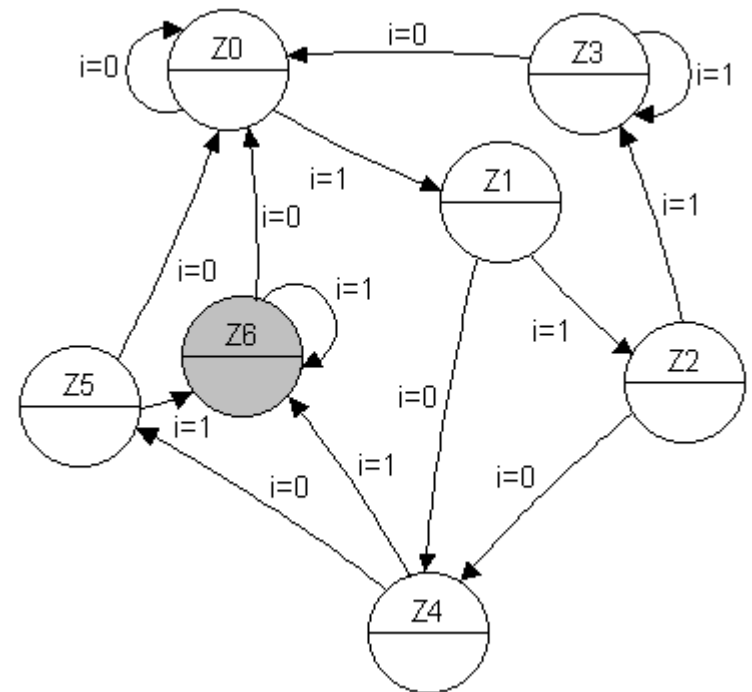
# Ex 10.5



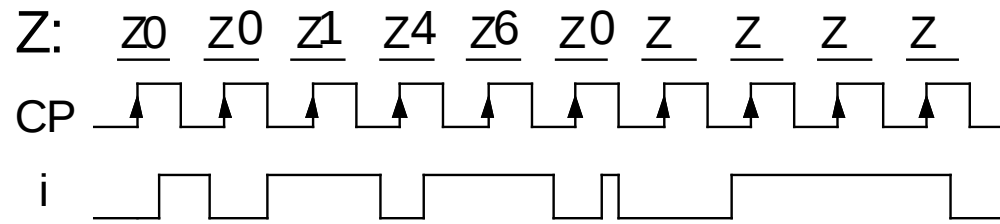
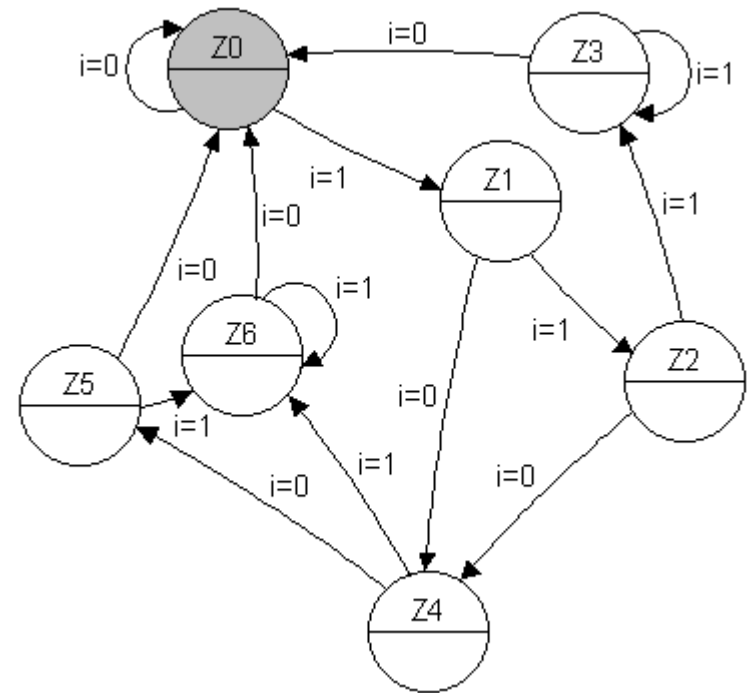
# Ex 10.5



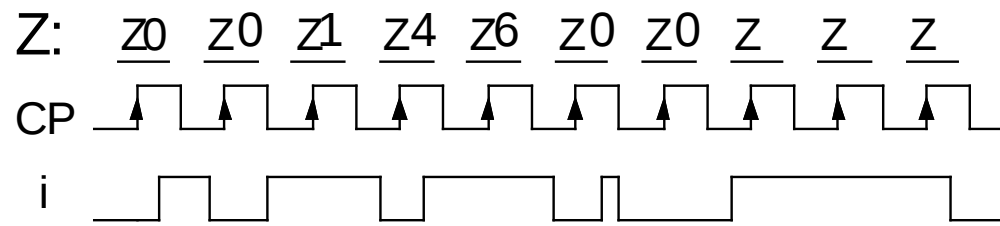
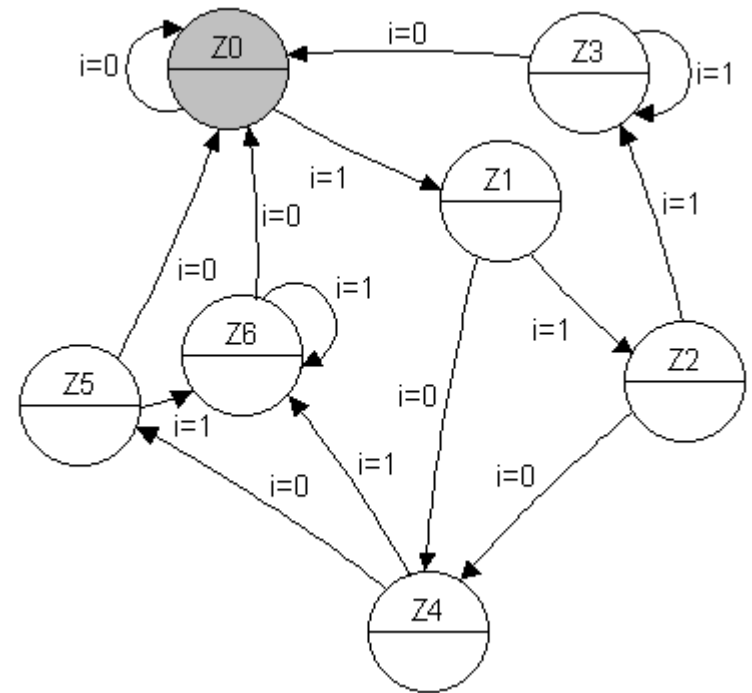
# Ex 10.5



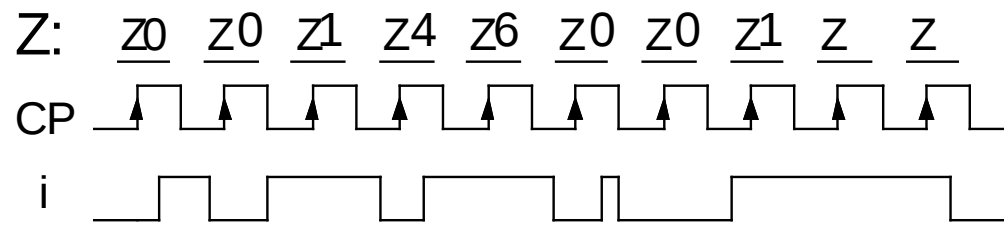
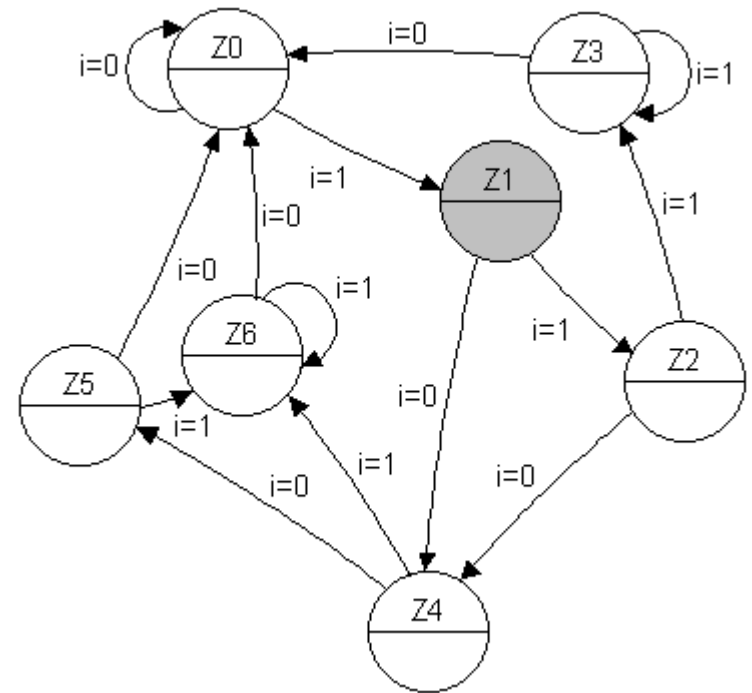
# Ex 10.5



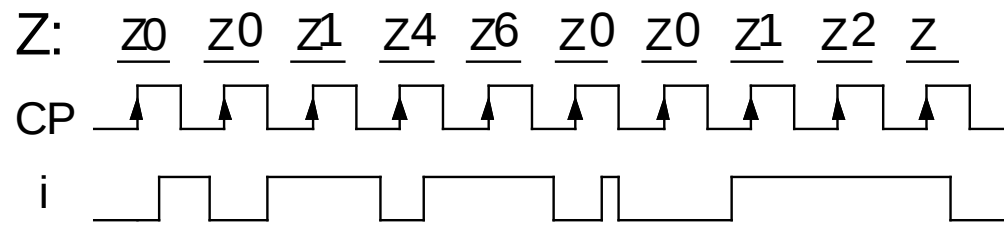
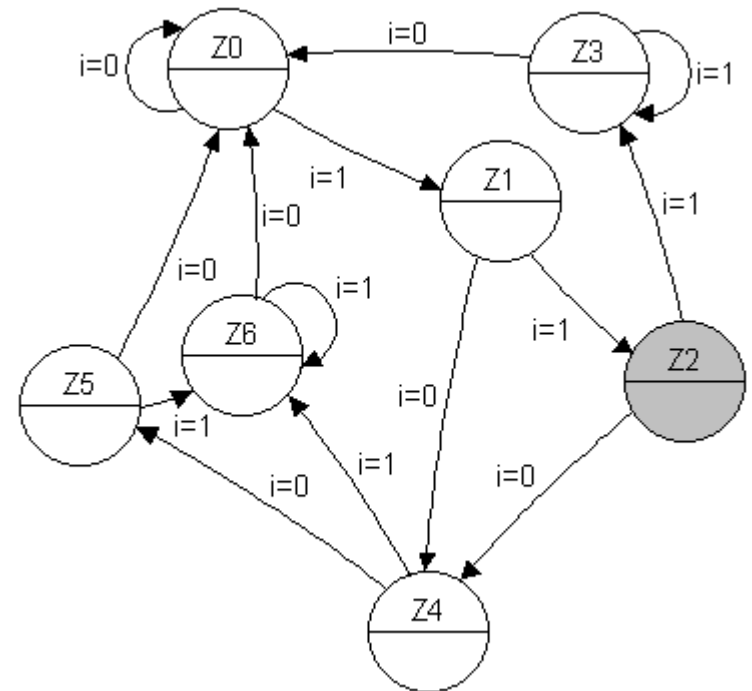
# Ex 10.5



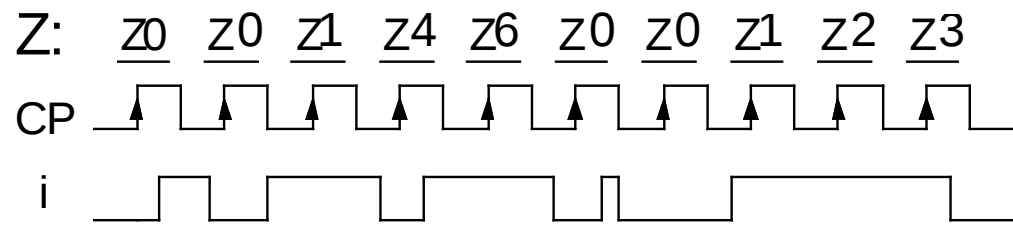
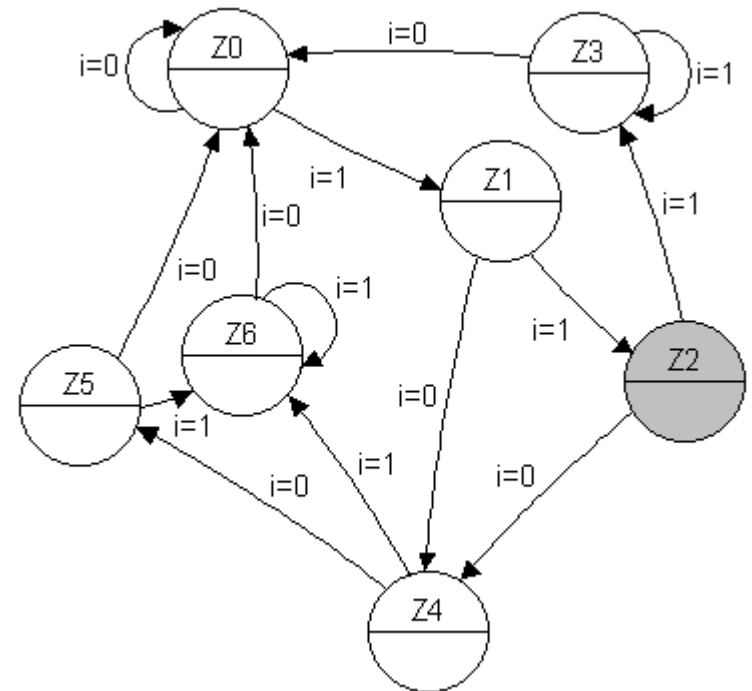
# Ex 10.5



# Ex 10.5



# Ex 10.5

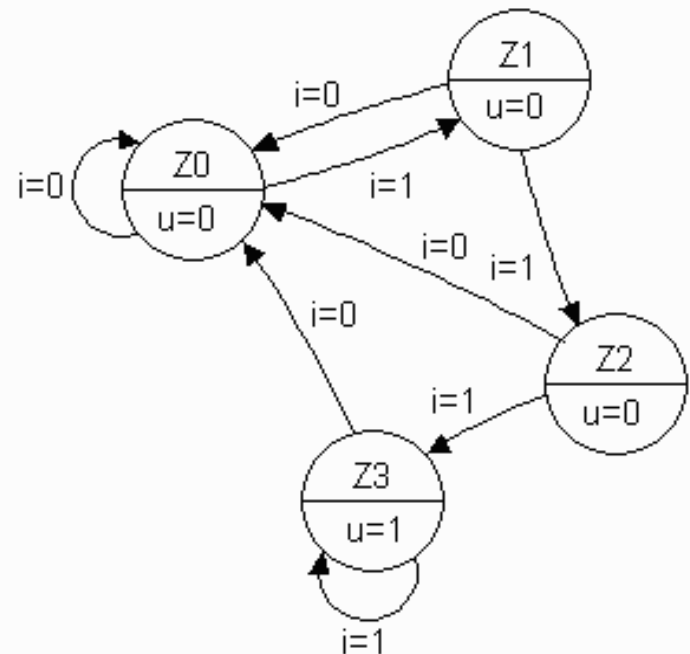
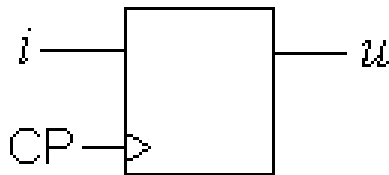


William Sandqvist [william@kth.se](mailto:william@kth.se)

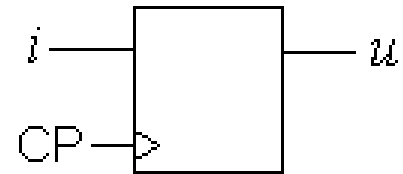
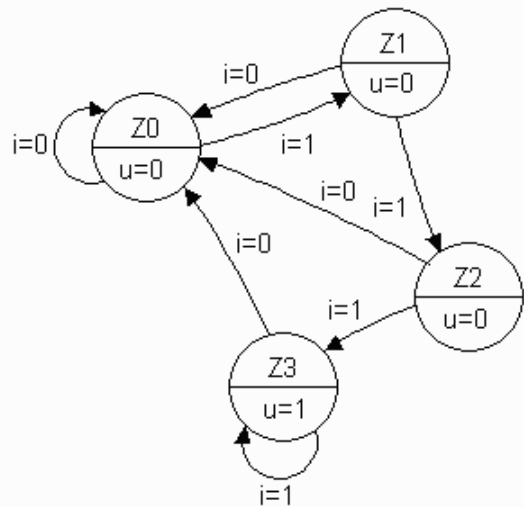
# Ex 10.6

Construct a Moore machine which requires that the input signal is equal to one ( $i = 1$ ) during three successive clock pulse interval, for the output to be one ( $u = 1$ ). As soon as the input signal becomes zero ( $i = 0$ ) during a clock pulse interval, the circuit output should return to zero ( $u = 0$ ). See the state diagram. Choose Gray code for state encoding. ( $Z0=00$ ,  $Z1=01$ ,  $Z2=11$ ,  $Z3=10$ ). Use D-flip-flops and AND-OR gates.

(This is a safety circuit to prevent "false alarms")



# Ex 10.6



From statediagram to  
coded state table:

$$q_1^+ q_0^+ (q_1 q_0 i)$$

| $q_1 q_0$ |    | $i$ |    |
|-----------|----|-----|----|
|           |    | 0   | 1  |
| Z0:       | 00 | 00  | 01 |
| Z1:       | 01 | 00  | 11 |
| Z2:       | 11 | 00  | 10 |
| Z3:       | 10 | 00  | 10 |

$$q_1^+ = i q_0 + i q_1$$

| $q_1 q_0$ |  | $i$ |   |
|-----------|--|-----|---|
|           |  | 0   | 1 |
| 00        |  | 0   | 0 |
| 01        |  | 0   | 1 |
| 11        |  | 0   | 1 |
| 10        |  | 0   | 1 |

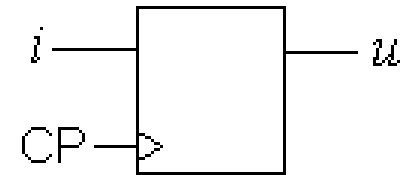
$$q_0^+ = i \bar{q}_1$$

| $q_1 q_0$ |  | $i$ |   |
|-----------|--|-----|---|
|           |  | 0   | 1 |
| 00        |  | 0   | 1 |
| 01        |  | 0   | 1 |
| 11        |  | 0   | 0 |
| 10        |  | 0   | 0 |

$$u = q_1 \bar{q}_0$$

| $q_1 q_0$ |  | $i$ |   |
|-----------|--|-----|---|
|           |  | 0   | 1 |
| 00        |  | 0   | 1 |
| 01        |  | 0   | 1 |
| 11        |  | 0   | 0 |
| 10        |  | 0   | 0 |

# 10.6



$$q_1^+ = i q_0 + i q_1$$

|                        |   |   |
|------------------------|---|---|
| $i \backslash q_1 q_0$ | 0 | 1 |
| 00                     | 0 | 0 |
| 01                     | 0 | 1 |
| 11                     | 0 | 1 |
| 10                     | 0 | 1 |

Labels in the table:  $i q_0$  points to the 01 row, 1 column cell.  $i q_1$  points to the 11 and 10 rows, 1 column cells.

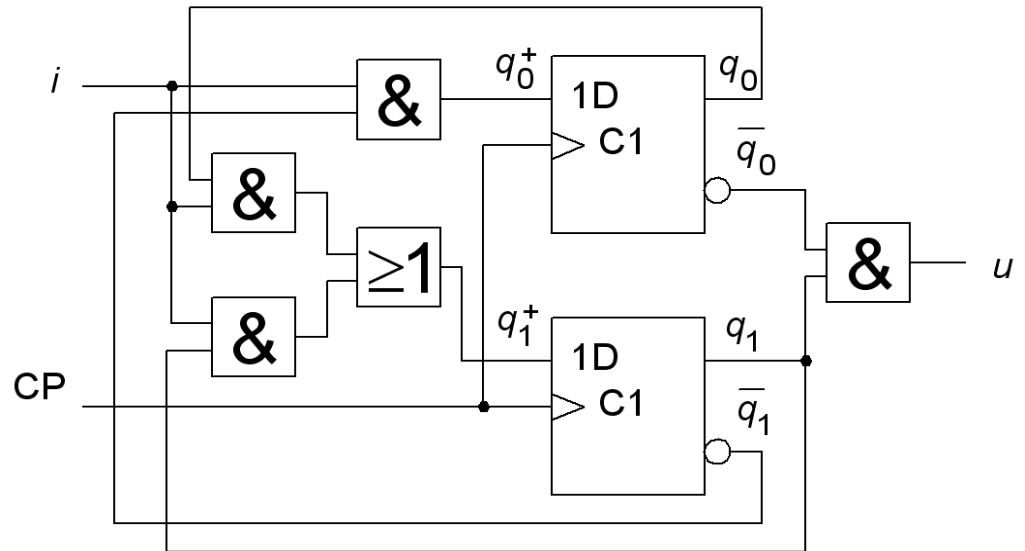
$$u = q_1 \bar{q}_0$$

|           |   |
|-----------|---|
| $q_1 q_0$ |   |
| 00        | 0 |
| 01        | 0 |
| 11        | 0 |
| 10        | 1 |

$$q_0^+ = i \bar{q}_1$$

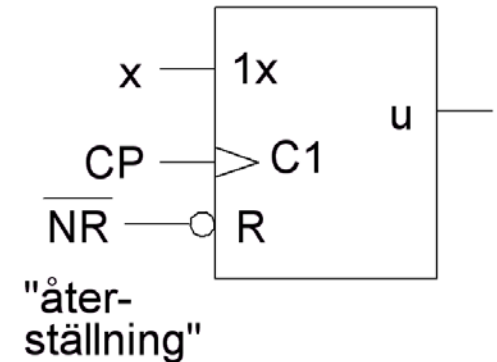
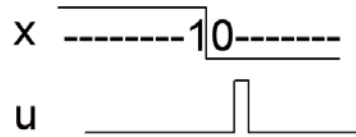
|                        |   |   |
|------------------------|---|---|
| $i \backslash q_1 q_0$ | 0 | 1 |
| 00                     | 0 | 1 |
| 01                     | 0 | 1 |
| 11                     | 0 | 0 |
| 10                     | 0 | 0 |

Label in the table:  $i \bar{q}_1$  points to the 00 and 01 rows, 1 column cells.



# Ex 10.7

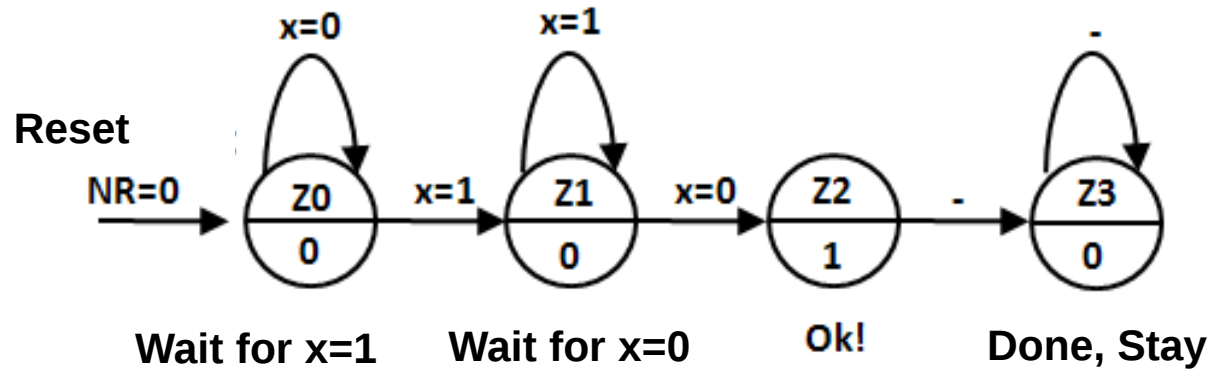
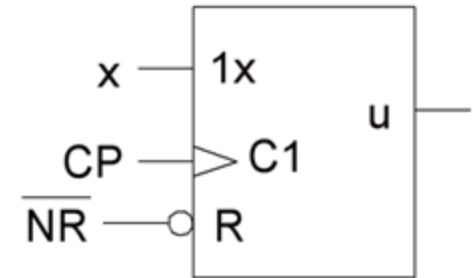
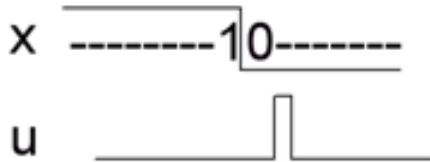
Construct a sequential circuits that detects when the input signal  $x$  has a transition  $1 \rightarrow 0$  and then has the output  $u = 1$  in the following clock-pulse interval, det nästföljande klockpulsintervallet and then being 0 for the rest of the sequence.

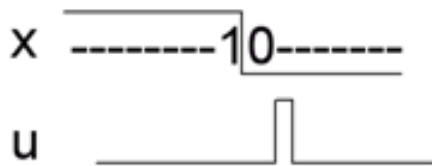


The circuit should be able to "reset" with an asynchronous reset pulse (NR active low), so that it monitors the input signal again.

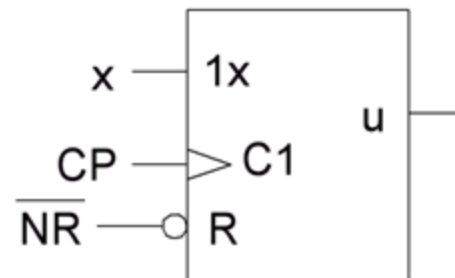
- Draw state a diagram of a Moore machine type for the sequence network.
- Derive the Boolean expressions for the next state and the output for three different state encoding:
  - "Binarycode"
  - "Graycode"
  - "One hot" code
- Show how the reset signal is connected to NR D-flip-flops PRE and CLR inputs.

# 10.7

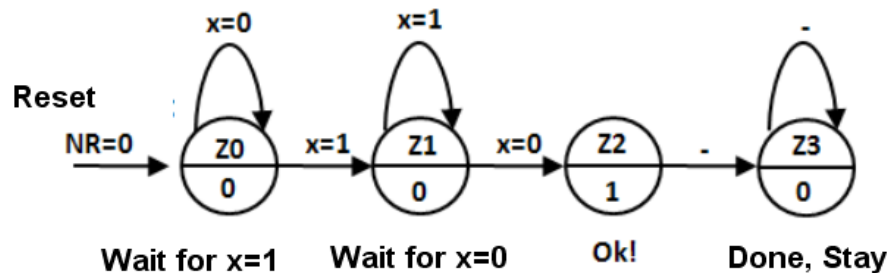




# 10.7



State code: Binary:



Bin  $q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0$ \ $x$ | 0  | 1  |
|-----------------|----|----|
| Z0: 00          | 00 | 01 |
| Z1: 01          | 10 | 01 |
| Z3: 11          | 11 | 11 |
| Z2: 10          | 11 | 11 |

$q_1^+ = q_0 \bar{x} + q_1$

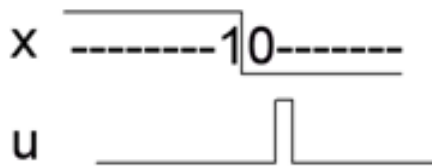
| $q_1 q_0$ \ $x$ | 0 | 1 |
|-----------------|---|---|
| 00              | 0 | 0 |
| 01              | 1 | 0 |
| 11              | 1 | 1 |
| 10              | 1 | 1 |

$q_0^+ = q_1 + x$

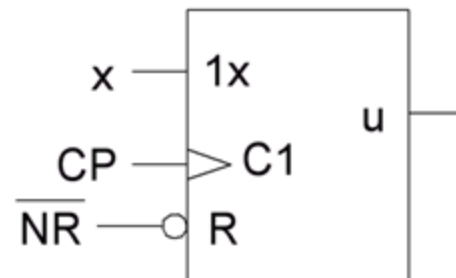
| $q_1 q_0$ \ $x$ | 0 | 1 |
|-----------------|---|---|
| 00              | 0 | 1 |
| 01              | 0 | 1 |
| 11              | 1 | 1 |
| 10              | 1 | 1 |

$U = q_1 \bar{q}_0$

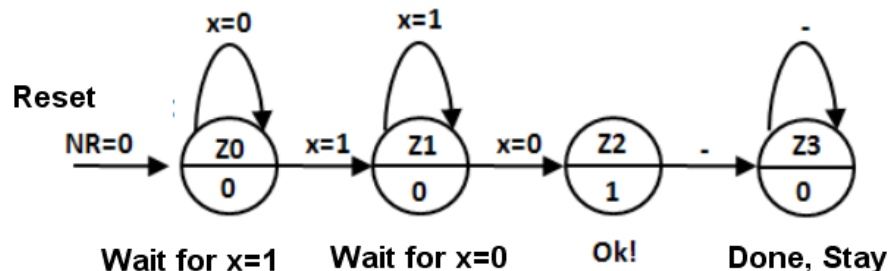
| $q_1 q_0$ |   |
|-----------|---|
| 00        | 0 |
| 01        | 0 |
| 11        | 0 |
| 10        | 1 |



# 10.7



Statecode Gray:



Gray  $q_1^+ q_0^+ (q_1 q_0 x)$

| $q_1 q_0 \backslash x$ | 0  | 1  |
|------------------------|----|----|
| Z0: 00                 | 00 | 01 |
| Z1: 01                 | 11 | 01 |
| Z2: 11                 | 10 | 10 |
| Z3: 10                 | 10 | 10 |

$q_1^+ = q_0 \bar{x} + q_1$

| $q_1 q_0 \backslash x$ | 0 | 1 |
|------------------------|---|---|
| 00                     | 0 | 0 |
| 01                     | 1 | 0 |
| 11                     | 1 | 1 |
| 10                     | 1 | 1 |

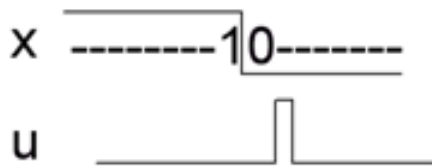
$q_0^+ = \bar{q}_1 q_0 + \bar{q}_1 x$

| $q_1 q_0 \backslash x$ | 0 | 1 |
|------------------------|---|---|
| 00                     | 0 | 1 |
| 01                     | 1 | 1 |
| 11                     | 0 | 0 |
| 10                     | 0 | 0 |

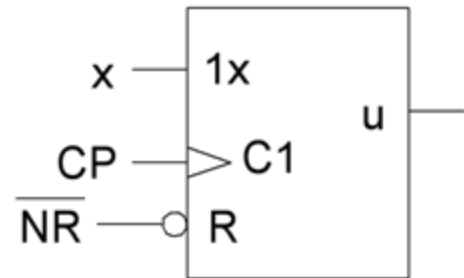
$U = q_1 q_0$

| $q_1 q_0 \backslash x$ | 0 | 1 |
|------------------------|---|---|
| 00                     | 0 | 0 |
| 01                     | 0 | 0 |
| 11                     | 1 | 1 |
| 10                     | 0 | 0 |

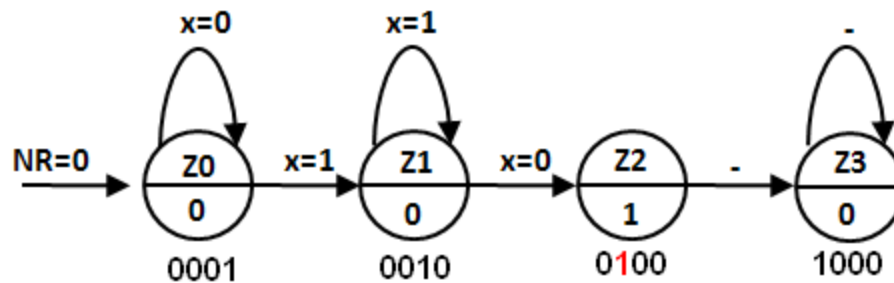
*This time the binary state code seems to be the better one.*



# 10.7



State code: One Hot:



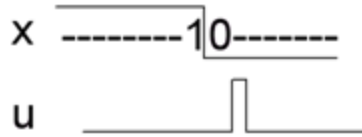
$$q_3^+ q_2^+ q_1^+ q_0^+ (q_3 q_2 q_1 q_0 x)$$

$$\overline{x}$$

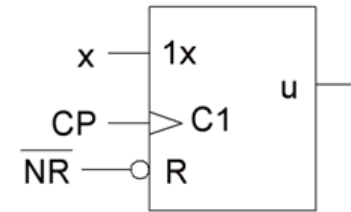
| $q_3 q_2$ | $q_1 q_0$ | 00   | 01   | 11 | 10   |
|-----------|-----------|------|------|----|------|
| 0         | 0         | 0    | 1    | 3  | 2    |
| 0         | 0         | -    | 0001 | -  | 0100 |
| 0         | 1         | 4    | 5    | 7  | 6    |
| 0         | 1         | 1000 | -    | -  | -    |
| 1         | 0         | 12   | 13   | 15 | 14   |
| 1         | 0         | -    | -    | -  | -    |
| 1         | 1         | 8    | 9    | 11 | 10   |
| 1         | 1         | 1000 | -    | -  | -    |

$$x$$

| $x_3 x_2$ | $x_1 x_0$ | 00   | 01   | 11 | 10   |
|-----------|-----------|------|------|----|------|
| 0         | 0         | 16   | 17   | 19 | 18   |
| 0         | 0         | -    | 0010 | -  | 0010 |
| 0         | 1         | 20   | 21   | 23 | 22   |
| 0         | 1         | 1000 | -    | -  | -    |
| 1         | 0         | 28   | 29   | 31 | 30   |
| 1         | 0         | -    | -    | -  | -    |
| 1         | 1         | 24   | 25   | 27 | 26   |
| 1         | 1         | 1000 | -    | -  | -    |



# 10.7



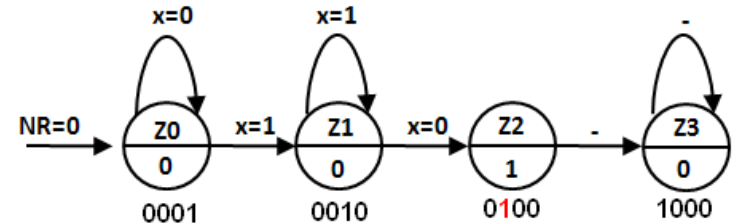
State code: One Hot:

$q_3^+ q_2^+ q_1^+ q_0^+ (q_3 q_2 q_1 q_0 x)$

| $q_1 q_0$ |   | $\bar{x}$ |      |    |      |
|-----------|---|-----------|------|----|------|
|           |   | 00        | 01   | 11 | 10   |
| 0         | 0 | -         | 0001 | -  | 0100 |
| 0         | 1 | 1000      | -    | -  | -    |
| 1         | 0 | -         | -    | -  | -    |
| 1         | 1 | -         | -    | -  | -    |

| $x_1 x_0$ |   | $x$ |      |    |      |
|-----------|---|-----|------|----|------|
|           |   | 00  | 01   | 11 | 10   |
| 0         | 0 | 16  | 0010 | -  | 0010 |
| 0         | 1 | 20  | 1000 | -  | -    |
| 1         | 0 | 28  | -    | 31 | 30   |
| 1         | 1 | 24  | 1000 | 25 | 27   |



$q_3^+ \quad \bar{x}$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 0 |
| 1 | - | - | - |
| - | - | - | - |
| 1 | - | - | - |

$x$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 0 |
| 1 | - | - | - |
| - | - | - | - |
| 1 | - | - | - |

$q_2^+ \quad \bar{x}$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 1 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$x$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 0 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$q_1^+ \quad \bar{x}$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 0 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$x$

|   |   |   |   |
|---|---|---|---|
| - | 1 | - | 1 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$q_0^+ \quad \bar{x}$

|   |   |   |   |
|---|---|---|---|
| - | 1 | - | 0 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$x$

|   |   |   |   |
|---|---|---|---|
| - | 0 | - | 0 |
| 0 | - | - | - |
| - | - | - | - |
| 0 | - | - | - |

$q_3^+ = \bar{q}_1 \bar{q}_0$

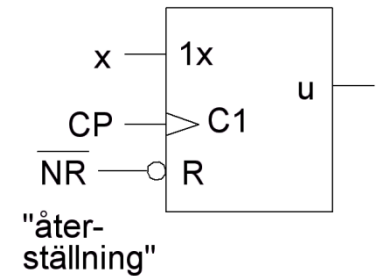
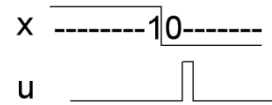
$q_2^+ = q_1 \bar{x}$

$q_1^+ = \bar{q}_3 \bar{q}_2 x$

$q_0^+ = q_0 \bar{x}$

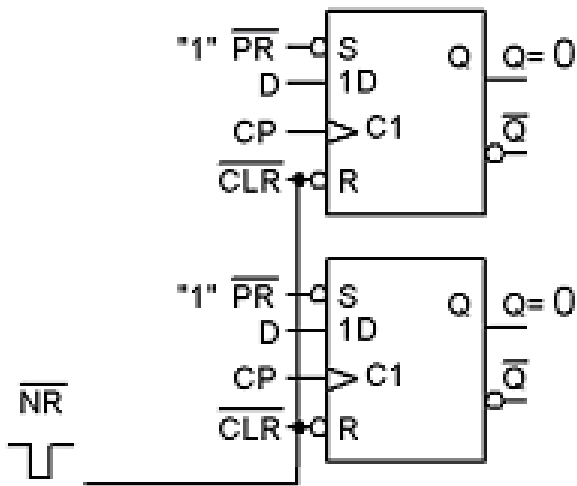
$u = q_2$

# 10.7



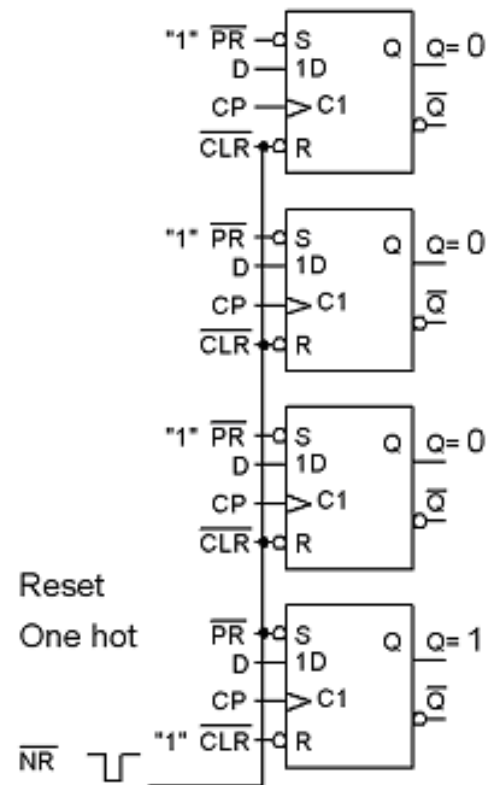
## Reset signals.

Reset Bin/Gray

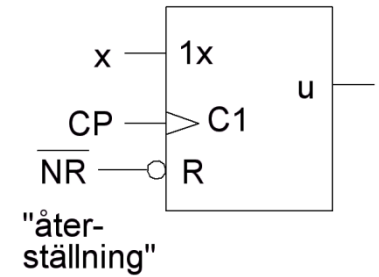
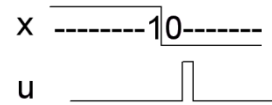


Bin / Gray networks is reseted by the flip-flop's CLR inputs.

One Hot network is restored by setting the flip-flops to "0001" with the CLR and PR inputs.

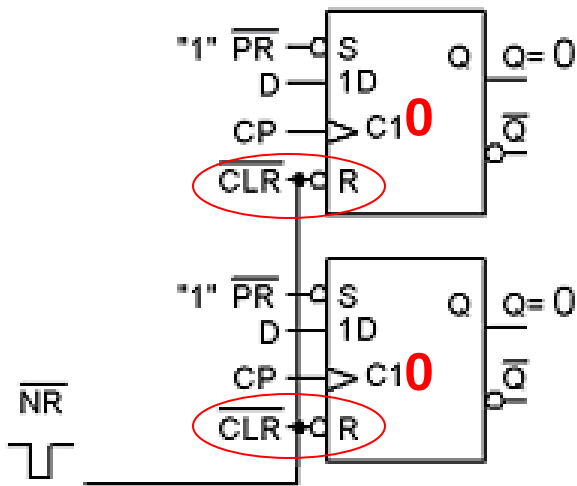


# 10.7

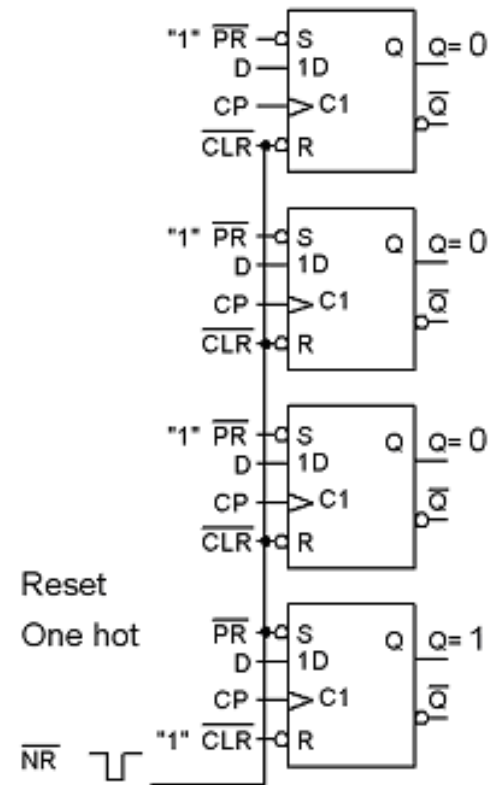


## Reset signals.

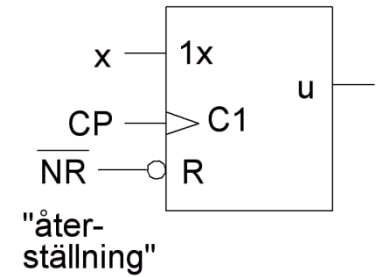
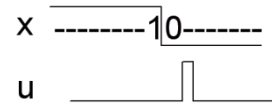
Reset Bin/Gray



Bin / Gray networks is reseted by the flip-flop's CLR inputs.

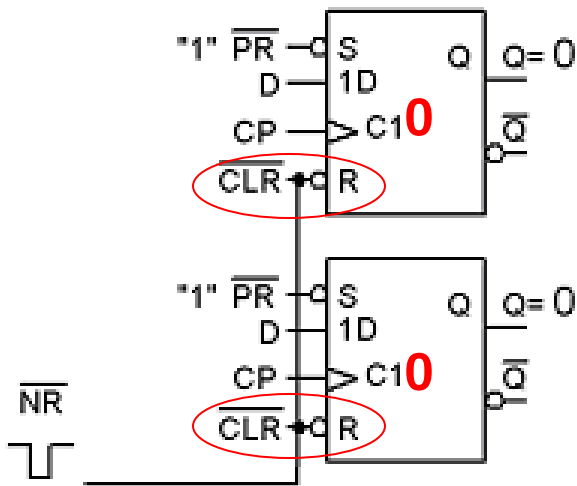


# 10.7



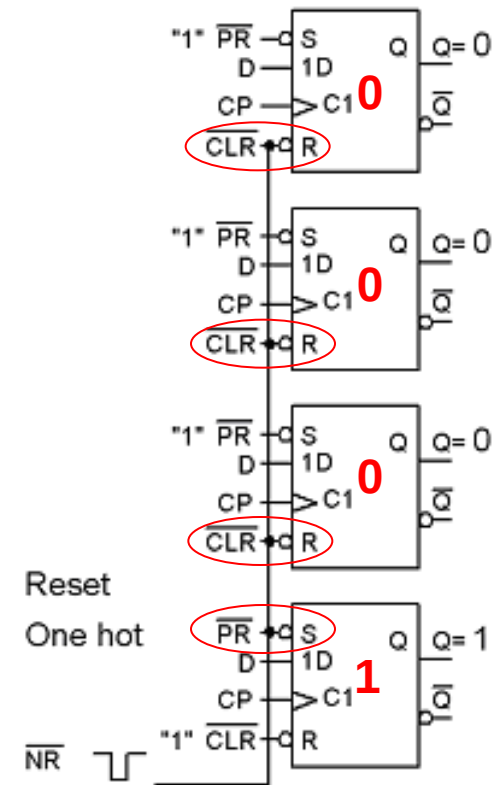
## Reset signals.

Reset Bin/Gray

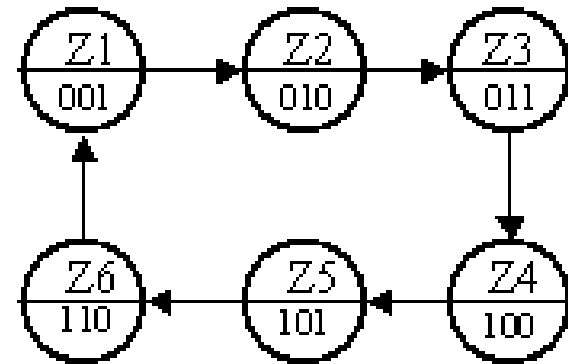
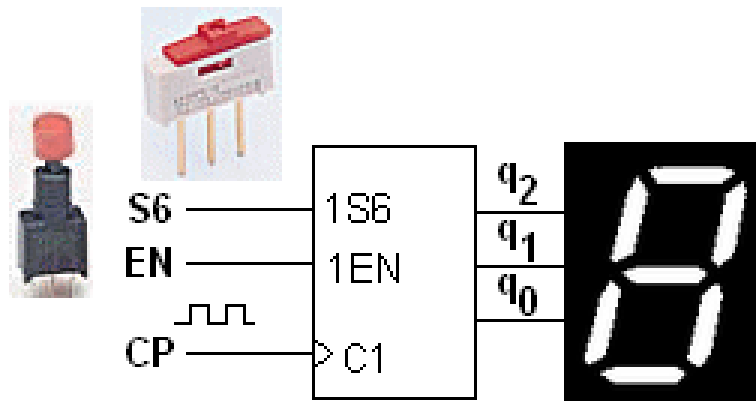


Bin / Gray networks is reseted by the flip-flop's CLR inputs.

One Hot network is restored by setting the flip-flops to "0001" with the CLR and PR inputs.



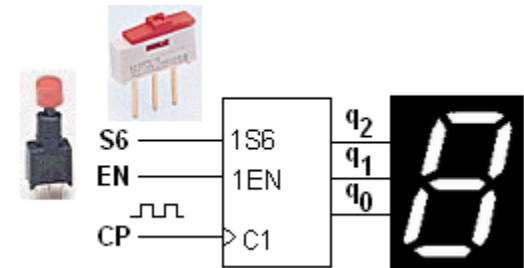
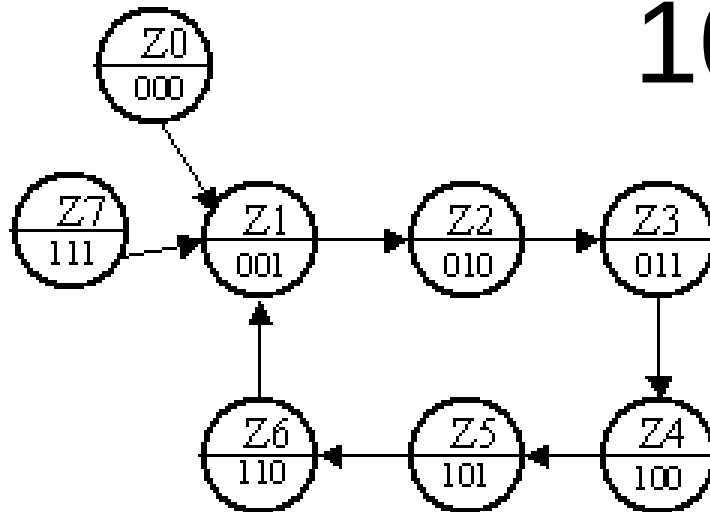
# Ex 10.8



Design a counter that counts  $\{... 1, 2, 3, 4, 5, 6, 1 ... \}$ . The counting sequence,  $q_2q_1q_0$ , is to be shown with a 7-segment display, as a roll of the dice.

- State the expressions for the next state..
- Complete the expressions with a variable EN which will "freeze" the state when  $EN = 0$  (unpressed button). The counter should count for  $EN = 1$  (pressed button).
- Complete the expressions with a variable S6 which forces the counter to state "6" when  $S6 = 1$  (hidden button pressed). This is the "cheat-button". S6 takes precedence over one.

# 10.8



We let the two unused states Z0 and Z7 as a precaution go to Z1.

$q_2^+ q_1^+ q_0^+ (q_2 q_1 q_0)$

|       |   | $q_0$ |     |
|-------|---|-------|-----|
|       |   | 0     | 1   |
| $q_2$ | 0 | 001   | 010 |
|       | 1 | 011   | 100 |
| $q_1$ | 0 | 001   | 001 |
|       | 1 | 101   | 110 |

$q_2^+$ 

|   |   |
|---|---|
| 0 | 0 |
| 0 | 1 |
| 0 | 0 |
| 1 | 1 |

$q_1^+$ 

|   |   |
|---|---|
| 0 | 1 |
| 1 | 0 |
| 0 | 0 |
| 0 | 1 |

$q_0^+$ 

|   |   |
|---|---|
| 1 | 0 |
| 1 | 0 |
| 1 | 1 |
| 1 | 0 |

$$q_2^+ = q_2 \bar{q}_1 + \bar{q}_2 q_1 q_0$$

$$q_1^+ = \bar{q}_1 q_0 + \bar{q}_2 q_1 \bar{q}_0$$

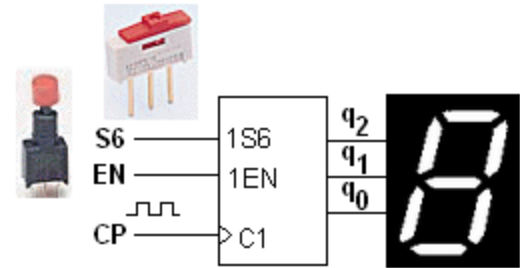
$$q_0^+ = \bar{q}_0 + q_2 q_1$$

# 10.8

$$q_2^+ = q_2 \bar{q}_1 + \bar{q}_2 q_1 q_0$$

$$q_1^+ = \bar{q}_1 q_0 + \bar{q}_2 q_1 \bar{q}_0$$

$$q_0^+ = \bar{q}_0 + q_2 q_1$$



Equations with EN

(EN=0 → next state same)

Equations with S6

(S6 = 1 → next state is 110) :

$$(q_2^+)' = EN \cdot (q_2^+) + \overline{EN} \cdot (q_2)$$

$$(q_1^+)' = EN \cdot (q_1^+) + \overline{EN} \cdot (q_1)$$

$$(q_0^+)' = EN \cdot (q_0^+) + \overline{EN} \cdot (q_0)$$

$$(q_2^+)'' = (q_2^+)' + S6$$

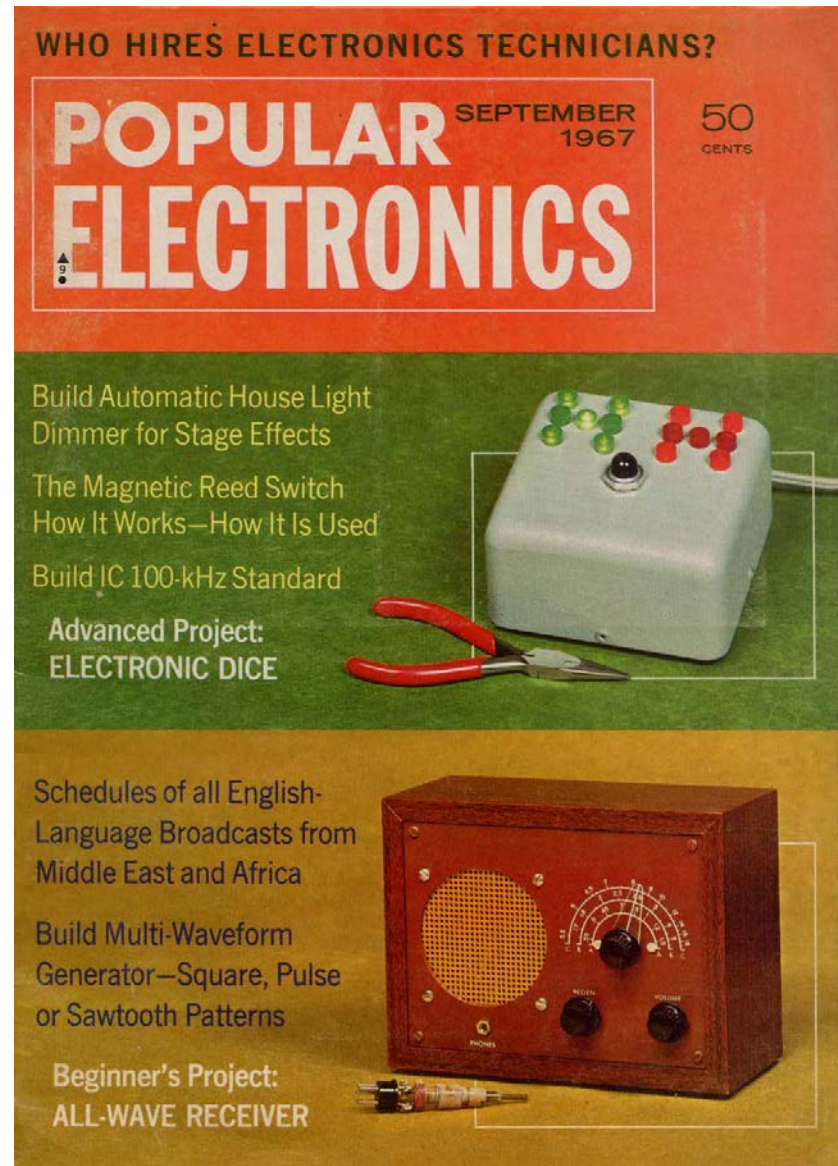
$$(q_1^+)'' = (q_1^+)' + S6$$

$$(q_0^+)'' = (q_0^+)' \cdot \overline{S6}$$

1967 was the construction of an electronic dice an "advanced project".

Today it is the analog technology that is advanced!

The construction of an all-band receiver was an entry-level project!



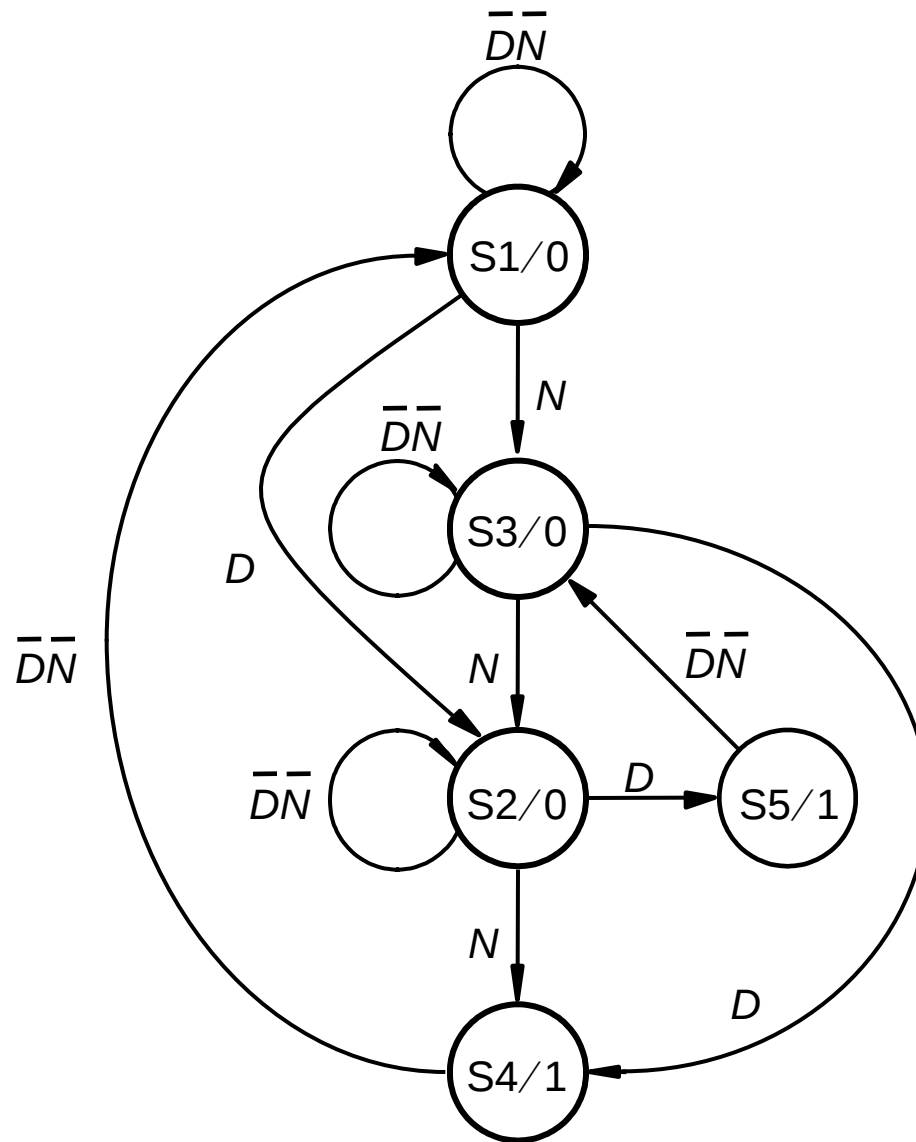
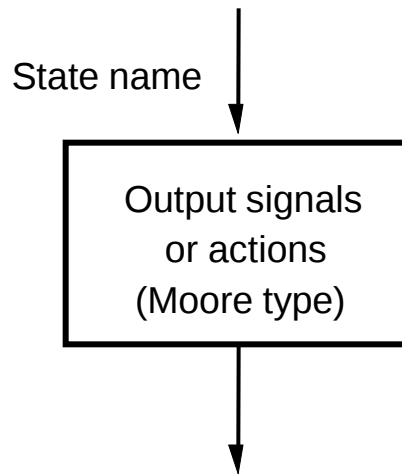
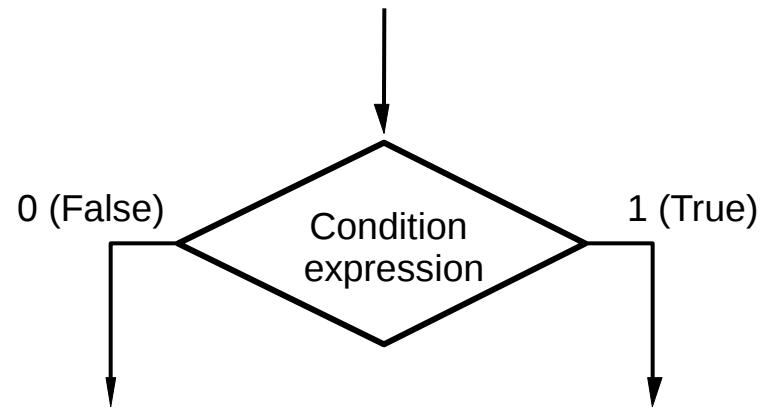


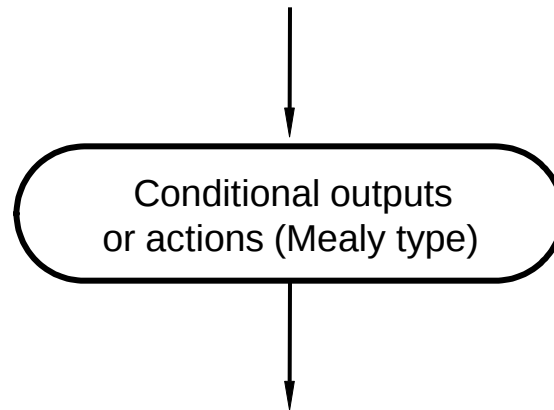
Figure 8.57. Minimized state diagram for Example 8.6.



(a) State box



(b) Decision box

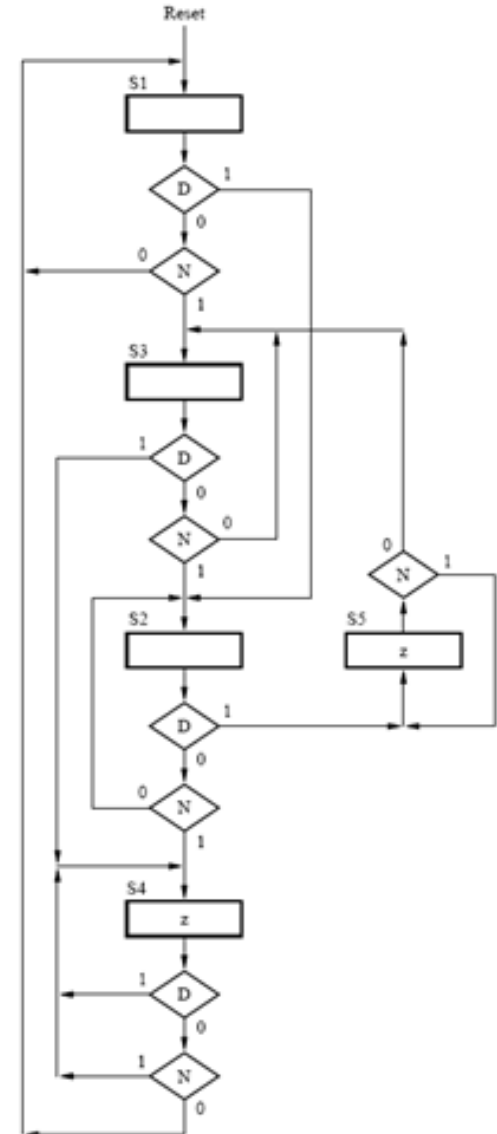
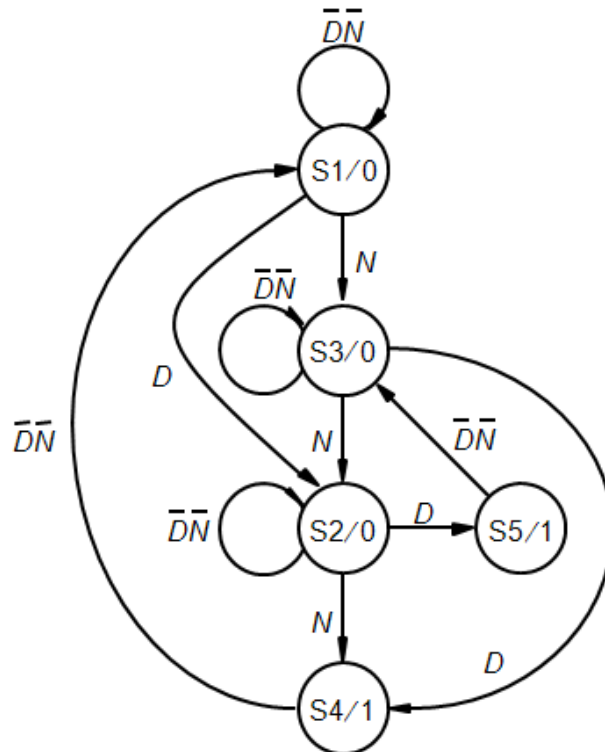


(c) Conditional output box

Figure 8.86. Elements used in ASM charts.

# BV 8.36

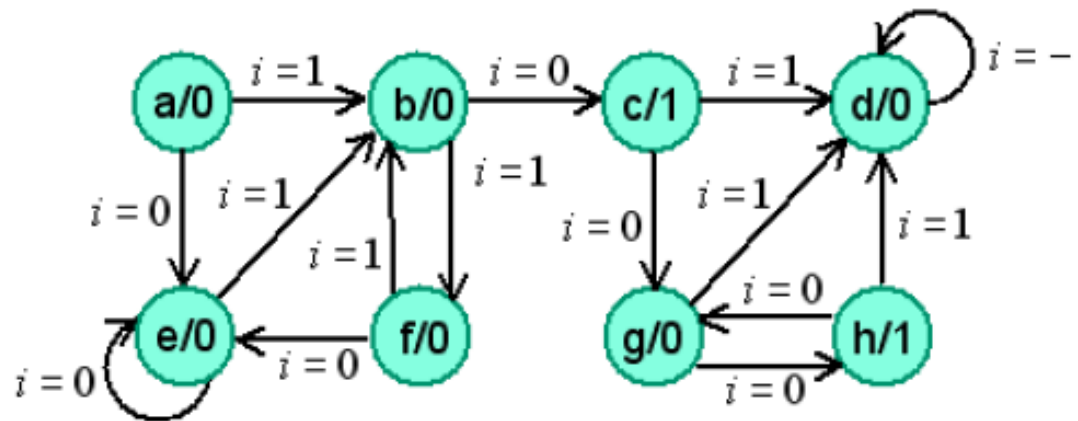
Represent the FSM in Figure 8.57 in form of an ASM chart.



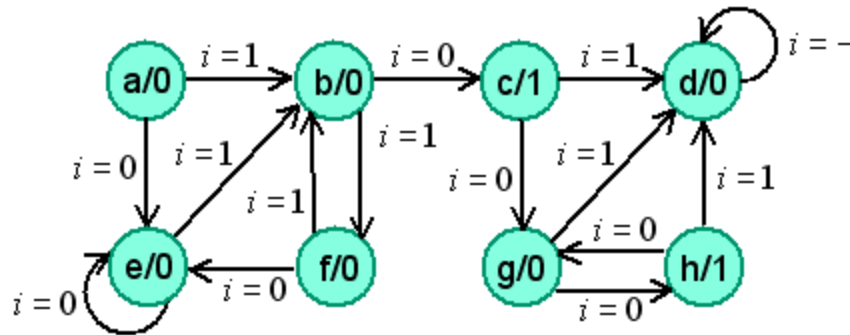
# Ex 10.10 stateminimization

This statediagram is for a synchronous sequential circuit.

- State table
- Minimize states
- Minimal statediagram



# Ex 10.10 stateminimization



Write down the state table

Two states can not be equivalent if the output is different or if subsequent state output is different.

*now next out*

| <i>i =</i> | 0        | 1        | <i>z</i> |
|------------|----------|----------|----------|
| <i>a</i>   | <i>e</i> | <i>b</i> | 0        |
| <i>b</i>   | <i>c</i> | <i>f</i> | 0        |
| <i>c</i>   | <i>g</i> | <i>d</i> | 1        |
| <i>d</i>   | <i>d</i> | <i>d</i> | 0        |
| <i>e</i>   | <i>e</i> | <i>b</i> | 0        |
| <i>f</i>   | <i>e</i> | <i>b</i> | 0        |
| <i>g</i>   | <i>h</i> | <i>d</i> | 0        |
| <i>h</i>   | <i>g</i> | <i>d</i> | 1        |

# Ex 10.10 stateminimization

Groups with the same output:

$$P_1 = (a, b, d, e, f, g)(c, h)$$

Examine subsequent state:

now next out

| $i =$ | 0 | 1 | z |
|-------|---|---|---|
| a     | e | b | 0 |
| b     | c | f | 0 |
| c     | g | d | 1 |
| d     | d | d | 0 |
| e     | e | b | 0 |
| f     | e | b | 0 |
| g     | h | d | 0 |
| h     | g | d | 1 |

$$a_{i=0} \rightarrow (a, b, d, e, f, g) \quad a_{i=1} \rightarrow (a, b, d, e, f, g)$$

$$b_{i=0} \rightarrow (c, h) \quad b_{i=1} \rightarrow (a, b, d, e, f, g)$$

$$d_{i=0} \rightarrow (a, b, d, e, f, g) \quad d_{i=1} \rightarrow (a, b, d, e, f, g)$$

$$e_{i=0} \rightarrow (a, b, d, e, f, g) \quad e_{i=1} \rightarrow (a, b, d, e, f, g)$$

$$f_{i=0} \rightarrow (a, b, d, e, f, g) \quad f_{i=1} \rightarrow (a, b, d, e, f, g)$$

$$g_{i=0} \rightarrow (c, h) \quad g_{i=1} \rightarrow (a, b, d, e, f, g)$$

$(b, g)$  forms a group of them self.

$$P_2 = (a, d, e, f)(b, g)(c, h)$$

# Ex 10.10 stateminimization

now next out

| $i =$ | 0   | 1   | z |
|-------|-----|-----|---|
| $a$   | $e$ | $b$ | 0 |
| $b$   | $c$ | $f$ | 0 |
| $c$   | $g$ | $d$ | 1 |
| $d$   | $d$ | $d$ | 0 |
| $e$   | $e$ | $b$ | 0 |
| $f$   | $e$ | $b$ | 0 |
| $g$   | $h$ | $d$ | 0 |
| $h$   | $g$ | $d$ | 1 |

$$P_2 = (a, d, e, f)(b, g)(c, h)$$

Examine subsequent state :

$$a_{i=0} \rightarrow (a, d, \mathbf{e}, f) \quad a_{i=1} \rightarrow (\mathbf{b}, g)$$

$$d_{i=0} \rightarrow (a, \mathbf{d}, e, f) \quad d_{i=1} \rightarrow (a, \mathbf{d}, e, f)$$

$$e_{i=0} \rightarrow (a, d, \mathbf{e}, f) \quad e_{i=1} \rightarrow (\mathbf{b}, g)$$

$$f_{i=0} \rightarrow (a, d, \mathbf{e}, f) \quad f_{i=1} \rightarrow (\mathbf{b}, g)$$

(d) Forms a group of it self.

$$P_3 = (a, e, f)(b, g)(\mathbf{d})(c, h)$$

# Ex 10.10 stateminimization

now next out

| $i =$ | 0 | 1 | z |
|-------|---|---|---|
| a     | e | b | 0 |
| b     | c | f | 0 |
| c     | g | d | 1 |
| d     | d | d | 0 |
| e     | e | b | 0 |
| f     | e | b | 0 |
| g     | h | d | 0 |
| h     | g | d | 1 |

$$P_3 = (a, e, f)(\boxed{b, g})(d)(c, h)$$

Examine subsequent state :

$$\begin{array}{l} \boxed{b_{i=0} \rightarrow (c, h) \quad b_{i=1} \rightarrow (a, e, f)} \\ \boxed{g_{i=0} \rightarrow (c, h) \quad g_{i=1} \rightarrow (d)} \end{array}$$

(b) (g) forms own groups.

$$P_4 = (a, e, f)(\boxed{b})(d)(\boxed{g})(c, h)$$

# Ex 10.10 stateminimization

now next out

| $i =$ | 0   | 1   | z |
|-------|-----|-----|---|
| $a$   | $e$ | $b$ | 0 |
| $b$   | $c$ | $f$ | 0 |
| $c$   | $g$ | $d$ | 1 |
| $d$   | $d$ | $d$ | 0 |
| $e$   | $e$ | $b$ | 0 |
| $f$   | $e$ | $b$ | 0 |
| $g$   | $h$ | $d$ | 0 |
| $h$   | $g$ | $d$ | 1 |

$$P_4 = (a, e, f)(b)(d)(g)(c, h)$$

Examine subsequent state :

$$\begin{array}{ll} c_{i=0} \rightarrow (\mathbf{g}) & c_{i=1} \rightarrow (\mathbf{d}) \\ h_{i=0} \rightarrow (\mathbf{g}) & h_{i=1} \rightarrow (\mathbf{d}) \end{array}$$

$$P_5 = P_4 \quad \text{Done!}$$

# Ex 10.10 stateminimization

$$P_4 = (a, e, f)(b)(d)(g)(c, h)]$$

|       | now | next | out |
|-------|-----|------|-----|
| $i =$ | 0   | 1    | $z$ |
| $a$   | $e$ | $b$  | 0   |
| $b$   | $c$ | $f$  | 0   |
| $c$   | $g$ | $d$  | 1   |
| $d$   | $d$ | $d$  | 0   |
| $e$   | $e$ | $b$  | 0   |
| $f$   | $e$ | $b$  | 0   |
| $g$   | $h$ | $d$  | 0   |
| $h$   | $g$ | $d$  | 1   |

Changing  
names

$$(a, e, f) \Rightarrow a$$

$$(b) \Rightarrow b$$

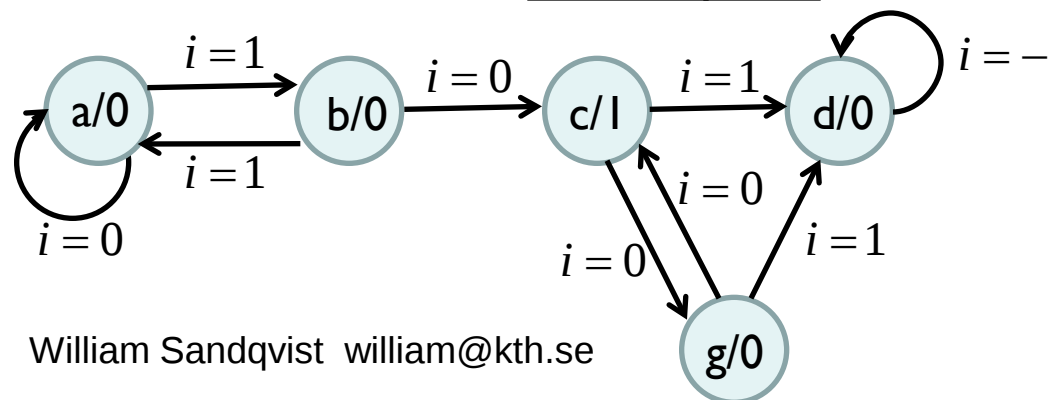
$$(c, h) \Rightarrow c$$

$$(d) \Rightarrow d$$

$$(g) \Rightarrow g$$

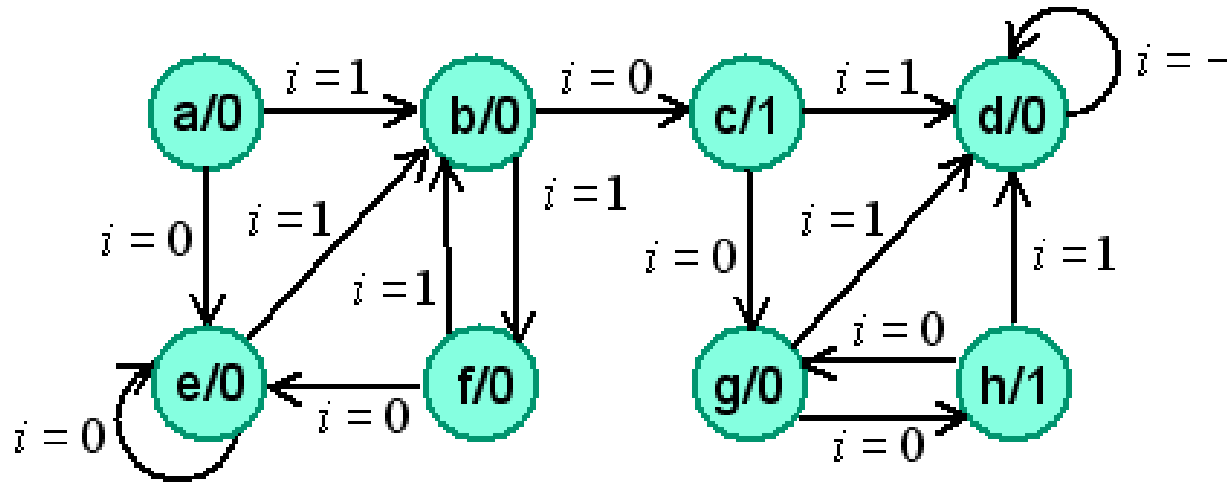
now next out

| $i =$ | 0   | 1   | $z$ |
|-------|-----|-----|-----|
| $a$   | $a$ | $b$ | 0   |
| $b$   | $c$ | $a$ | 0   |
| $c$   | $g$ | $d$ | 1   |
| $d$   | $d$ | $d$ | 0   |
| $g$   | $c$ | $d$ | 0   |



# Ex 10.10 stateminimization

Before:



After:

