



# Last lecture (5)

- Ionosphere
  - index of refraction
  - reflection of radio waves
  - particle drift motion in magnetized plasma
  - electrical conductivity in ionosphere

# Today's lecture (6)

- Magnetosphere, introduction
- Magnetospheric size (standoff distance)
- Particle motion in the magnetosphere



# Today

<u>Activity</u>	<u>Date</u>	<u>Time</u>	<u>Room</u>	<u>Subject</u>	<u>Litterature</u>
L1	31/8	13-15	V22	Course description, Introduction, The Sun 1, Plasma physics 1	CGF Ch 1, 5, (p 110-113)
L2	3/9	15-17	Q36	The Sun 2, Plasma physics 2	CGF Ch 5 (p 114-121), 6.3
L3	7/9	13-15	Q36	Solar wind, The ionosphere and atmosphere 1, Plasma physics 3	CGF Ch 6.1, 2.1-2.6, 3.1-3.2, 3.5, LL Ch III, Extra material
T1	10/9	15-17	Q36	Mini-group work 1	
L4	14/9	13-15	E2	The ionosphere 2, Plasma physics 4	CGF Ch 3.4, 3.7, 3.8
T2	17/9	8-10	Q31	Mini-group work 2	
L5	17/9	15-17	L52	The Earth's magnetosphere 1, Plasma physics 5	CGF 4.1-4.3, LL Ch I, II, IV.A
L6	21/9	13-15	L52	The Earth's magnetosphere 2, Other magnetospheres	CGF Ch 4.6-4.9, LL Ch V.
T3	24/9	16-18	Q36	Mini-group work 3	
L7	28/9	13-15	Q36	Aurora, Measurement methods in space plasmas and data analysis 1	CGF Ch 4.5, 10, LL Ch VI, Extra material
T4	1/10	15-17	V22	Mini-group work 4	
L8	5/10	13-15	M33	Space weather and geomagnetic storms	CGF Ch 4.4, LL Ch IV.B-C, VII.A-C
L9	6/10	8-10	Q36	Interstellar and intergalactic plasma, Cosmic radiation,	CGF Ch 7-9
T5	8/10	15-17	Q34	Mini-group work 5	
L10	12/10	13-15	Q36	Swedish and international space physics research.	
T6	15/10	15-17	Q33	Round-up.	
Written examination	28/10	8-13	Q21, Q26		



# **Sign up for the exam on My Pages (before Oct 14)**

**(Make sure you are registered. If you are not, contact [stex@ee.kth.se](mailto:stex@ee.kth.se))**

# **EF22445 Space Physics II**

## **7.5 ECTS credits, P2**

- shocks and boundaries in space
- solar wind interaction with magnetized and unmagnetized bodies
- reconnection
- sources of magnetospheric plasma
- magnetospheric and ionospheric convection
- auroral physics
- storms and substorms
- global oscillations of the magnetosphere

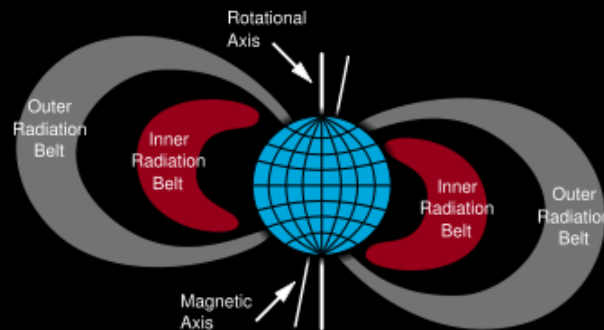
# Courses at the Alfvén Laboratory

## EF2260 SPACE ENVIRONMENT AND SPACECRAFT ENGINEERING , 6 ECTS credits, period 2

- environments spacecraft may encounter in various orbits around the Earth, and the constraints this places on spacecraft design
- basic operation principles underlying the thermal control system and the power systems in spacecraft
- measurements principles in space



*The Astrid-2 satellite*



*Radiation environment in near-earth space*

### Projects:

- Design power supply for spacecraft
- Study of radiation effects on electronics

# Index of refraction for electromagnetic waves in a plasma (corrected)

$$(1) \quad \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$(2) \quad \nabla \times \mathbf{B} = \mu_0 \mathbf{j} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}$$

$$(3) \quad \mathbf{j} = -en_e \mathbf{v}_e$$

$$(4) \quad m_e \frac{\partial \mathbf{v}_e}{\partial t} = -e\mathbf{E}$$

Assume all quantities vary sinusoidally, with frequency  $\omega$ , e.g.:

$$\mathbf{E} = \mathbf{E}_0 e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$$

$$(1) \Rightarrow \nabla \times (\nabla \times \mathbf{E}) = -\nabla \times \frac{\partial \mathbf{B}}{\partial t}$$

$$(2) \Rightarrow \nabla \times \frac{\partial \mathbf{B}}{\partial t} = \mu_0 \frac{\partial \mathbf{j}}{\partial t} + \frac{1}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2}$$

$$\therefore \nabla \times (\nabla \times \mathbf{E}) = +\mu_0 \frac{\partial}{\partial t} (en_e \mathbf{v}_e) - \frac{1}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2}$$

$\Rightarrow$

$$\nabla (\nabla \cdot \mathbf{E}) - \nabla^2 \mathbf{E} = +\mu_0 en_e \frac{\partial \mathbf{v}_e}{\partial t} - \frac{1}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2}$$

$\Rightarrow$

# Index of refraction for electromagnetic waves in a plasma (corrected)

~~$$ik(\mathbf{k} \cdot \mathbf{E}) - k^2 \mathbf{E} = \mu_0 (-i\omega) en_e \mathbf{v}_e - \frac{1}{c^2} (-i\omega)^2 \mathbf{E}$$~~

*Does not represent E.M. wave*

(4)  $\Rightarrow$

$$k^2 \mathbf{E} = -\mu_0 en_e \frac{e\mathbf{E}}{m_e} + \frac{1}{c^2} \omega^2 \mathbf{E}$$

$\Rightarrow$

$$c^2 k^2 = -c^2 \frac{\mu_0 n_e e^2}{m_e} + \omega^2 = \frac{-1}{\cancel{\mu_0 \epsilon_0}} \frac{\cancel{\mu_0} n_e e^2}{m_e} + \omega^2$$

$$\therefore \omega^2 = c^2 k^2 + \omega_p^2$$

$$n^2 = \frac{c^2}{v_{ph}^2} = \frac{c^2 k^2}{\omega^2} = \frac{\omega^2 - \omega_p^2}{\omega^2} = 1 - \frac{\omega_p^2}{\omega^2}$$

$\therefore$

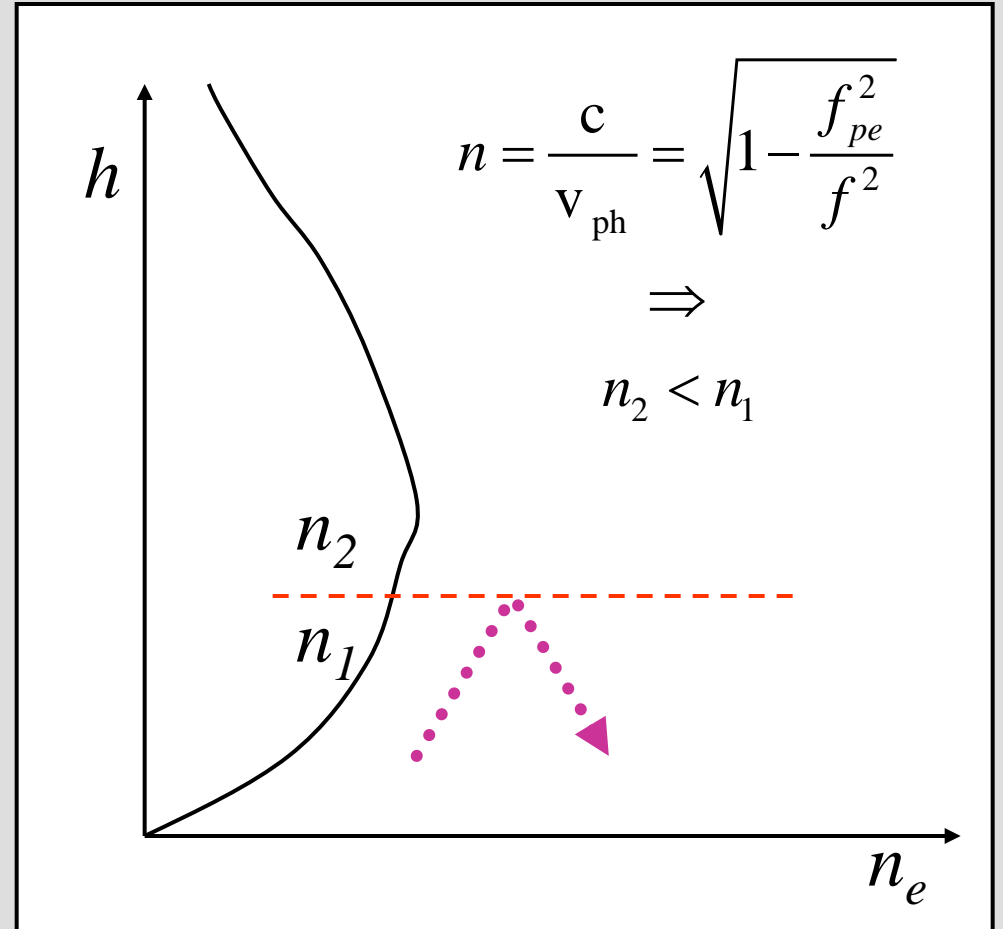
$$n = \sqrt{1 - \frac{\omega_p^2}{\omega^2}} = \sqrt{1 - \frac{f_p^2}{f^2}}$$

# Where does the total reflection take place?

Large gradient when

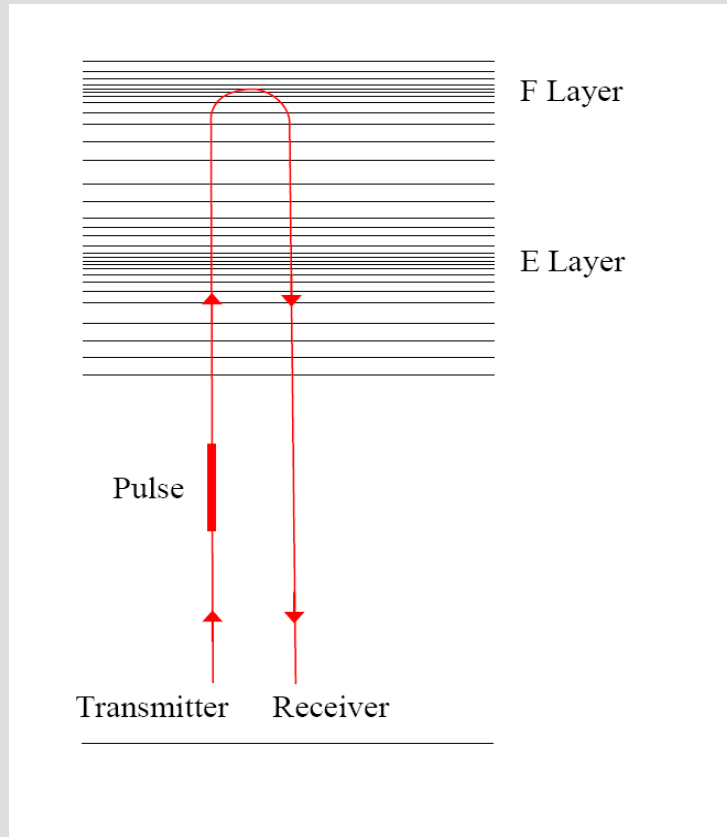
$$f \approx f_{pe}$$

Higher frequencies  $\rightarrow$  higher  $f_{pe}(n_e)$





# Ionosonde



The pulse will be reflected where

$$f = f_{pe}$$

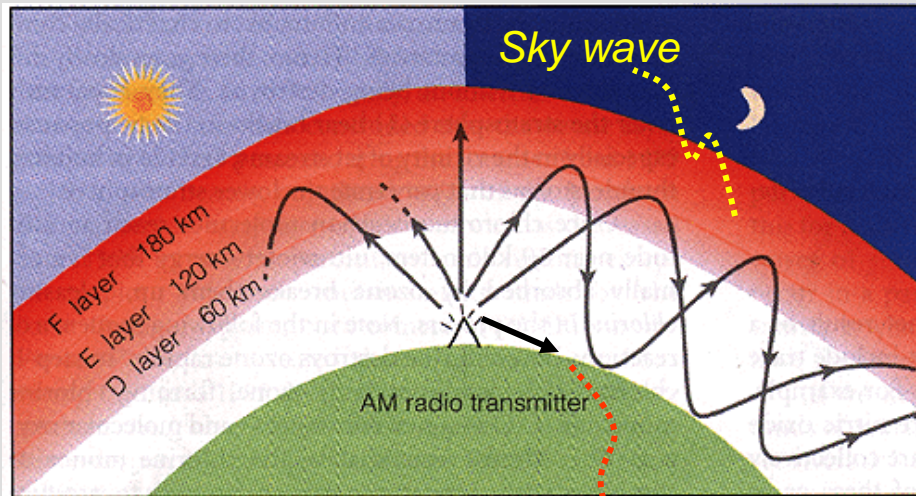
The altitude will be determined by

$$2h = ct$$

Where  $t$  is the time between when the pulse is sent out and the registered again.

# Reflection of radio waves

*F2-layer during night:*

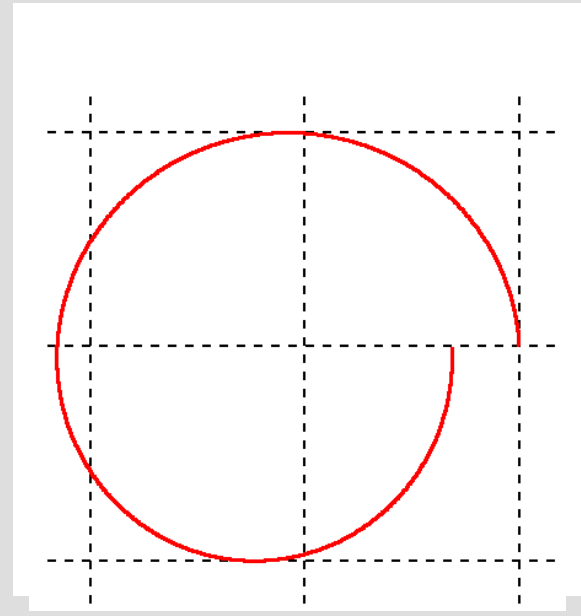
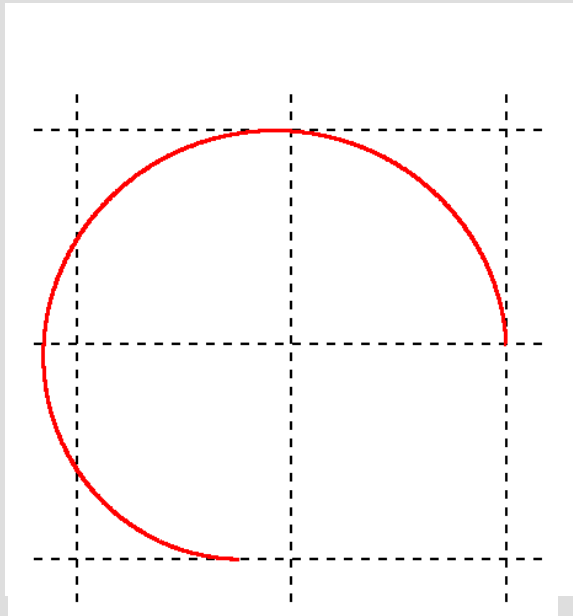
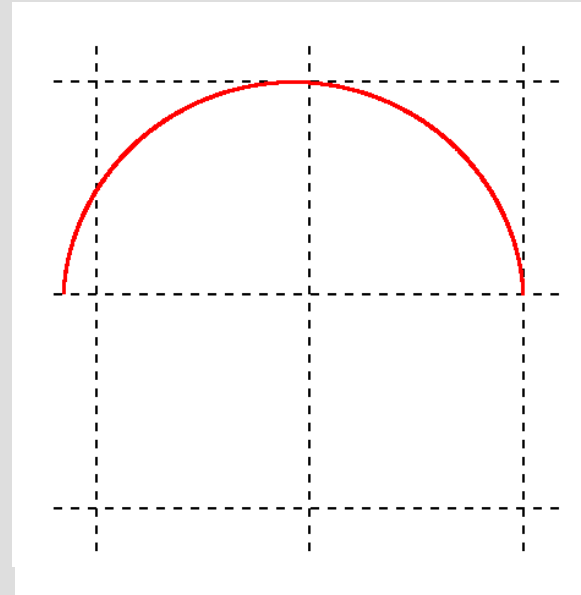
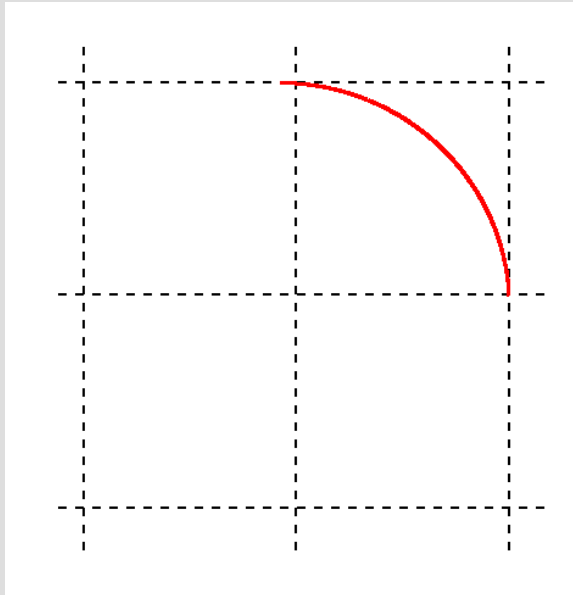


*Ground wave*

$$n_e = 5 \cdot 10^{11} \text{ m}^{-3} \Rightarrow$$

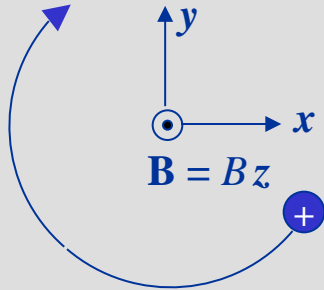
$$f_{pe} = 10^7 \text{ Hz} = 10 \text{ MHz}$$

= HF/short wave



# Drift motion

Consider a charged particle in a magnetic field.



Assume an electric field in the x-z plane:

$$\mathbf{E} = (E_x, 0, E_z)$$

$$m \frac{d\mathbf{v}}{dt} = q(\mathbf{v} \times \mathbf{B} + \mathbf{E}) \implies$$

$$\left\{ \begin{array}{l} m \frac{dv_x}{dt} = qv_y B + qE_x \\ m \frac{dv_y}{dt} = -qv_x B \\ m \frac{dv_z}{dt} = qE_z \end{array} \right. \quad \text{Constant acceleration along } z$$



$$\left\{ \begin{array}{l} \frac{d^2 v_x}{dt^2} = \frac{qB}{m} \frac{dv_y}{dt} = \omega_g \frac{dv_y}{dt} = -\omega_g^2 v_x \\ \frac{d^2 v_y}{dt^2} = -\frac{qB}{m} \frac{dv_x}{dt} = -\omega_g \frac{dv_x}{dt} = -\omega_g^2 v_y - \frac{q^2 B}{m^2} E_x \end{array} \right.$$



# Drift motion

$$\begin{cases} \frac{d^2 v_x}{dt^2} = \frac{qB}{m} \frac{dv_y}{dt} = \omega_g \frac{dv_y}{dt} = -\omega_g^2 v_x \\ \frac{d^2 v_y}{dt^2} = -\frac{qB}{m} \frac{dv_x}{dt} = -\omega_g \frac{dv_x}{dt} = -\omega_g^2 v_y - \frac{q^2 B}{m^2} E_x \end{cases}$$

∴

$$\begin{cases} \frac{d^2 v_x}{dt^2} - \omega_g^2 v_x \\ \frac{d^2 \left( v_y + \frac{E_x}{B} \right)}{dt^2} = -\omega_g^2 \left( v_y + \frac{E_x}{B} \right) \end{cases}$$



$$\begin{cases} v_x = v_{\perp} e^{i\omega_g t + \delta_x} \\ v_y = -\frac{E_x}{B} + v_{\perp} e^{i\omega_g t + \delta_y} \end{cases}$$

Average over a gyro period:

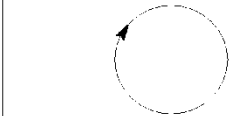
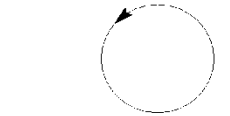
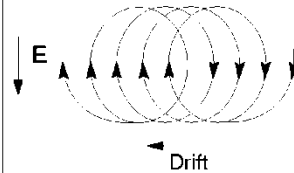
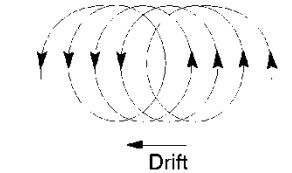
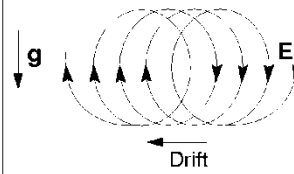
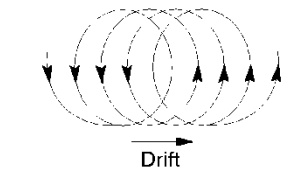
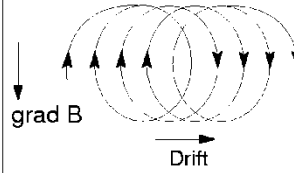
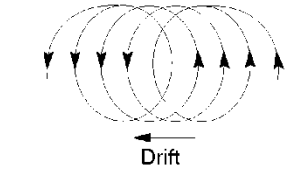
$$v_{drift,y} = -\frac{E_x}{B} = -\frac{E_x B_z}{B^2} = \frac{(\mathbf{E} \times \mathbf{B})_y}{B^2}$$

In general:

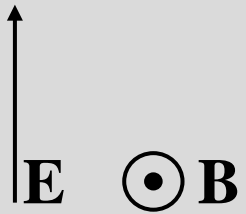
$$\mathbf{v}_{drift} = \frac{\mathbf{E} \times \mathbf{B}}{B^2} = \frac{q\mathbf{E} \times \mathbf{B}}{qB^2} = \frac{\mathbf{F} \times \mathbf{B}}{qB^2}$$

# Drift motion

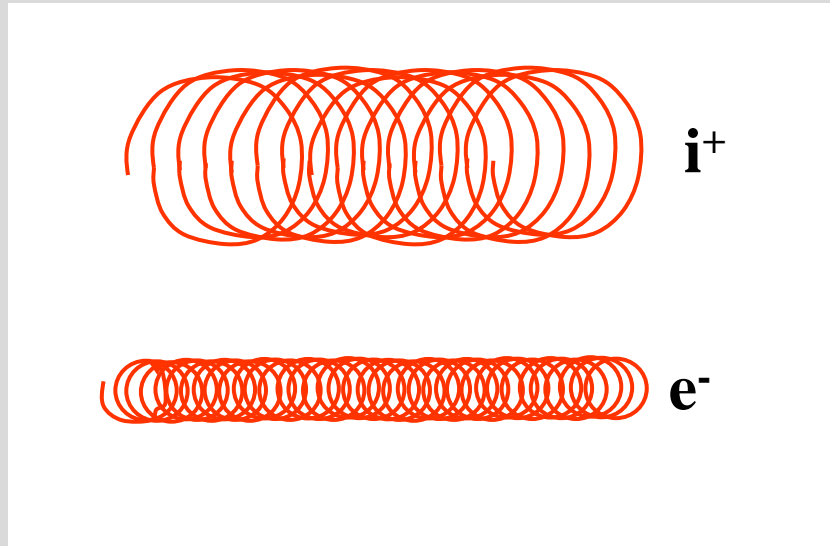
$$\mathbf{u}_{drift} = \frac{\mathbf{F} \times \mathbf{B}}{qB^2}$$

	Positive particles	Negative particles
Homogeneous magnetic field No disturbing force $\mathbf{F} = 0$		
Homogeneous magnetic field Homogeneous electric field $\mathbf{F} = q\mathbf{E}$		
Homogeneous magnetic field Gravitation $\mathbf{F} = m\mathbf{g}$		
Inhomogeneous magnetic field $\mathbf{F} = -\mu \text{grad } \mathbf{B}$		

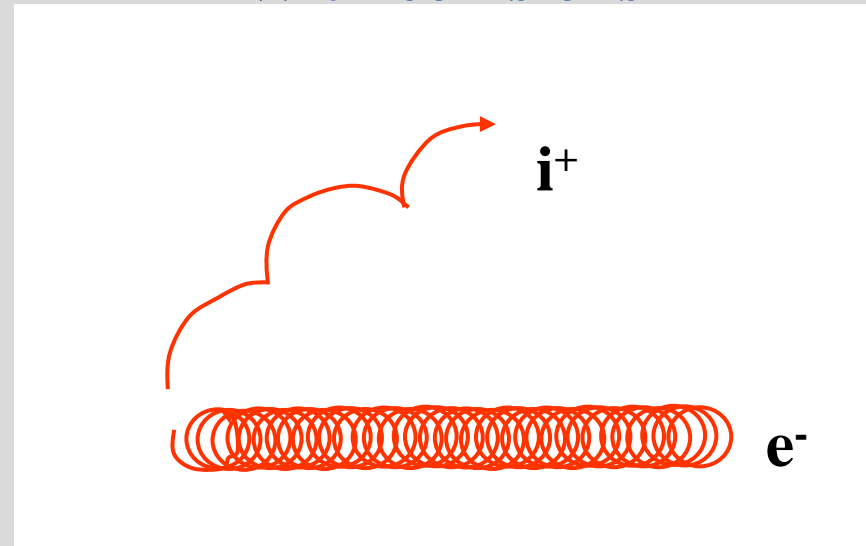
# ExB-drift



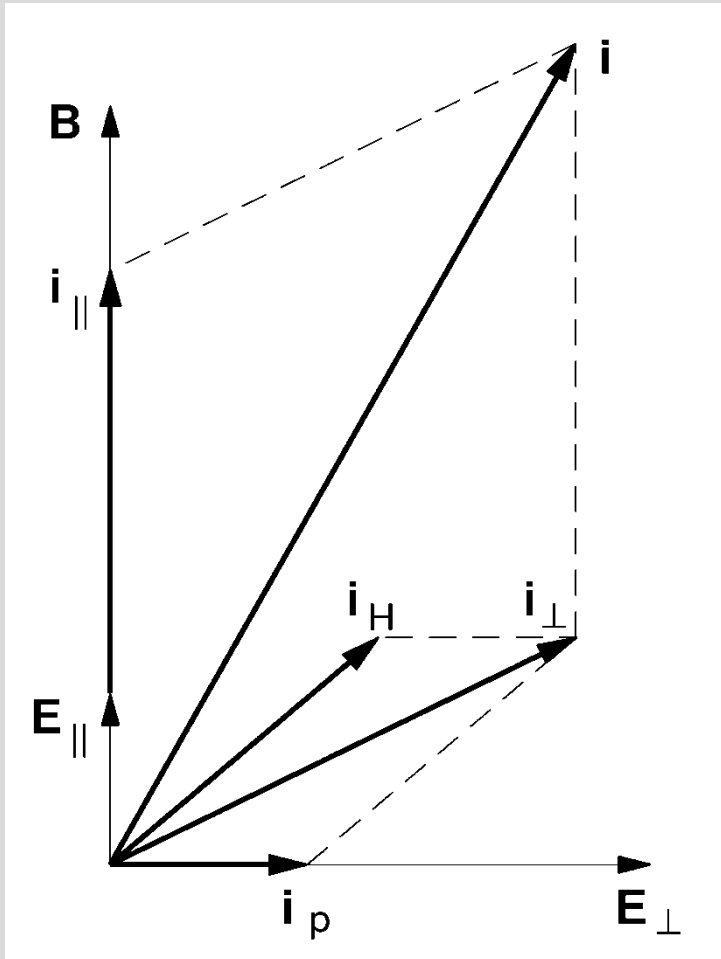
Without collisions



With collisions



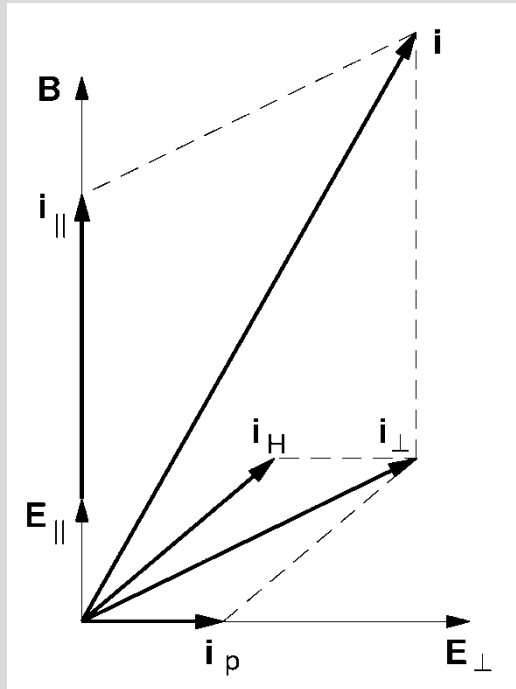
# Electric conductivity in a magnetized plasma



- $i_{\parallel}$  = parallel current
- $i_p$  = Pedersen current
- $i_H$  = Hall current



# Electric conductivity in a magnetized plasma II



$$\sigma_P = \sigma_e \frac{1}{1 + \omega_{ge}^2 \tau_e^2} + \sigma_i \frac{1}{1 + \omega_{gi}^2 \tau_i^2}$$

$$\sigma_H = \sigma_e \frac{\omega_{ge} \tau_e}{1 + \omega_{ge}^2 \tau_e^2} - \sigma_i \frac{\omega_{gi} \tau_i}{1 + \omega_{gi}^2 \tau_i^2}$$

$$\sigma_{//} = \sigma_e + \sigma_i$$

$$\sigma_e = e^2 n \tau_e / m_e$$

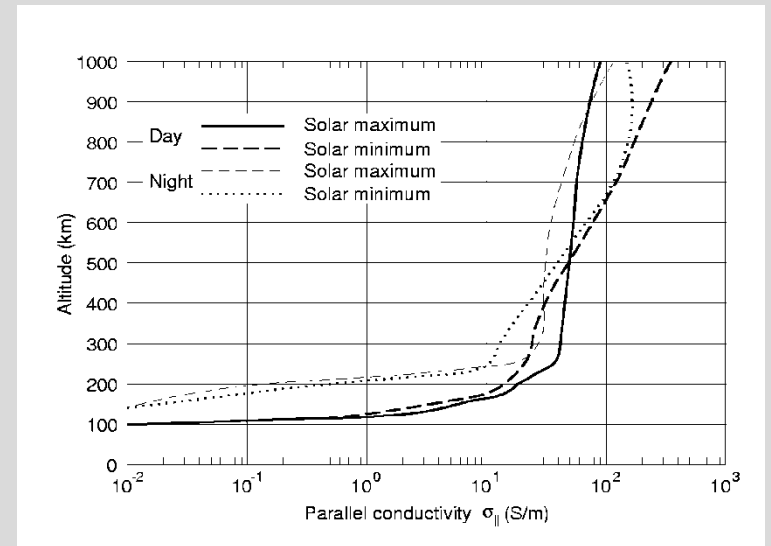
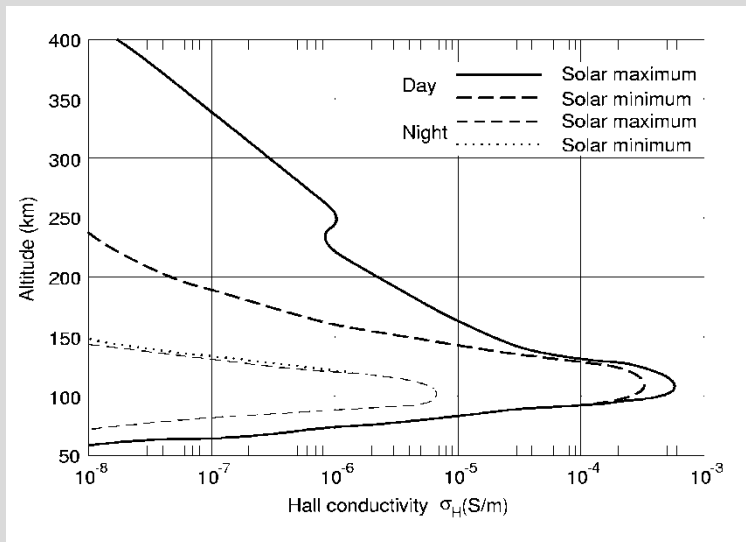
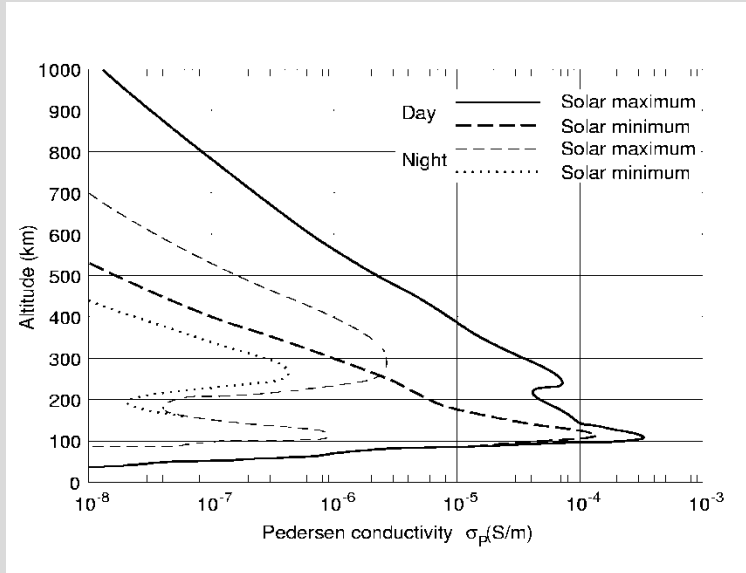
$$\sigma_i = e^2 n \tau_i / m_i$$

$$i_{//} = \sigma_{//} E_{//}$$

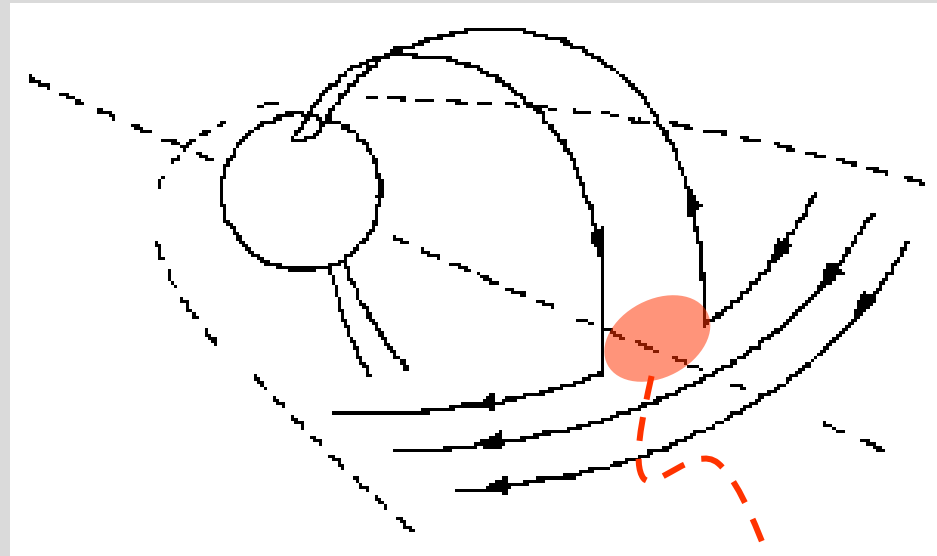
$$\left. \begin{aligned} i_P &= \sigma_P E_{\perp} \\ i_H &= \sigma_H E_{\perp} \end{aligned} \right\}$$

$$\text{or } \mathbf{i}_{\perp} = \sigma_P \mathbf{E}_{\perp} + \sigma_H \frac{\mathbf{B} \times \mathbf{E}_{\perp}}{B}$$

# Ionospheric conductivities



# Consequence: Birkeland currents



Region of low conductivity

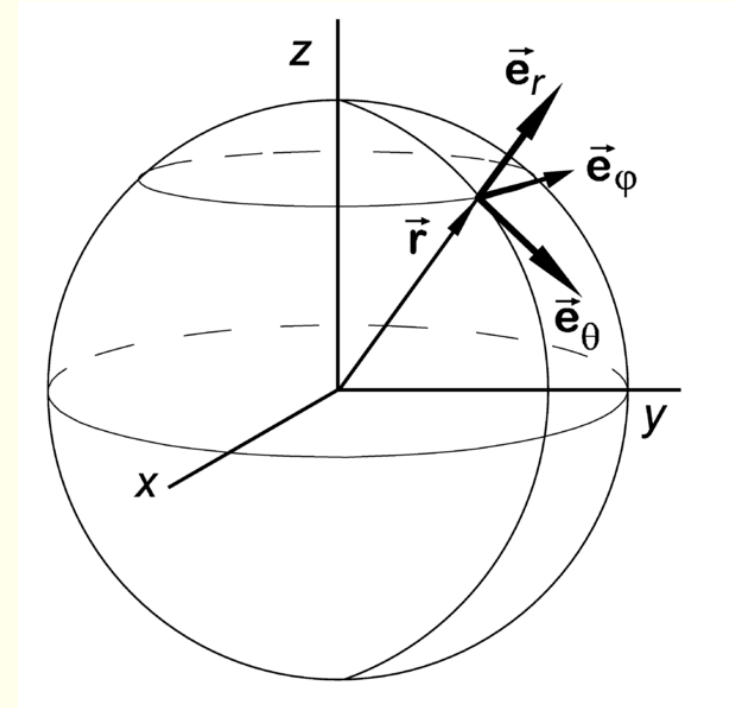
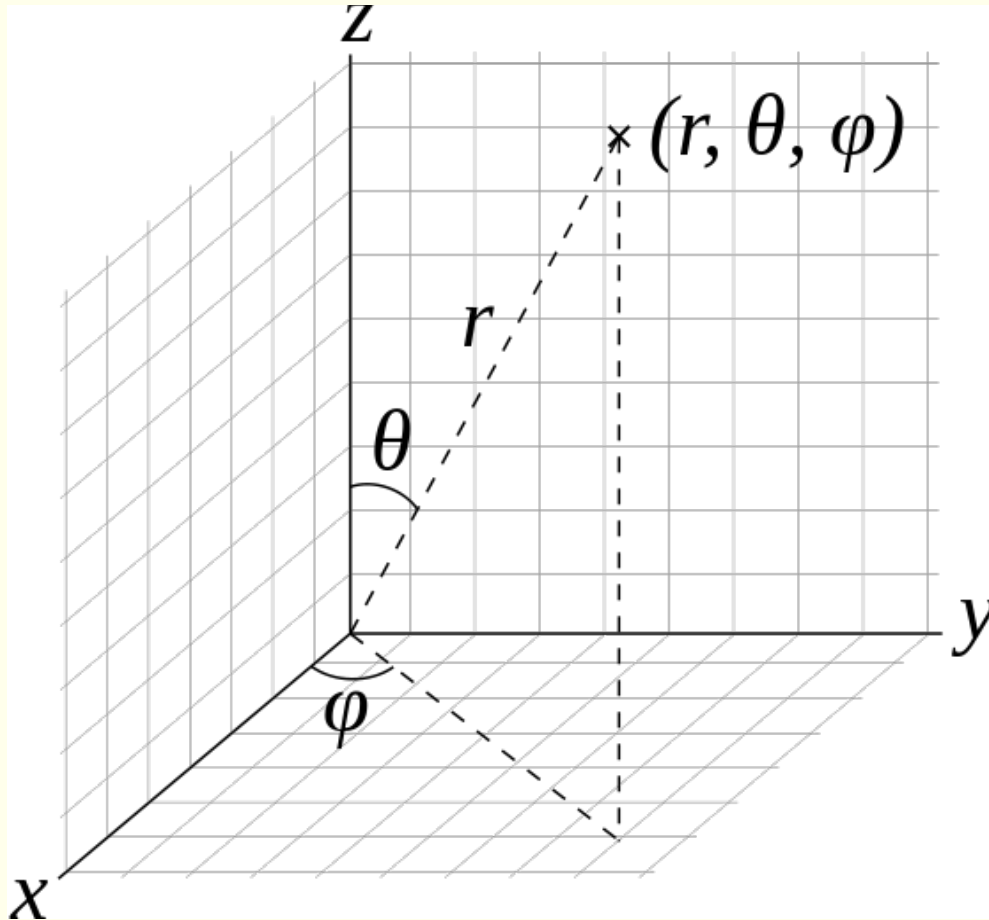
When the conductivity out in the magnetosphere is low, it is easier for the current to close through the ionosphere via currents parallel to the geomagnetic field. Such currents are called *Birkeland* currents.



# How do we define "the magnetosphere"?

The region in space where the magnetic field is dominated by the geomagnetic field.

# Polar (spherical) coordinates



$$r = \sqrt{x^2 + y^2 + z^2}$$

$$\theta = \arccos\left(\frac{z}{r}\right)$$

$$\varphi = \arctan\left(\frac{y}{x}\right)$$

$$x = r \sin \theta \cos \varphi$$

$$y = r \sin \theta \sin \varphi$$

$$z = r \cos \theta$$

# Geomagnetic field

Approximated by a dipole close to Earth.

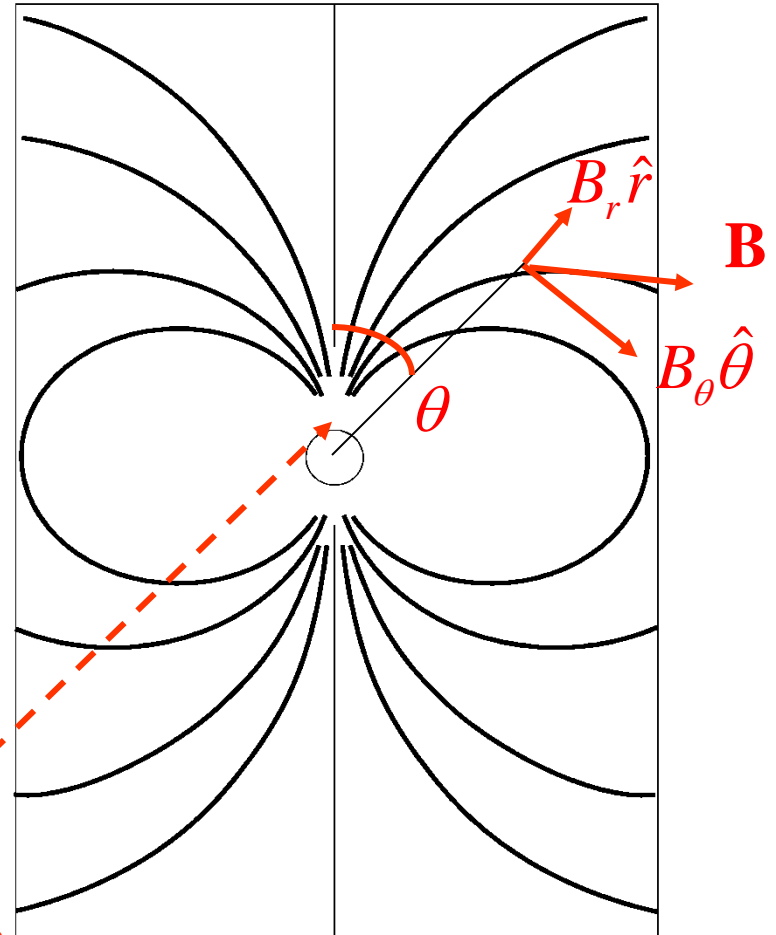
$$B_r = B_p \left(\frac{R_E}{r}\right)^3 \cos \theta$$

$$B_\theta = \frac{B_p}{2} \left(\frac{R_E}{r}\right)^3 \sin \theta$$

$$a = \frac{2\pi R_E^3 B_p}{\mu_0}$$

magnetic dipole moment

Magnetic field at the  
"north pole"



# Geomagnetic field

Alternative formulation of dipole field

$$B_r = B_p \left(\frac{R_E}{r}\right)^3 \cos \theta$$

$$B_\theta = \frac{B_p}{2} \left(\frac{R_E}{r}\right)^3 \sin \theta$$

$$B_r = \frac{\mu_0 a}{2\pi} \frac{1}{r^3} \cos \theta$$

$$B_\theta = \frac{\mu_0 a}{2\pi} \cdot \frac{1}{2} \cdot \frac{1}{r^3} \sin \theta$$

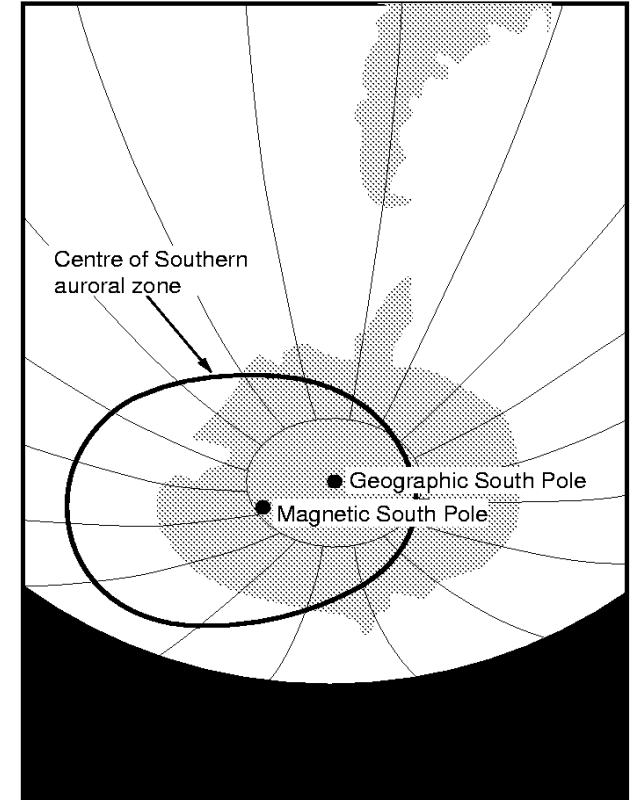
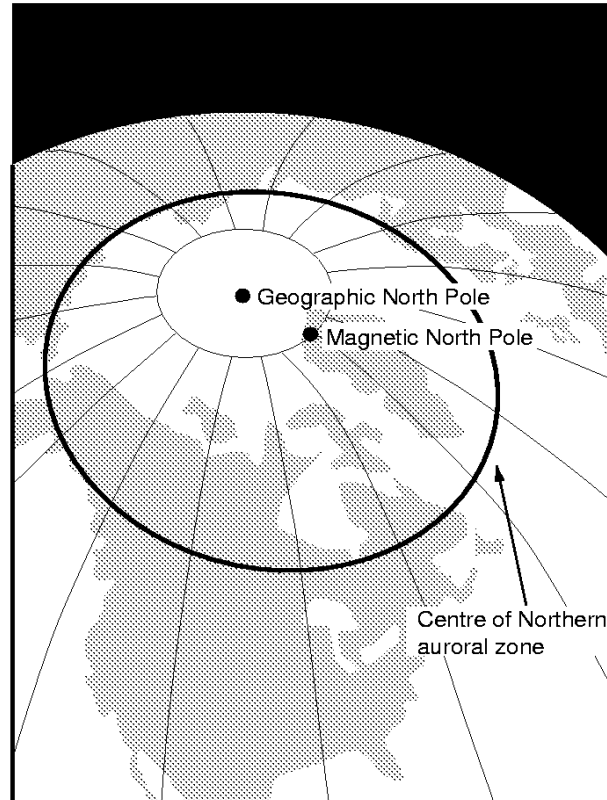
$$a = \frac{2\pi R_E^3 B_p}{\mu_0}$$

 magnetic dipole moment

# Geomagnetic field

- Angle between dipole axis and spin axis:  $\approx 11^\circ$
- The geographic north pole is a magnetic south pole, and vice versa.
- $B_{equator} = 31 \mu\text{T}$ ,

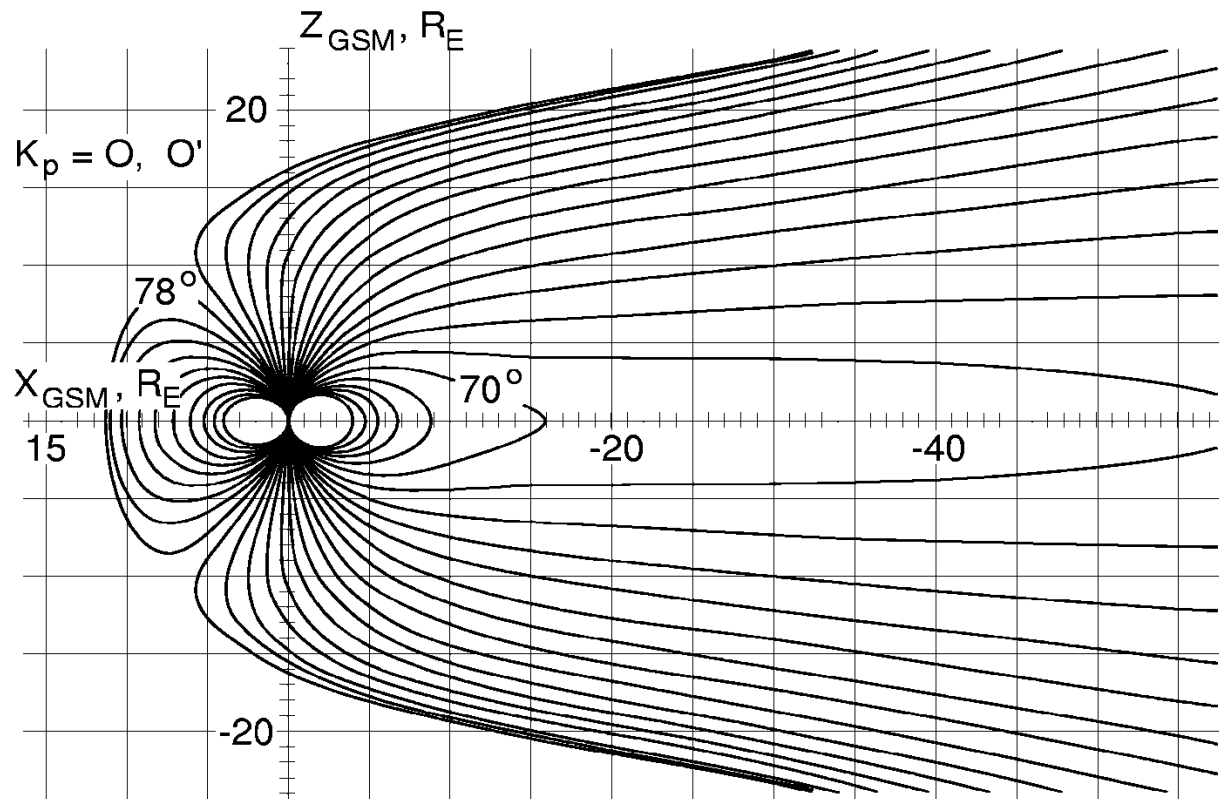
$$B_{pole} = 62 \mu\text{T}$$



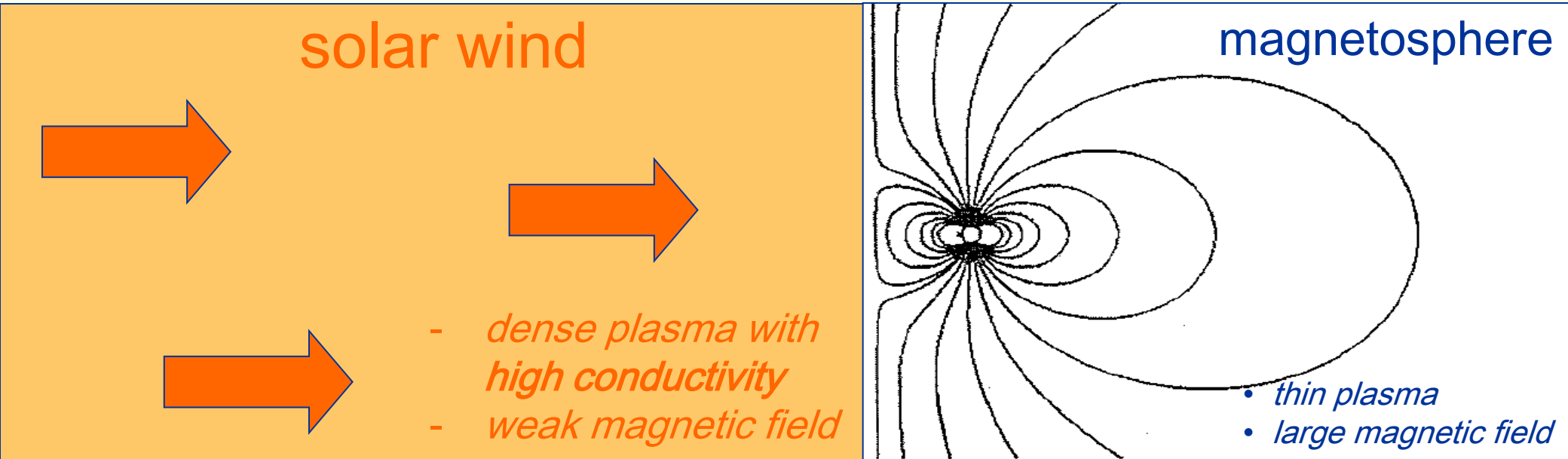


# Geomagnetic field

Modified by solar wind into tail-like configuration



# Stand-off distance from pressure balance



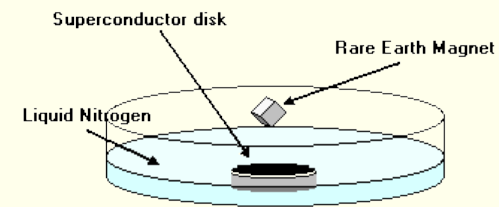
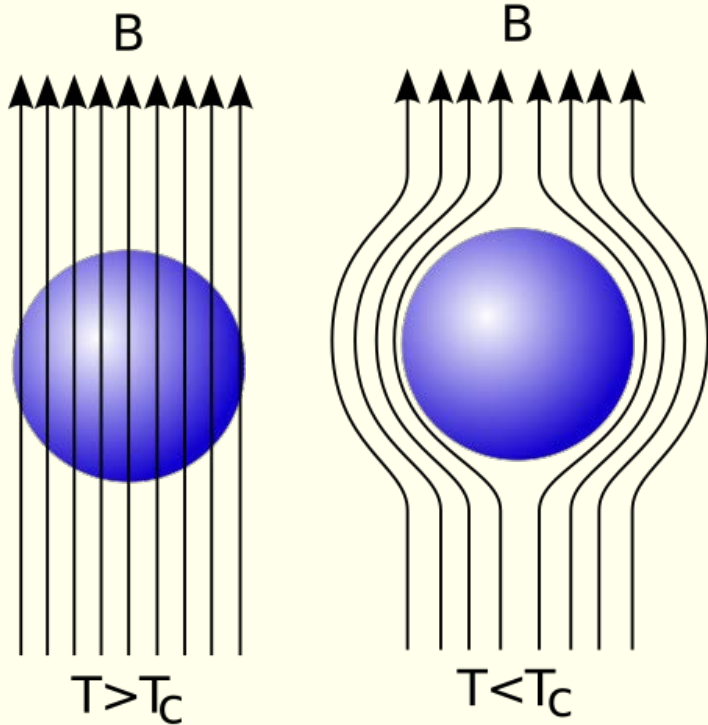
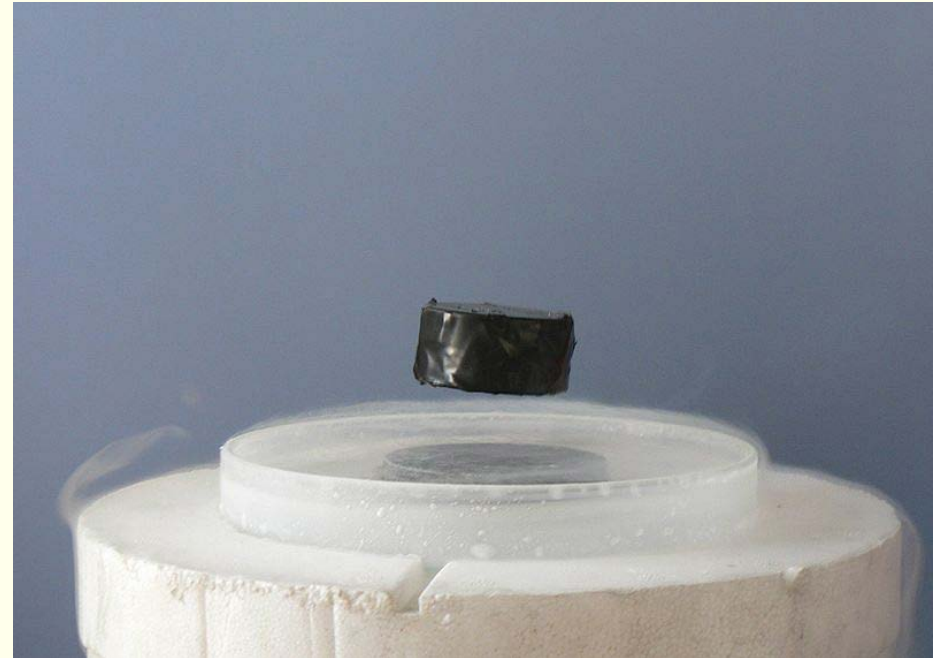
Dynamic pressure:

$$p_d = \rho_{SW} v_{SW}^2$$

Magnetic pressure:

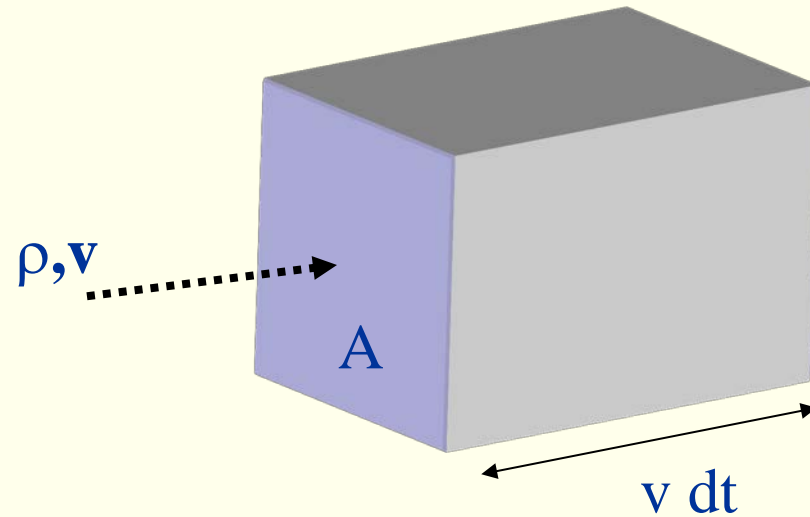
$$p_B = \frac{B^2}{2\mu_0}$$

# Meissner effect in super-conductors



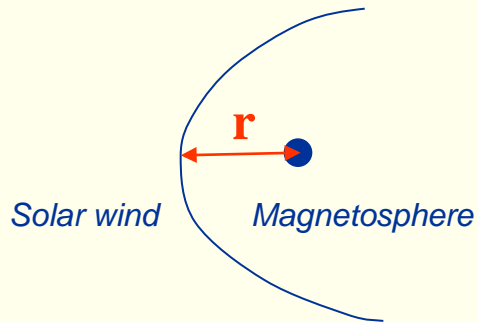
The Meissner Effect

# Dynamic (kinetic) pressure



$$p_d = \frac{F}{A} = \frac{d(mv)}{dt} \frac{1}{A} \approx \frac{\Delta(mv)}{\Delta t} \frac{1}{A} = \frac{\rho \cdot Av\Delta t \cdot v}{\Delta t A} = \rho v^2$$

# Magnetopause “stand-off distance”



Dynamic pressure:  $p_d = \rho_{SW} v_{SW}^2$

Magnetic pressure:  $p_B = \frac{1}{2\mu_0} B^2$

Dipole field strength  
(in equatorial plane):  $B = \frac{\mu_0 a}{4\pi} \frac{1}{r^3}$

$$p_d = p_B \Rightarrow \rho_{SW} v_{SW}^2 = \left[ \frac{\mu_0 a}{4\pi} \frac{1}{r^3} \right]^2 / 2\mu_0 \Rightarrow$$

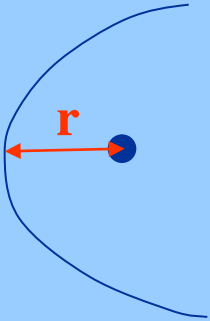
$$r = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

$a = 8 \times 10^{22} \text{ Am}^2$ ,  $v = 500 \text{ km/s}$ ,  $\rho_{SW} = 10^7 \times 1.7 \times 10^{-27} \text{ kg/m}^3$ :

$r = 7 R_e$  (1  $R_e = 6378 \text{ km}$ )

# Standoff distance

$$v=500 \text{ km/s}, \quad \rho_{SW}=10^7 \times 1.7 \times 10^{-27} \text{ kg/m}^3: \quad \mathbf{r = 7 R_e}$$



$$r = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

How will the standoff distance change if the magnetosphere is hit by a coronal mass ejection (CME)? ( $\rho = 10\rho_{SW}$ ,  $v = 1000 \text{ km/s}$ )

Blue

$$r = 1.8 R_e$$

Yellow

$$r = 5.8 R_e$$

Green

$$r = 3.8 R_e$$

Red

$$r = 9.8 R_e$$

# Standoff distance

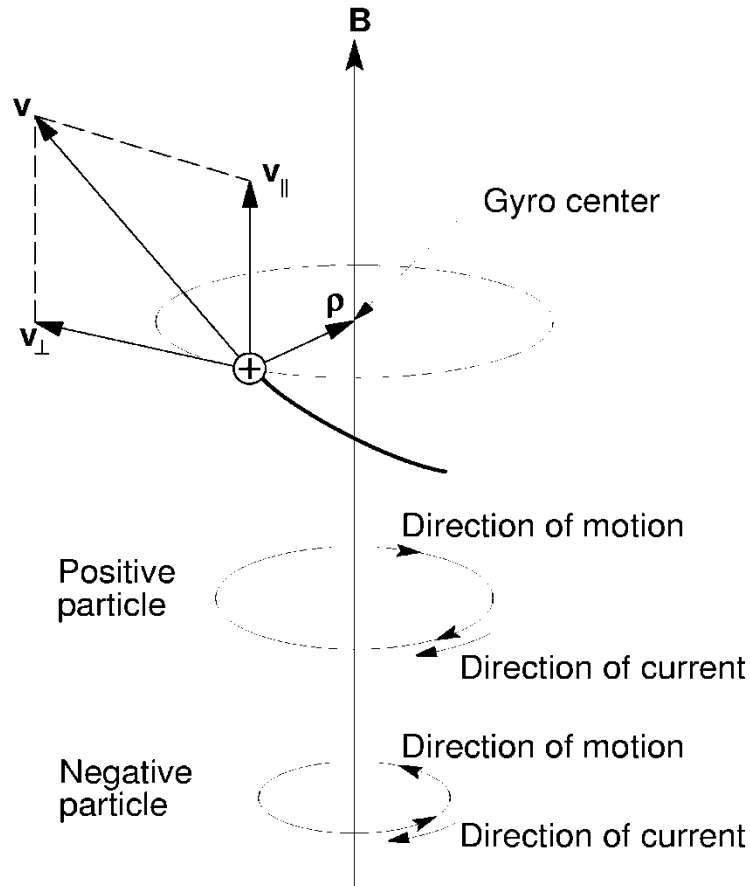
$$r = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \mathbf{10} \rho_{SW} (\mathbf{2}v)_{SW}^2 \right)^{-1/6} = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6} \mathbf{40}^{-1/6}$$

$$40^{-1/6} \cdot 7 = 0.54 \cdot 7 = 3.8$$

Green

$$r = 3.8 R_e$$

# Particle motion in magnetic field



## gyro radius

$$\rho = \frac{mv_{\perp}}{qB}$$

## gyro frequency

$$\omega_g = \frac{qB}{m}$$

## magnetic moment

$$\mu = IA = q f_g \pi \rho^2 = mv_{\perp}^2 / 2B$$





# Adiabatic invariant

## DEFINITION:

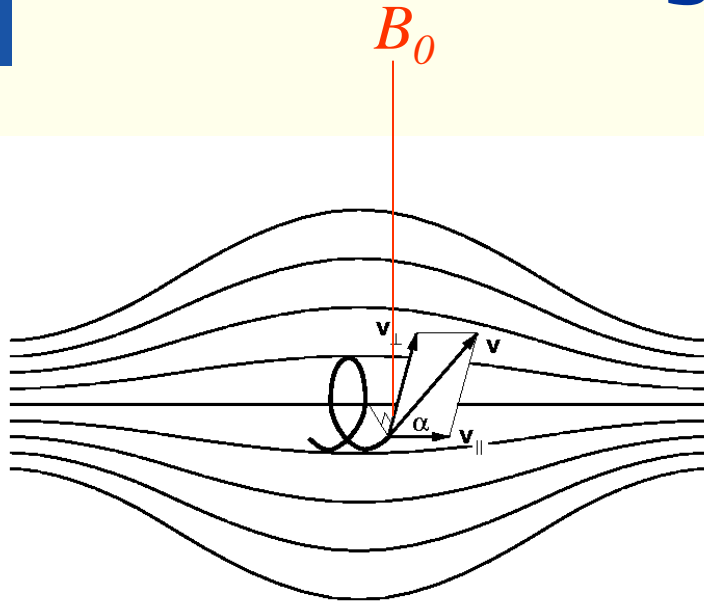
An **adiabatic invariant** is a property of a physical system which stays constant when changes are made slowly.

*By 'slowly' in the context of charged particle motion in magnetic fields, we mean much slower than the gyroperiod.*

'First adiabatic invariant' of particle drift:

$$\mu = \frac{mv_{\perp}^2}{2B}$$

# Magnetic mirror



$mv^2/2$  constant (energy conservation) 

$$\frac{\sin^2 \alpha}{B} = \textit{konst}$$

What happens with  $\alpha$  as the particle moves into the stronger magnetic field?

The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

Red

$\alpha$  increases

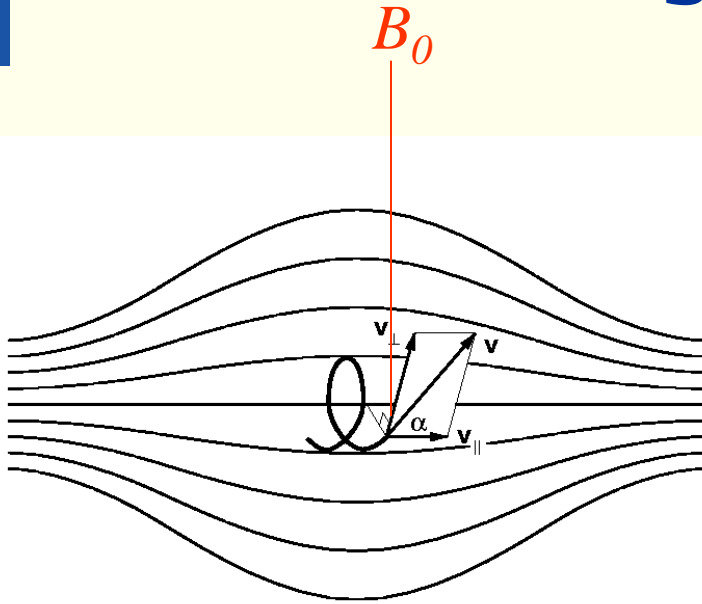
Yellow

$\alpha$  decreases

# Magnetic mirror

$mv^2/2$  constant (energy conservation) 

$$\frac{\sin^2 \alpha}{B} = konst$$



The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

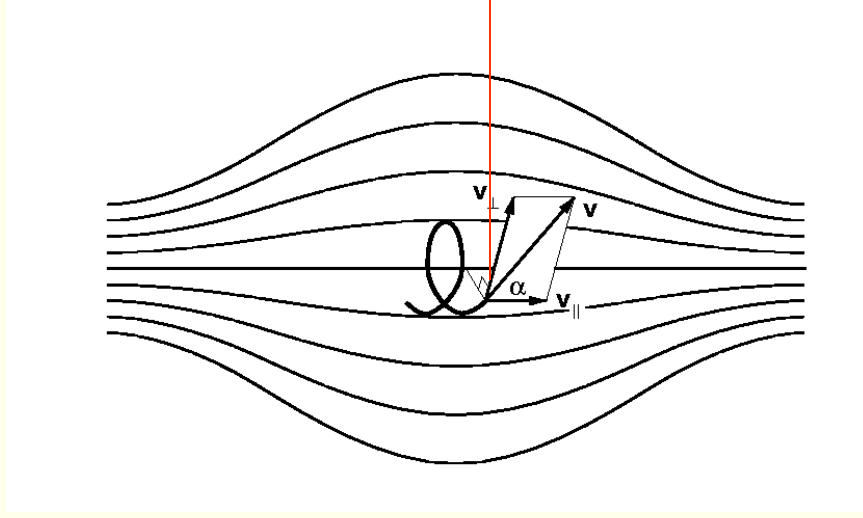
What happens with  $\alpha$  as the particle moves into the stronger magnetic field?

$$\sin \alpha = \sqrt{B \cdot konst}$$

**Red**

$\alpha$  increases

# Magnetic mirror



The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

$mv^2/2$  constant (energy conservation)  $\rightarrow$

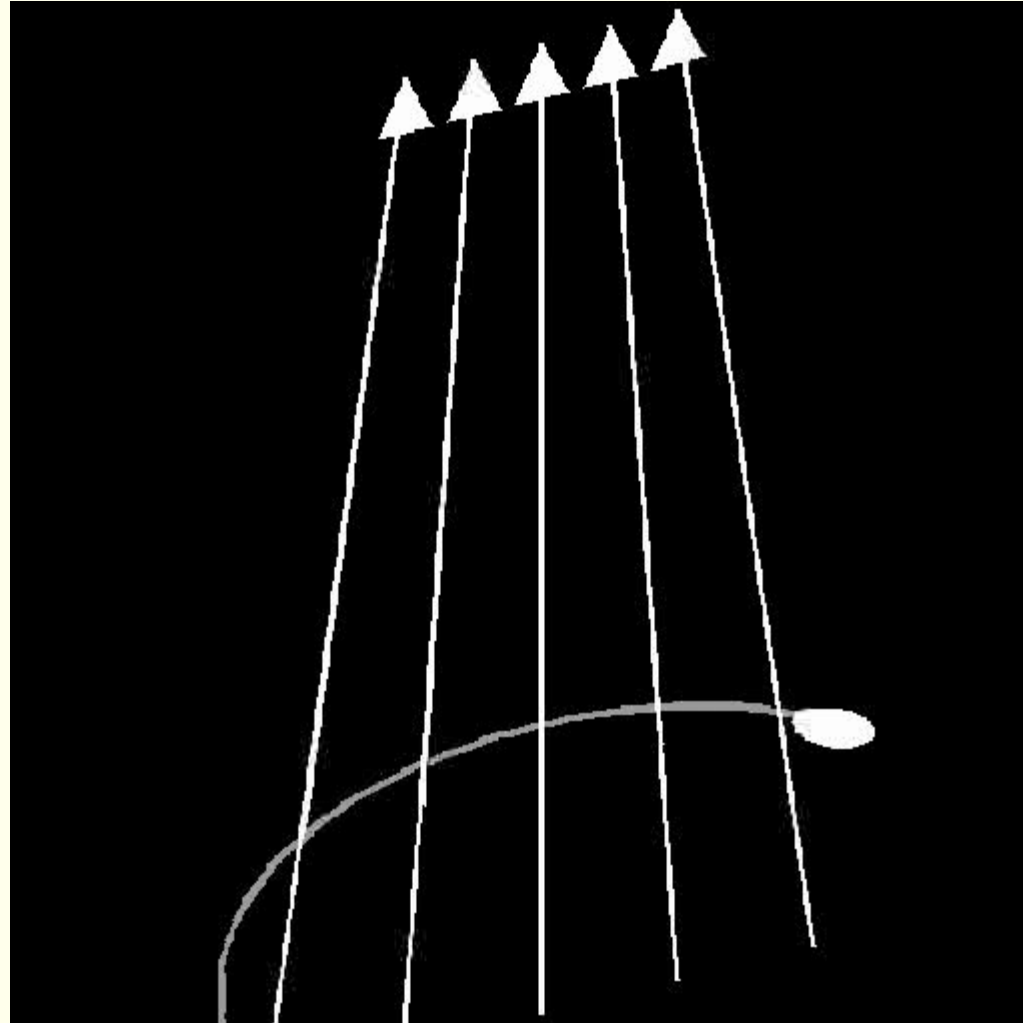
$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$   $\rightarrow$

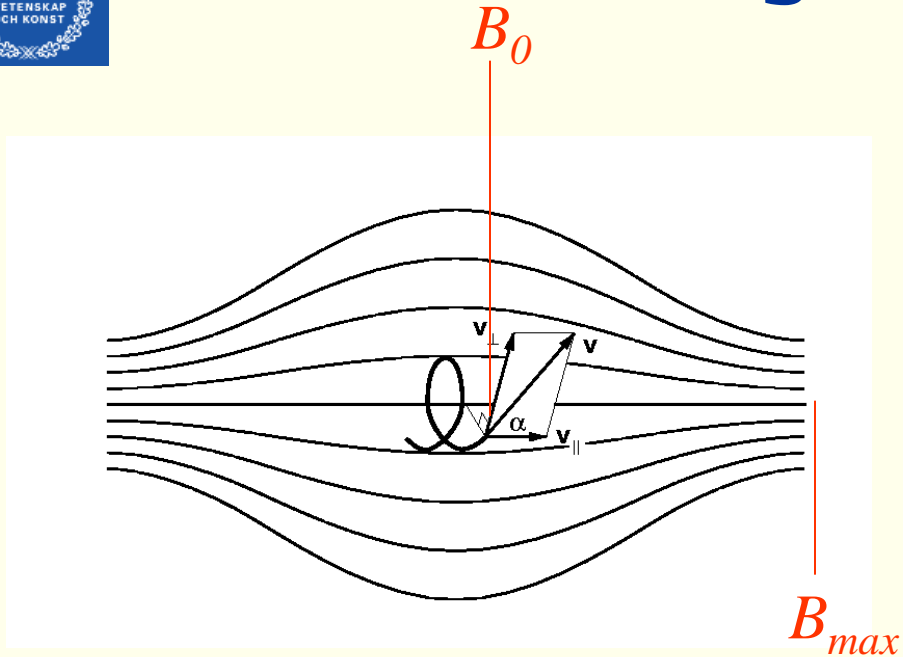
$$\frac{B_{\text{turn}}}{\sin^2 90^\circ} = \frac{B_0}{\sin^2 \alpha} \rightarrow$$

$$B_{\text{turn}} = \frac{B_0}{\sin^2 \alpha}$$

# Magnetic mirror



# Magnetic mirror



$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = konst$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{turn} = B_0 / \sin^2 \alpha$$

If maximal  $B$ -field is  $B_{max}$  a particle with pitch angle  $\alpha$  can only be turned around if

$$B_{turn} = B_0 / \sin^2 \alpha \leq B_{max} \rightarrow$$

$$\alpha > \alpha_{lc} = \arcsin \sqrt{B_0 / B_{max}}$$

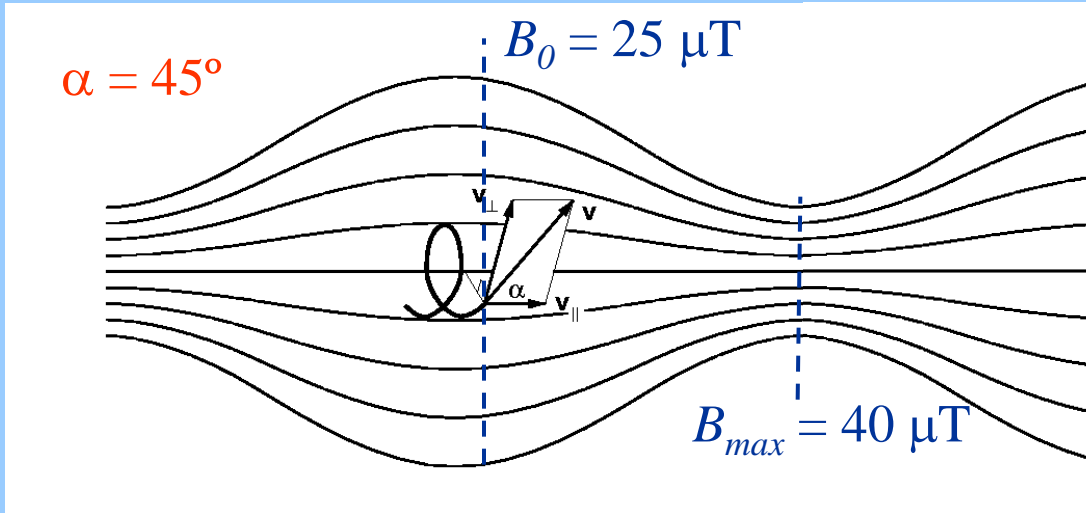
Particles in  
loss cone :

$$\alpha < \alpha_{lc}$$

The magnetic moment  $\mu$  is an  
*adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

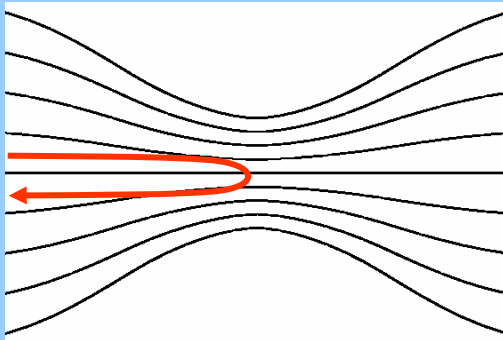
# What will happen to the particle?



$$\alpha_{lc} = \arcsin \sqrt{B_0 / B_{max}}$$

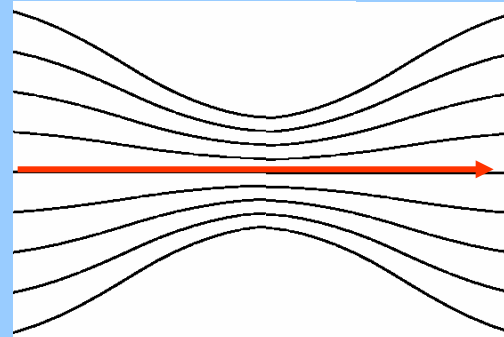
Blue

It will mirror

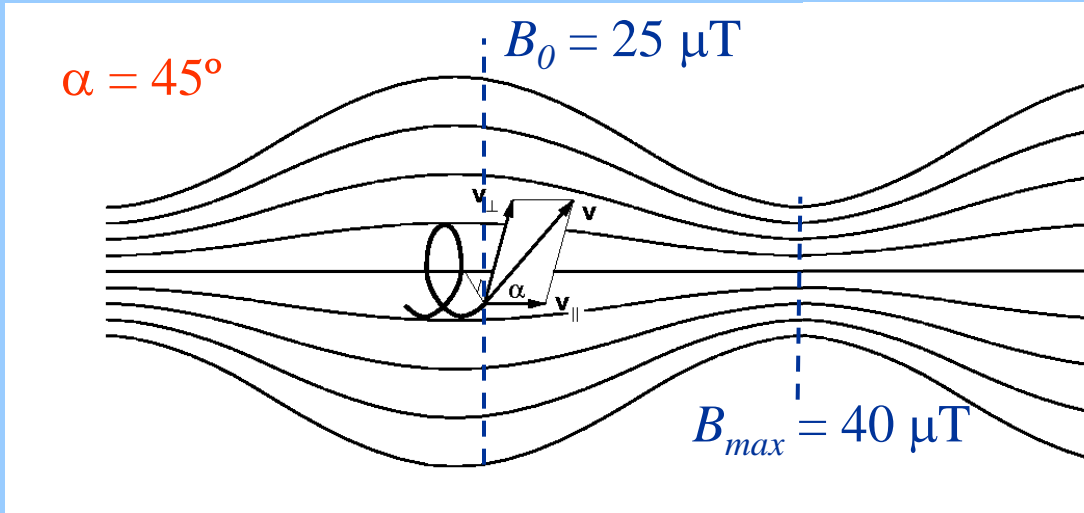


Yellow

It will escape



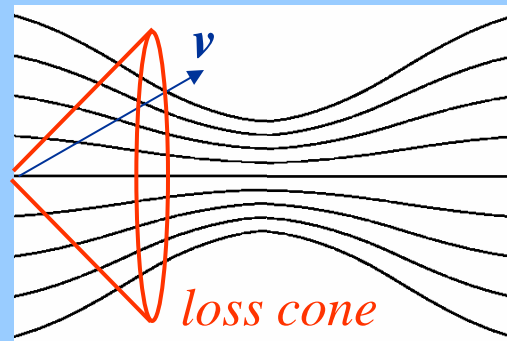
# What will happen to the particle?



$$\alpha_{lc} = \arcsin \sqrt{B_0 / B_{max}} =$$

$$\arcsin \sqrt{25 / 40} = 52^\circ$$

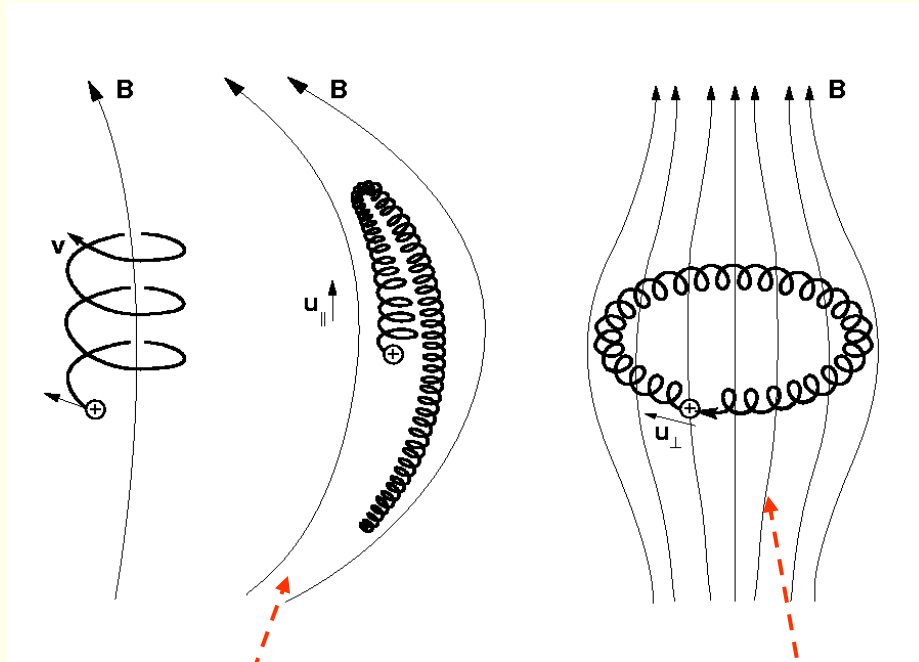
**Yellow** It will escape





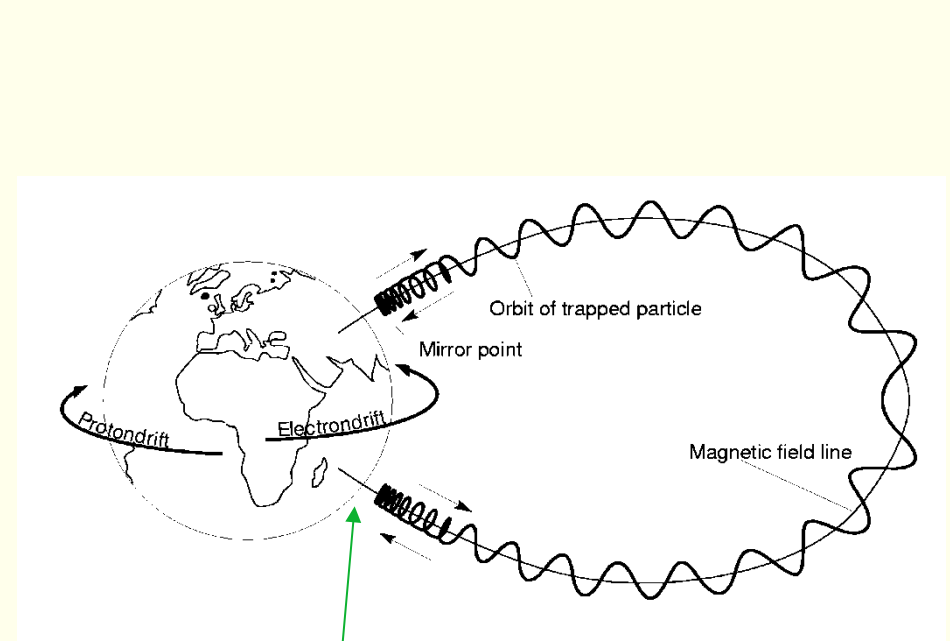
# Particle motion in geomagnetic field

longitudinal gyration      oscillation      azimuthal drift



Magnetic mirror

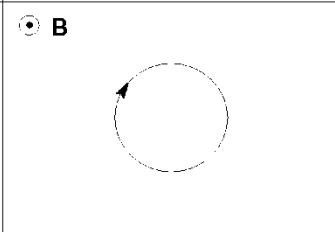
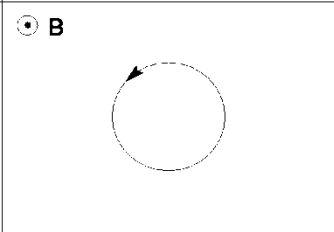
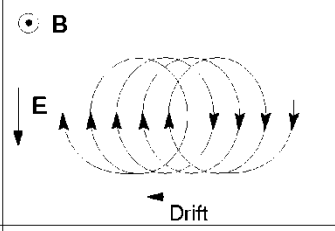
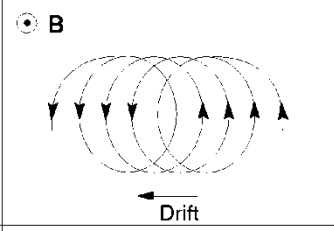
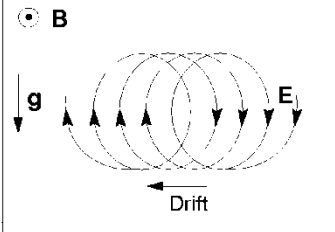
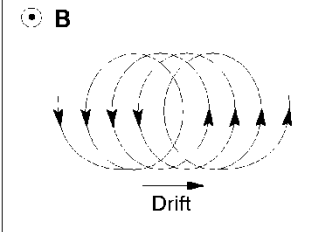
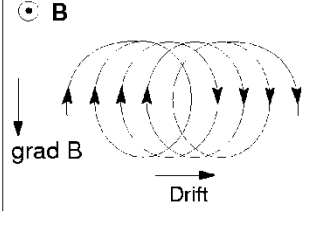
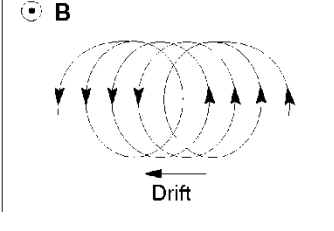
grad B drift



Particles in the loss cone create the aurora!

# Drift motion

$$\mathbf{u} = \frac{\mathbf{F} \times \mathbf{B}}{qB^2}$$

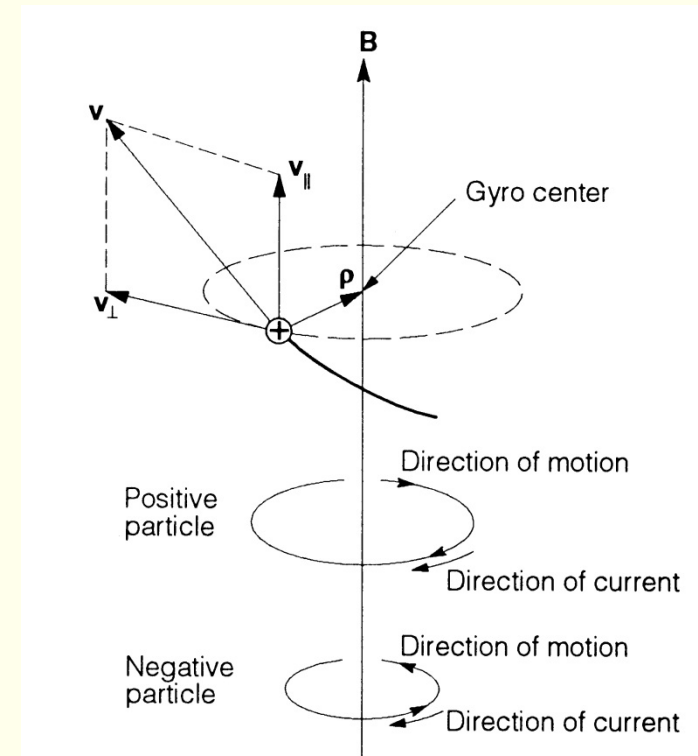
	Positive particles	Negative particles
Homogeneous magnetic field No disturbing force $\mathbf{F} = 0$		
Homogeneous magnetic field Homogeneous electric field $\mathbf{F} = q\mathbf{E}$		
Homogeneous magnetic field Gravitation $\mathbf{F} = m\mathbf{g}$		
Inhomogeneous magnetic field $\mathbf{F} = -\mu \text{ grad } B$		

# Force on magnetic dipole

$$\mu \sim -\mathbf{B} \Rightarrow \boldsymbol{\mu} = -\mu \frac{\mathbf{B}}{B}$$

$$\mathbf{F} = \nabla (\boldsymbol{\mu} \cdot \mathbf{B}) = -\mu \nabla \left( \frac{\mathbf{B}}{B} \cdot \mathbf{B} \right) =$$

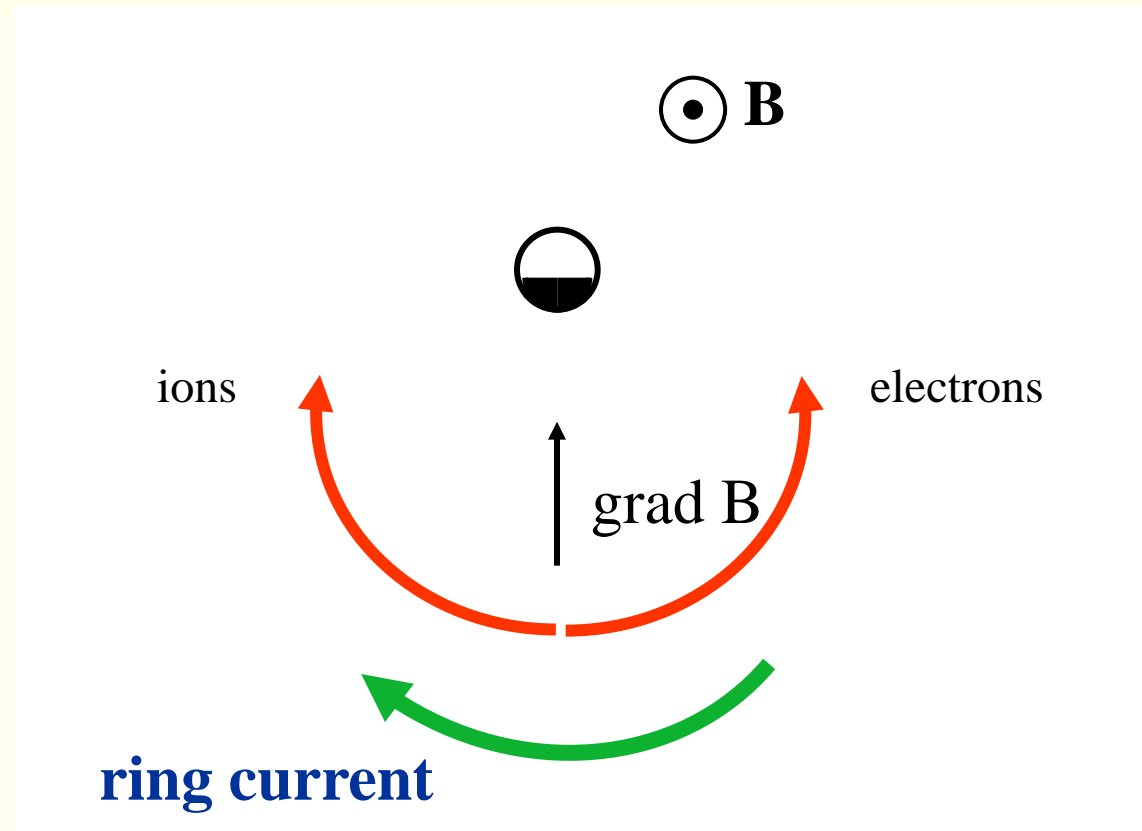
$$= -\mu \nabla \left( \frac{B^2}{B} \right) = -\mu \nabla B$$



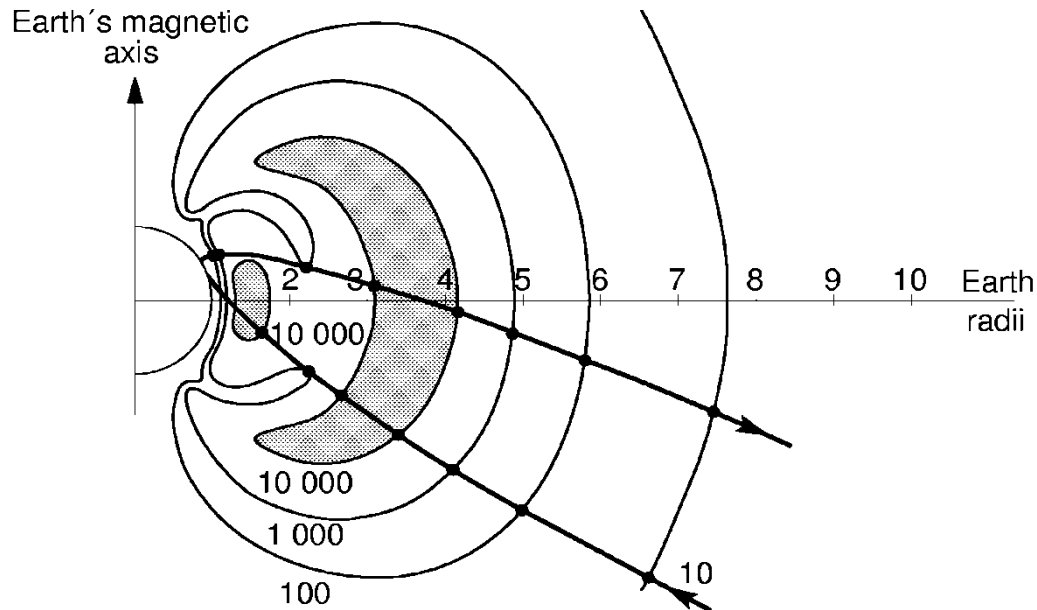
# Ring current and particle motion

$$\mathbf{u} = -\frac{\mu \nabla B \times \mathbf{B}}{qB^2}$$

$$\mu = \frac{mv_{\perp}^2}{2B}$$



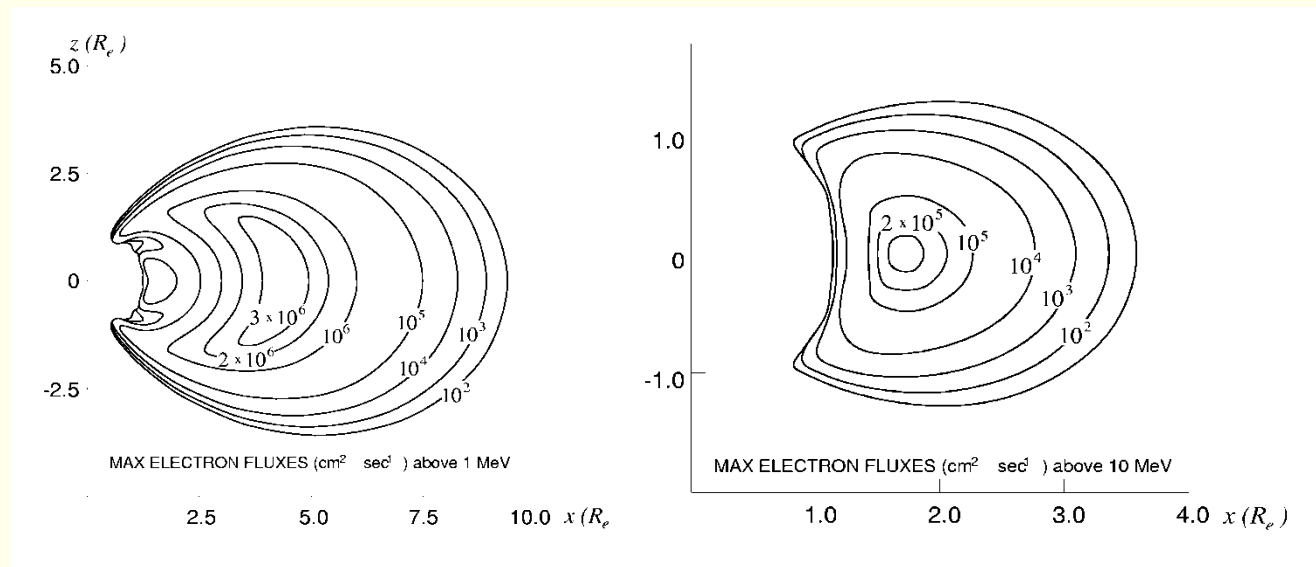
# Radiation belts



## I. Van Allen belts

- Discovered in the 50s , Explorer 1
- Inner belt contains protons with energies of  $\sim 30$  MeV
- Outer belt (Explorer IV, Pioneer III): electrons,  $W > 1.5$  MeV

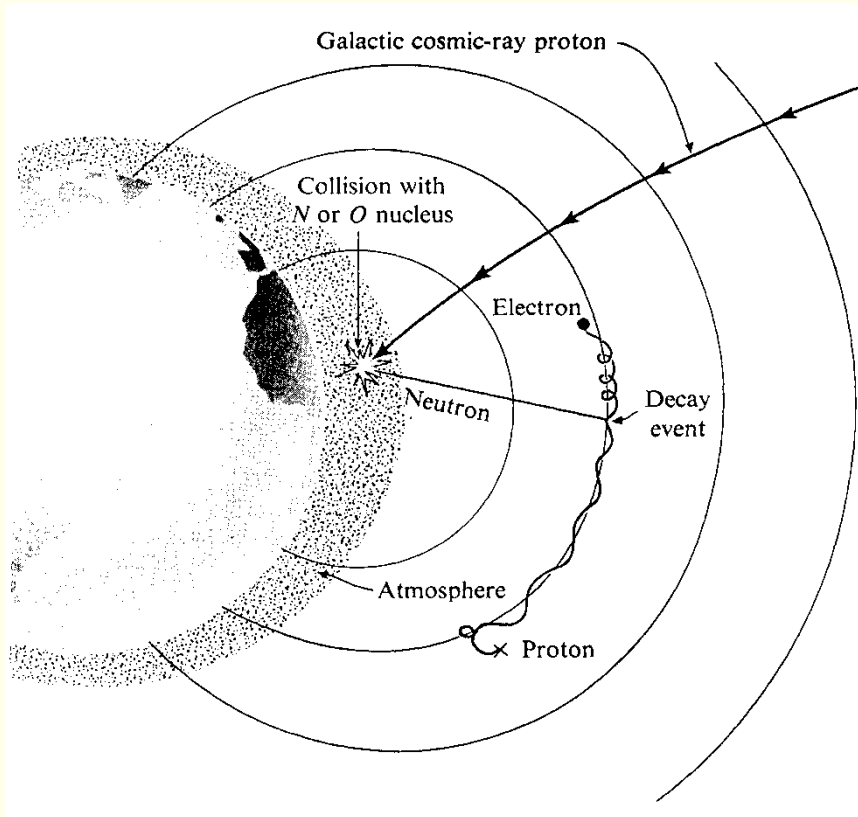
# Radiation belts



- At lower energies there is a more or less continuous population of energetic particles in the inner magnetosphere. (Inner part of *plasma sheet*)

- source: **CRAND** (Cosmic Ray Albedo Neutron Decay).
- a danger for satellites and astronauts.
- associated with a current (*ring current*) which distorts the inner part of the geomagnetic field.

# CRAND (Cosmic Ray Albedo Neutron Decay)

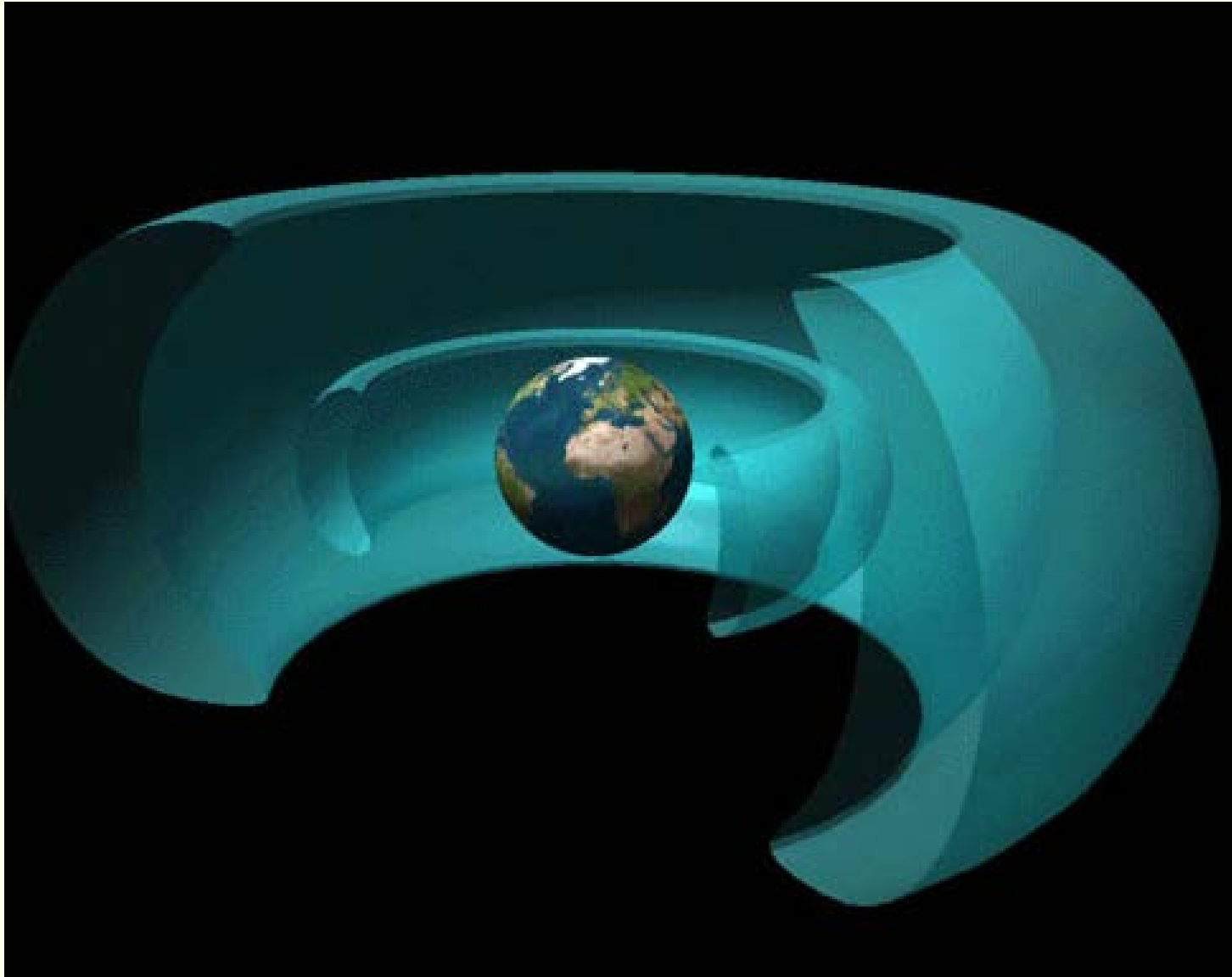


Collisions between cosmic ray particles and the Earth create new particles. Among these are neutrons, that are not affected by the magnetic field. They decay, soon after they happen to be in the radiation belts. The resulting protons and electrons are trapped in the radiation belts.

This contribution to the radiation belts are called the ***neutron albedo***.

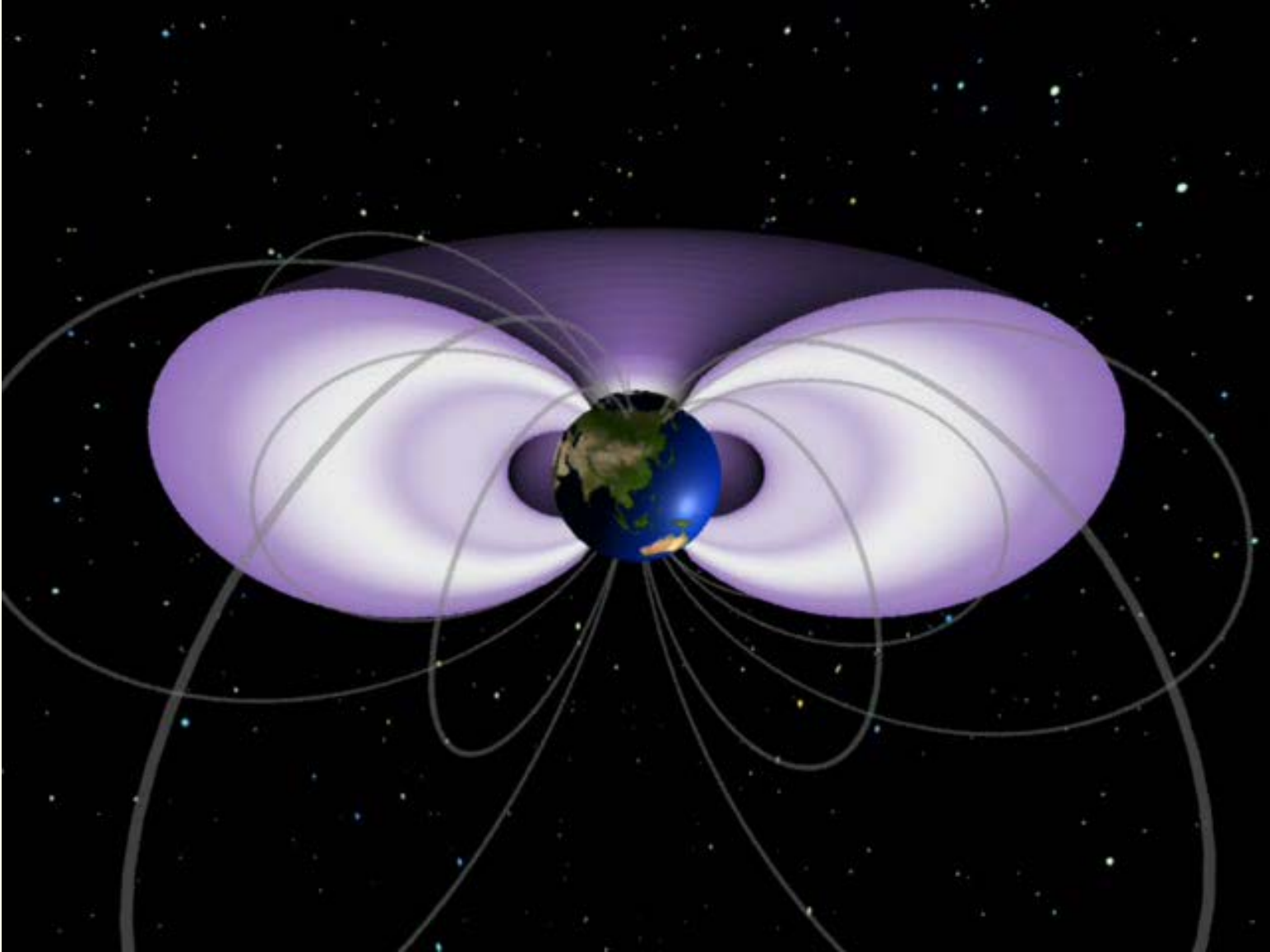
Figure 8. An illustration of the CRAND process for populating the inner radiation belts [Hess, 1968].

# Radiation belts





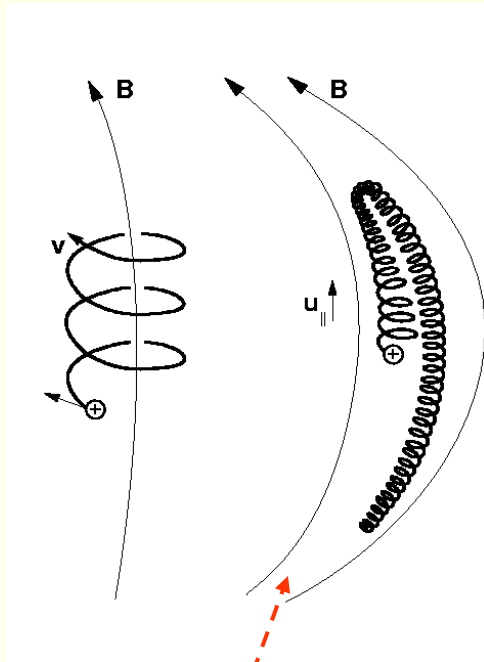
# Radiation belts



# Particle motion in geomagnetic field

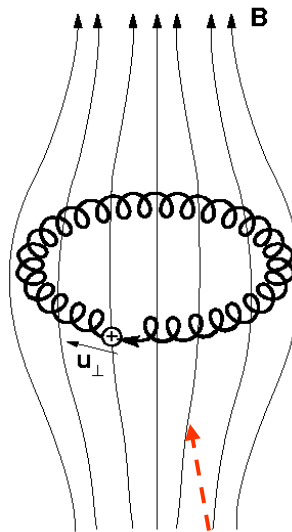
longitudinal oscillation

gyration

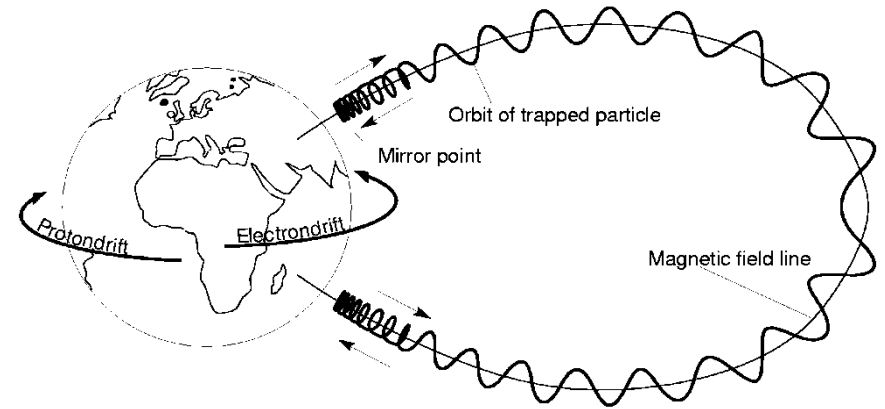


Magnetic mirror

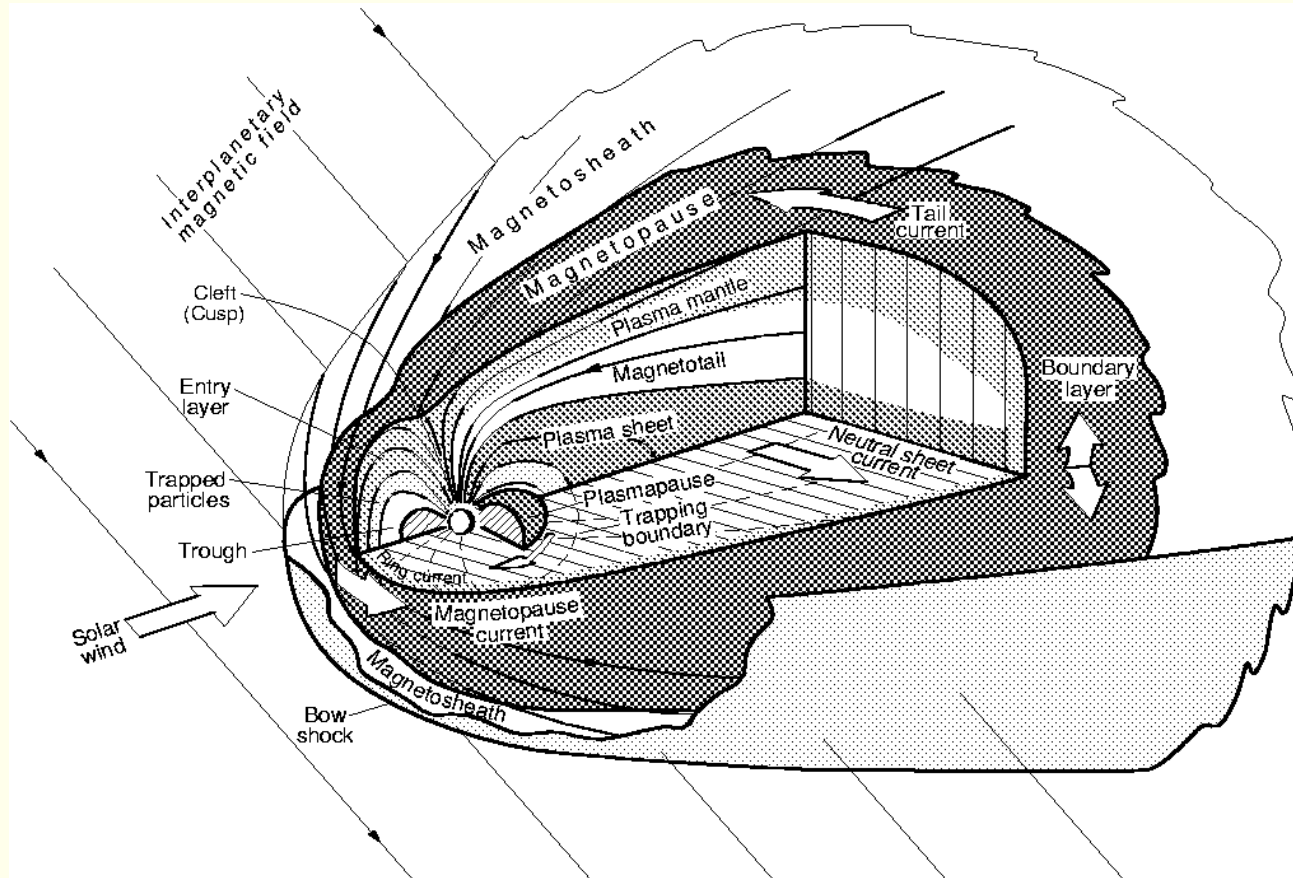
azimuthal drift



grad B drift



# Structure of magnetosphere

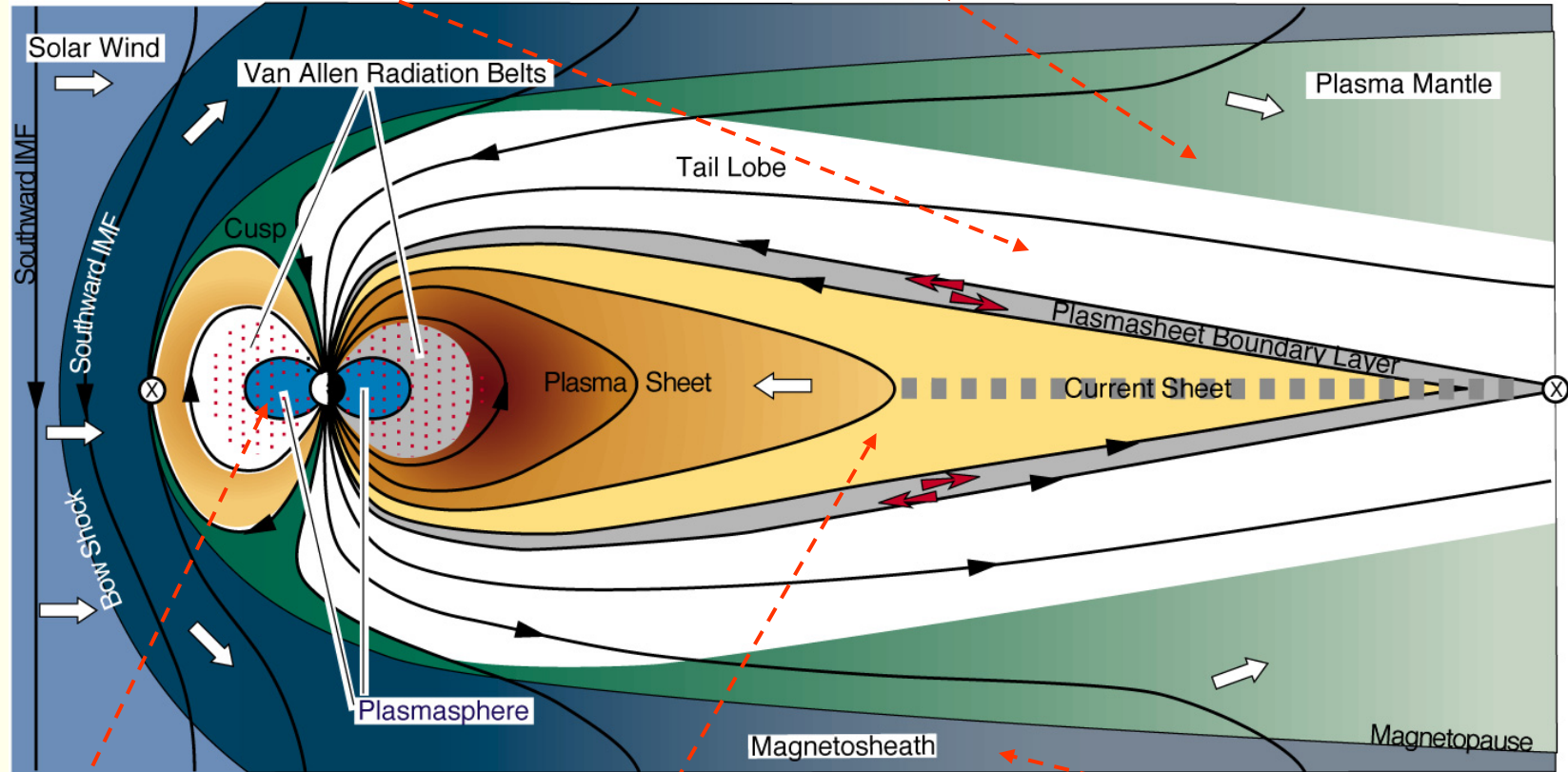


- The plasma in the is made up of approximately equal parts of  $H^+$  and  $O^+$ .
- Plasma populations organized by geomagnetic field.
- Particles will mirror between northern and southern hemispheres on closed field lines

# Magnetospheric structure

polar plumes = tail lobe  
 $n_e \sim 0,01 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

plasma mantle  
 $n_e \sim 0,1-1 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

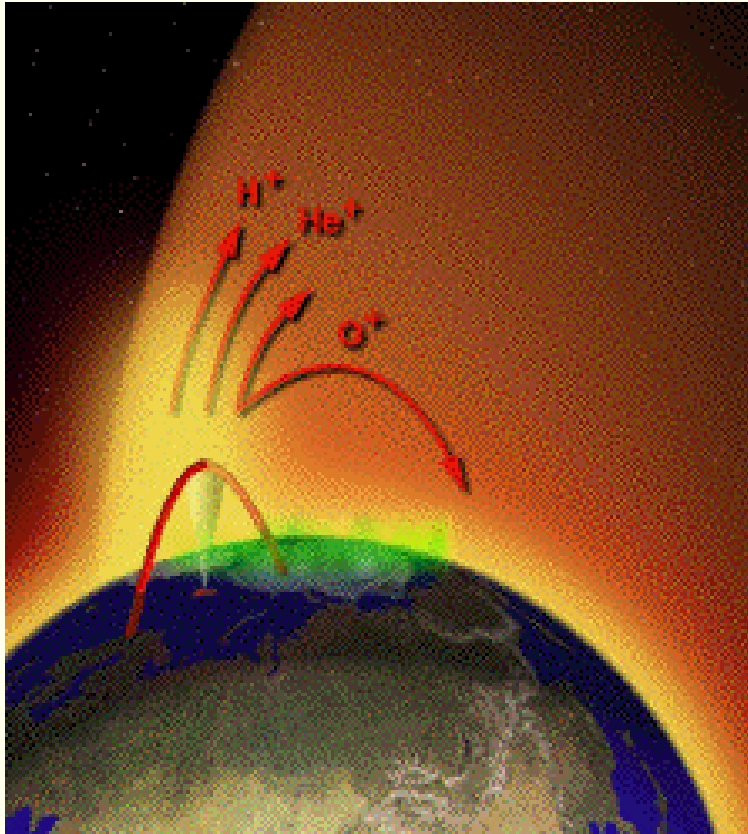


plasmasphere:  
 $n_e \sim 10-100 \text{ cm}^{-3}$ ,  $T_e \sim 1000 \text{ K}$

plasma sheet:  
 $n_e \sim 1 \text{ cm}^{-3}$ ,  $T_e \sim 10^7 \text{ K}$

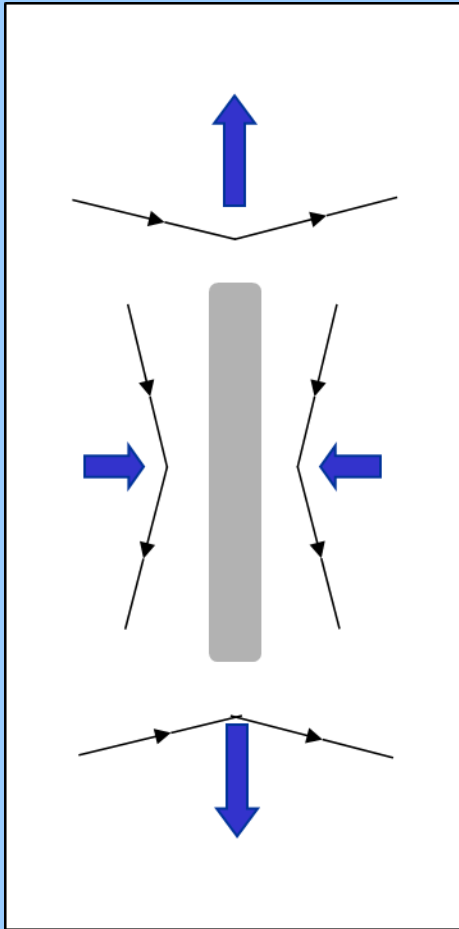
magnetosheath:  
 $n_e \sim 5 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

# Outflow from the ionosphere

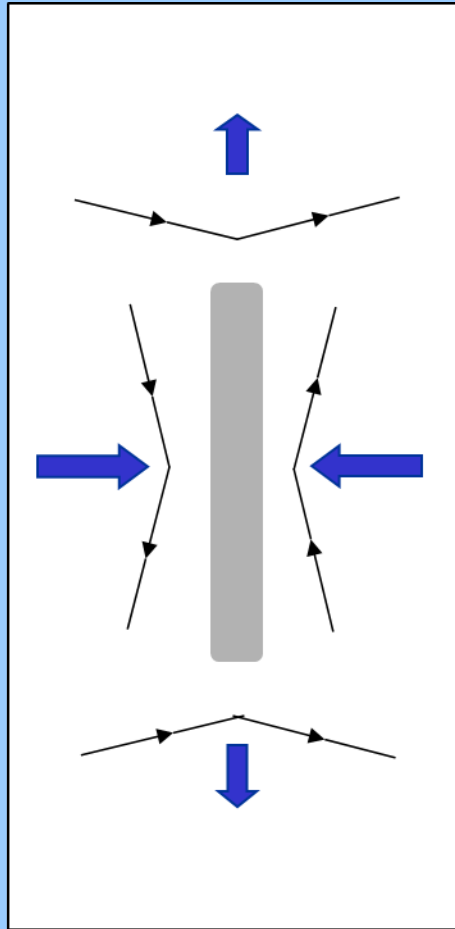


An important source for the magnetospheric plasma.  
Research is ongoing.

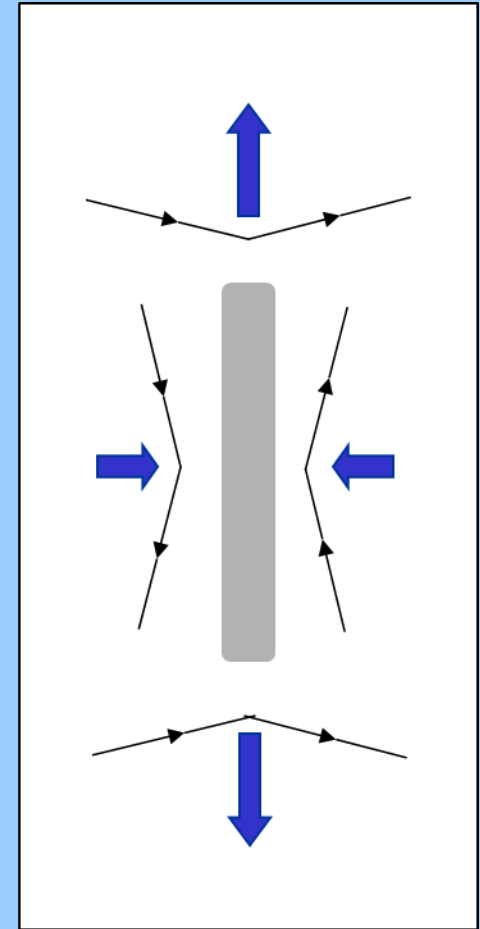
# Magnetic reconnection



Green

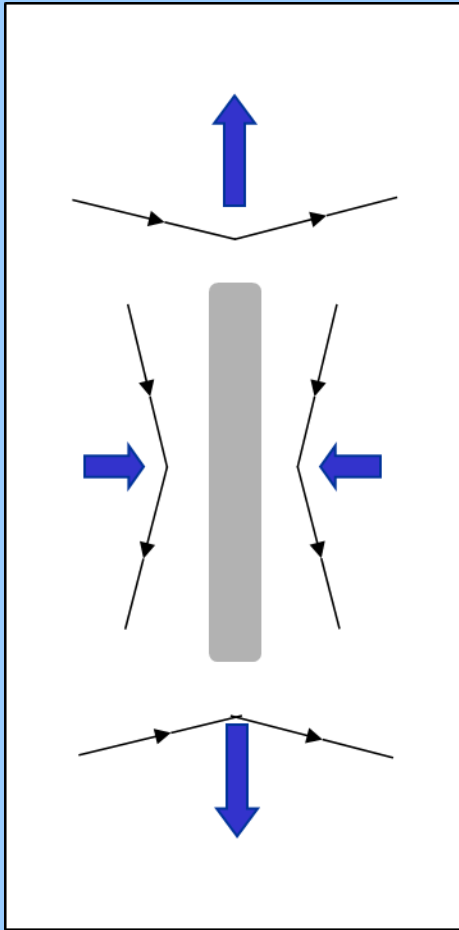


Yellow

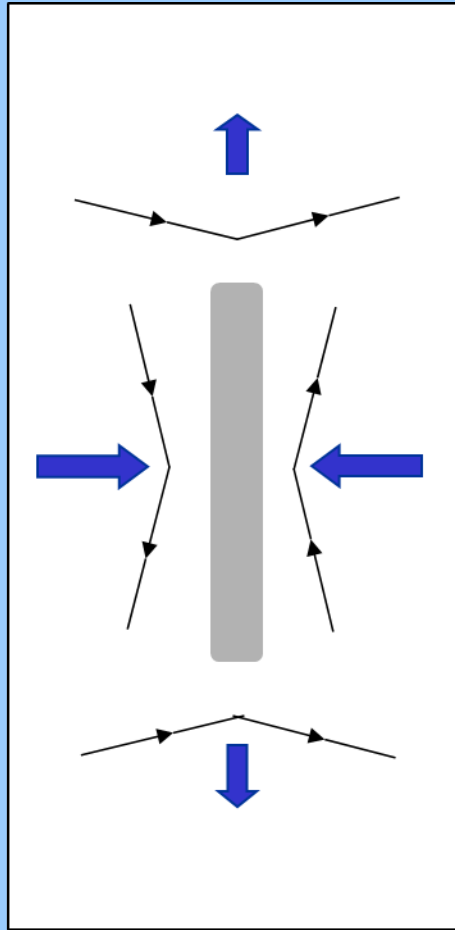


Red

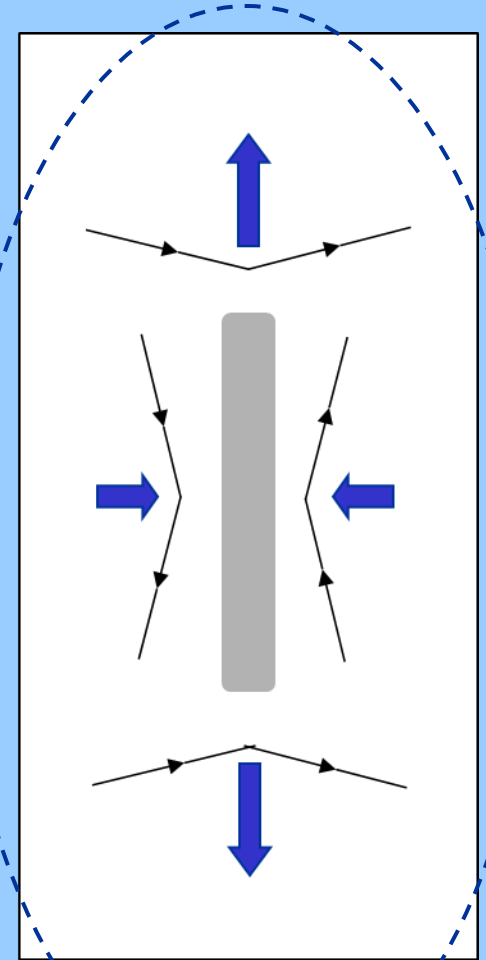
# Magnetic reconnection



Green

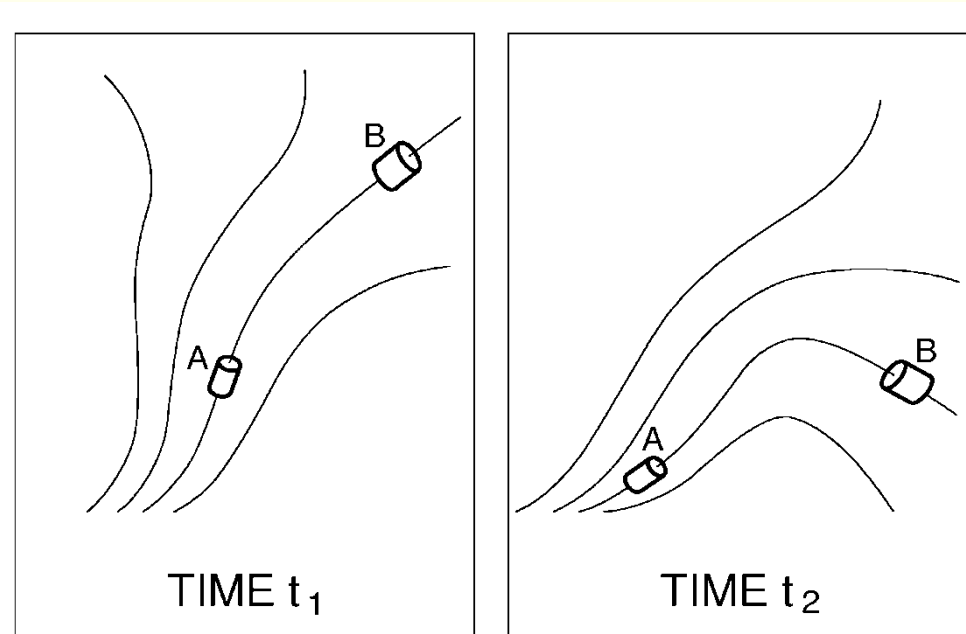


Yellow



Red

# Frozen in magnetic field lines



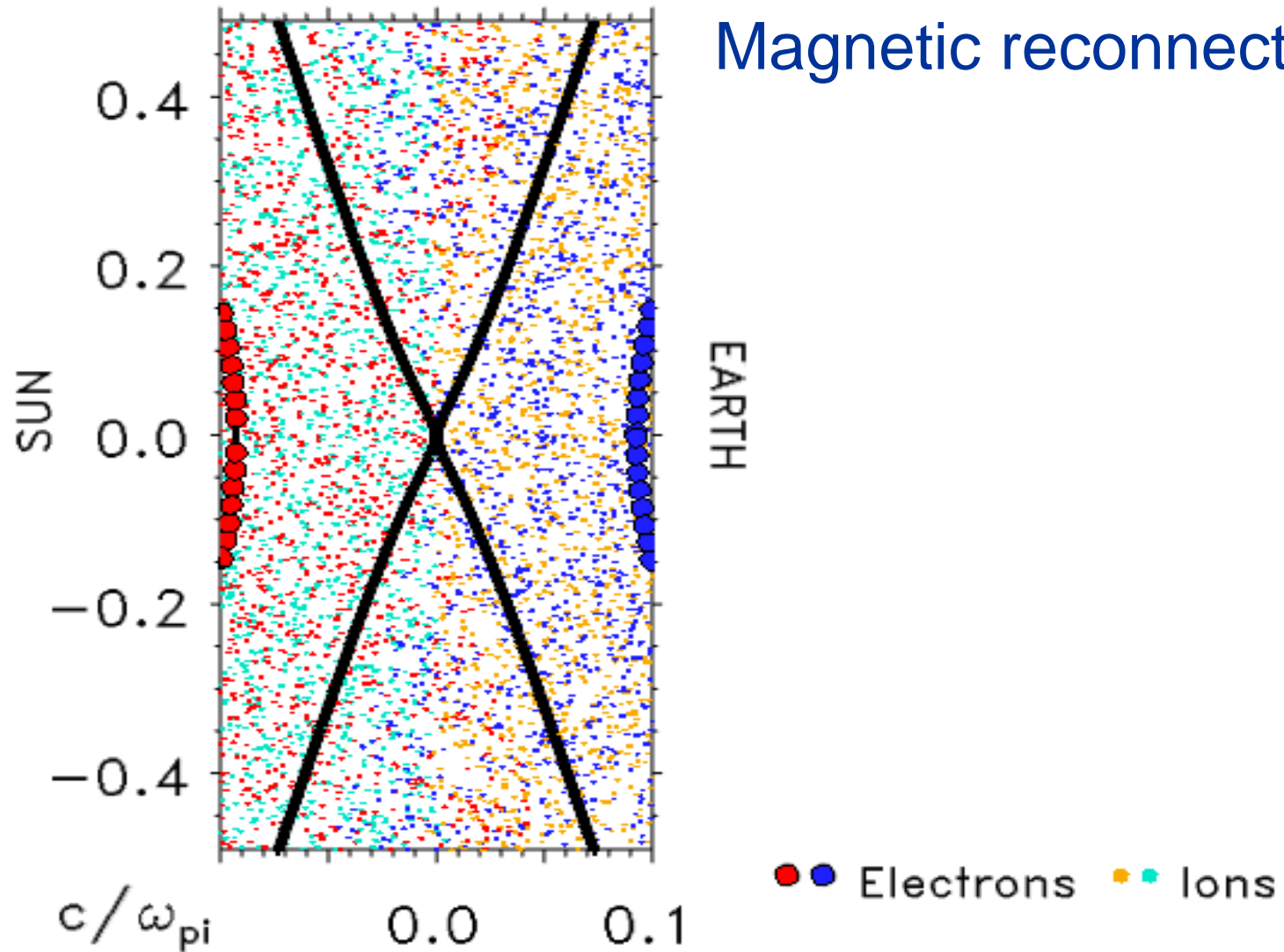
In fluid description of plasma two plasma elements that are connected by a common magnetic field line at time  $t_1$  will be so at any other time  $t_2$ .

This applies if the magnetic Reynolds number is large:

$$R_m = \mu_0 \sigma l_c v_c \gg 1$$

*An example of the collective behaviour of plasmas.*





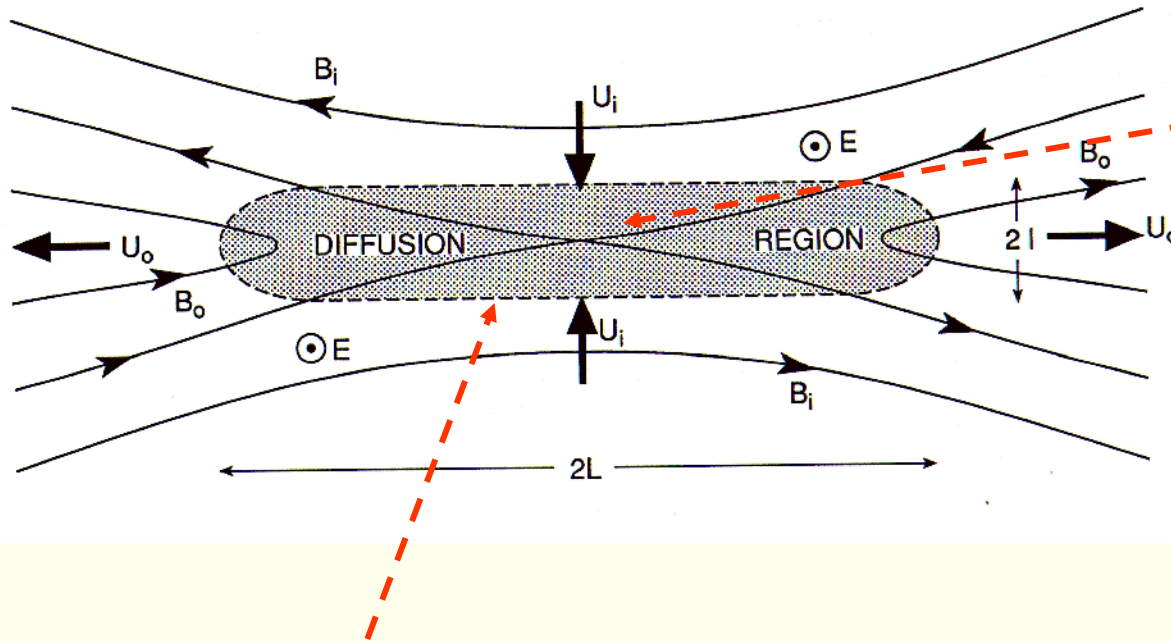
# Reconnection

In 'diffusion region':

$$R_m = \mu_0 \sigma l v \sim 1$$

Thus: **condition** for frozen-in magnetic field breaks down.

A second **condition** is that there are two regions of magnetic field pointing in *opposite* direction:

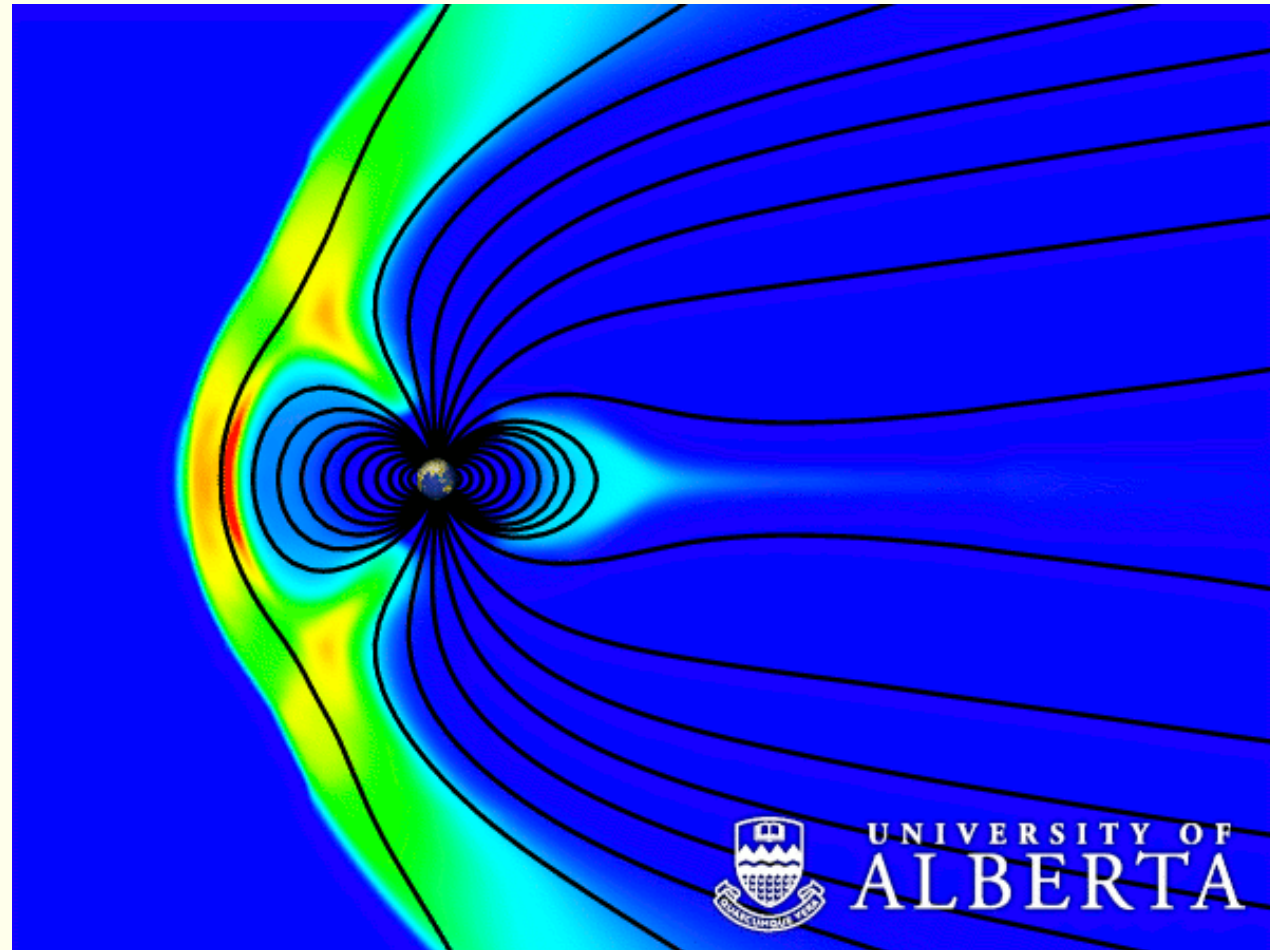


- Field lines are “cut” and can be re-connected to other field lines
- **Magnetic energy is transformed into kinetic energy ( $U_o \gg U_i$ )**
- **Plasma from different field lines can mix**

# Reconnection and plasma convection

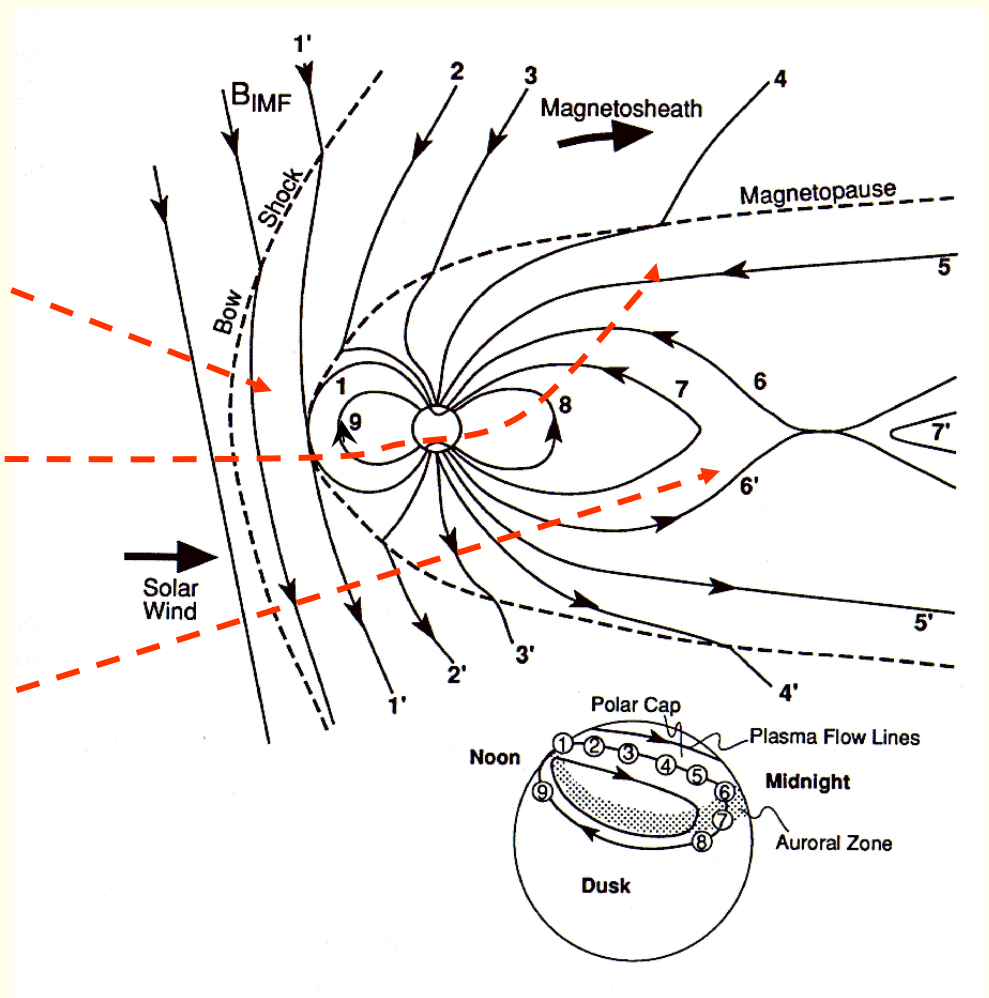


Solar wind

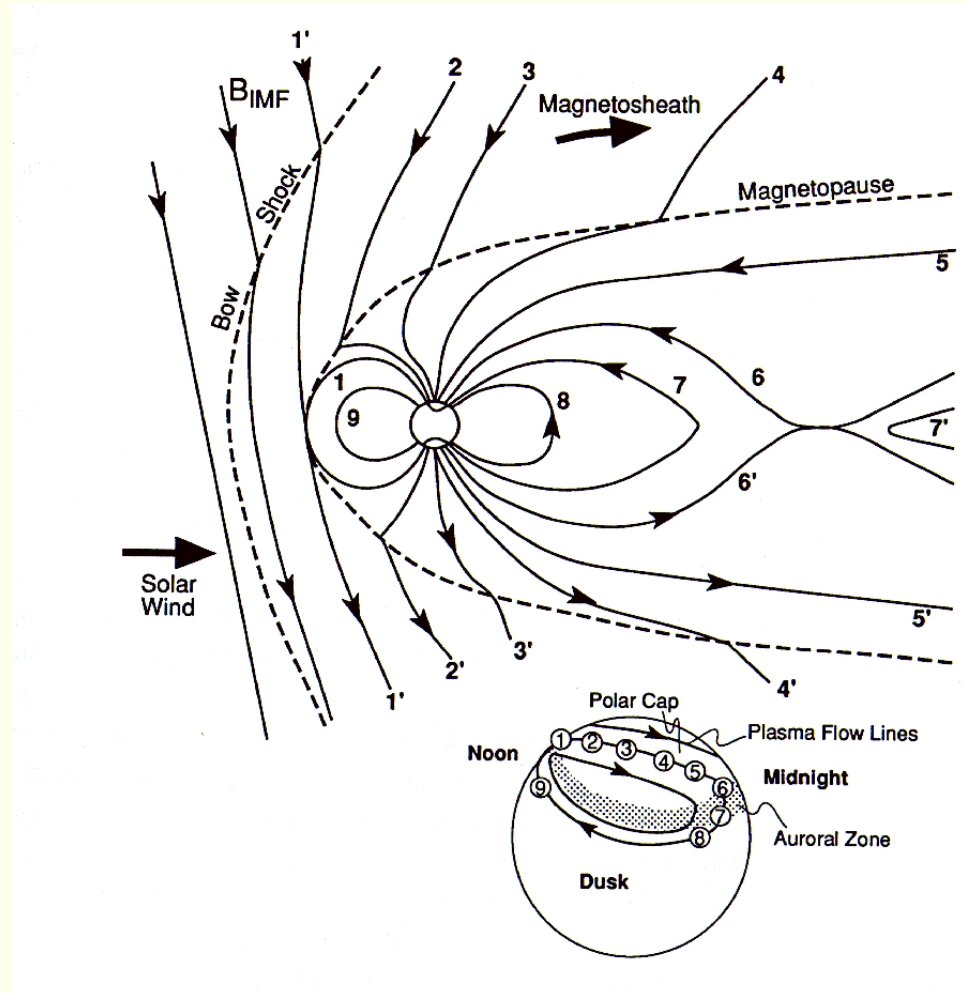


# Reconnection och plasma convection

- Reconnection on the dayside “re-connects” the solar wind magnetic field and the geomagnetic field
- In this way the plasma convection in the outer magnetosphere is driven
- In the night side a second reconnection region drives the convection in the inner magnetosphere. The reconnection also heats the plasmashet plasma.

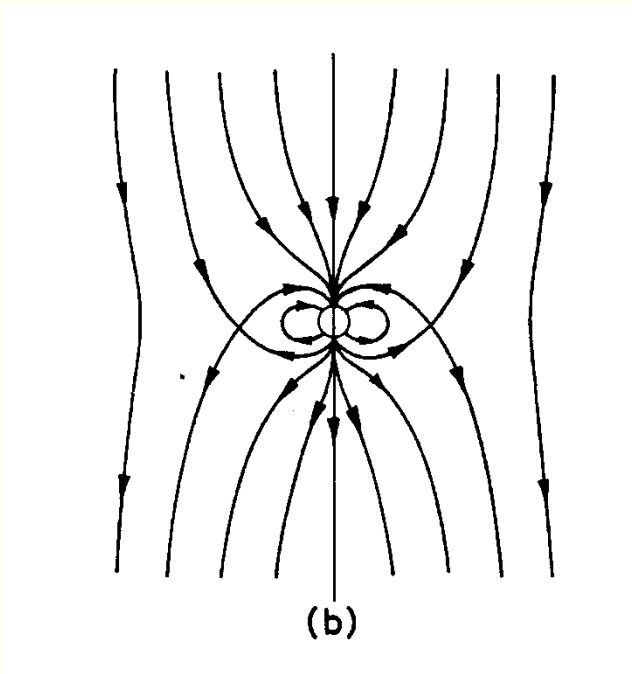


# What happens if IMF is northward instead?

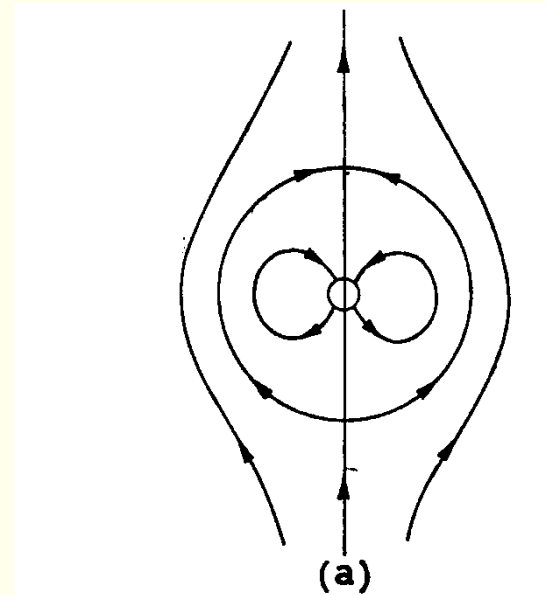


# Magnetospheric dynamics

*open magnetosphere*



*closed magnetosphere*



**southward**  


**Interplanetary  
magnetic field (IMF)**

 **northward**



# What do the magnetospheres of the other planets look like?



# Last Minute!





# Last Minute!

- What was the most important thing of today's lecture? Why?
- What was the most unclear or difficult thing of today's lecture, and why?
- Other comments