



# Last lecture (6)

- Drift motion
- Ionospheric conductivities
- Particle motion in the magnetosphere

# Today's lecture (7)

- Other magnetospheres
- Aurora
- Current measurements in space



# Today

Activity	Date	Time	Room	Subject	Litterature
L1	31/8	13-15	V22	Course description, Introduction, The Sun 1, Plasma physics 1	CGF Ch 1, 5, (p 110-113)
L2	3/9	15-17	Q36	The Sun 2, Plasma physics 2	CGF Ch 5 (p 114-121), 6.3
L3	7/9	13-15	Q36	Solar wind, The ionosphere and atmosphere 1, Plasma physics 3	CGF Ch 6.1, 2.1-2.6, 3.1-3.2, 3.5, LL Ch III, Extra material
T1	10/9	15-17	Q36	Mini-group work 1	
L4	14/9	13-15	E2	The ionosphere 2, Plasma physics 4	CGF Ch 3.4, 3.7, 3.8
T2	17/9	8-10	Q31	Mini-group work 2	
L5	17/9	15-17	L52	The Earth's magnetosphere 1, Plasma physics 5	CGF 4.1-4.3, LL Ch I, II, IV.A
L6	21/9	13-15	L52	The Earth's magnetosphere 2, <b>Other magnetospheres</b>	CGF Ch 4.6-4.9, LL Ch V.
T3	24/9	16-18	Q36	Mini-group work 3	
L7	28/9	13-15	Q36	<b>Aurora, Measurement methods in space plasmas and data analysis 1</b>	CGF Ch 4.5, 10, LL Ch VI, Extra material
T4	1/10	15-17	V22	Mini-group work 4	
L8	5/10	13-15	M33	Space weather and geomagnetic storms	CGF Ch 4.4, LL Ch IV.B-C, VII.A-C
L9	6/10	8-10	Q36	Interstellar and intergalactic plasma, Cosmic radiation,	CGF Ch 7-9
T5	8/10	15-17	Q34	Mini-group work 5	
L10	12/10	13-15	Q36	Swedish and international space physics research.	
T6	15/10	15-17	Q33	Round-up.	
Written examination	28/10	8-13	Q21, Q26		



# **Sign up for the exam on My Pages (before Oct 14)**

**(Make sure you are registered. If you are not, contact [stex@ee.kth.se](mailto:stex@ee.kth.se))**

# **EF22445 Space Physics II**

## **7.5 ECTS credits, P2**

- shocks and boundaries in space
- solar wind interaction with magnetized and unmagnetized bodies
- reconnection
- sources of magnetospheric plasma
- magnetospheric and ionospheric convection
- auroral physics
- storms and substorms
- global oscillations of the magnetosphere

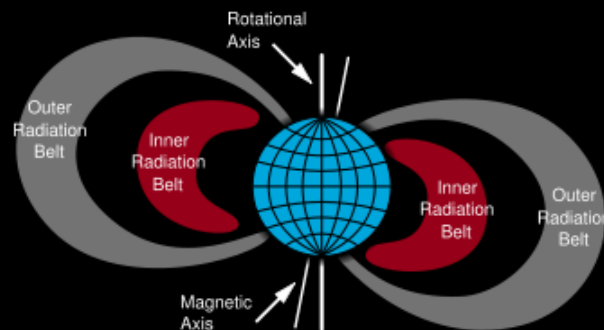
# Courses at the Alfvén Laboratory

## EF2260 SPACE ENVIRONMENT AND SPACECRAFT ENGINEERING , 6 ECTS credits, period 2

- environments spacecraft may encounter in various orbits around the Earth, and the constraints this places on spacecraft design
- basic operation principles underlying the thermal control system and the power systems in spacecraft
- measurements principles in space



*The Astrid-2 satellite*



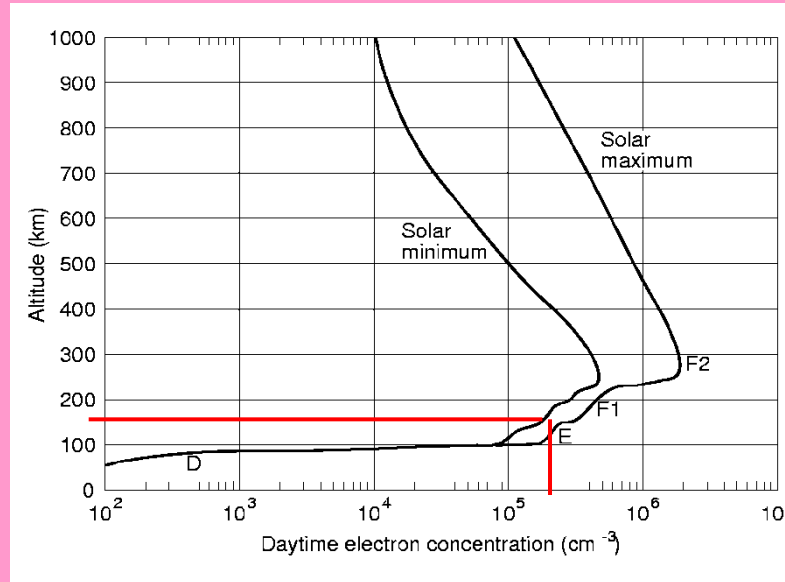
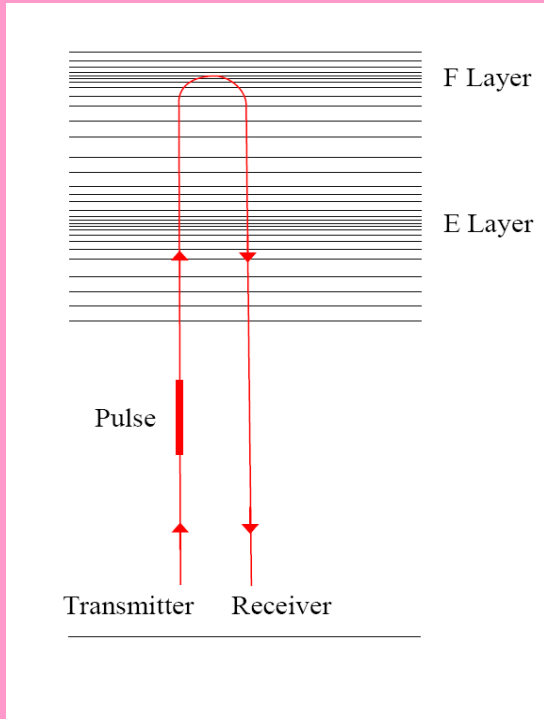
*Radiation environment in near-earth space*

### Projects:

- Design power supply for spacecraft
- Study of radiation effects on electronics

# Mini-groupwork 3

b)



$$f_p = \frac{1}{2\pi} \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} \approx 9\sqrt{n_e}$$

$$f_p = 5 \cdot 10^6 = 9\sqrt{n_e}$$

⇒

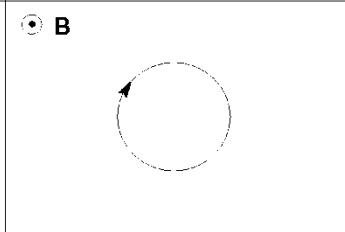
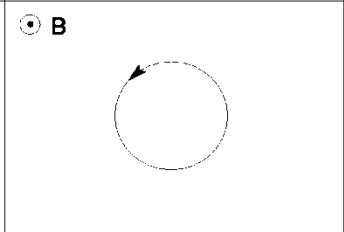
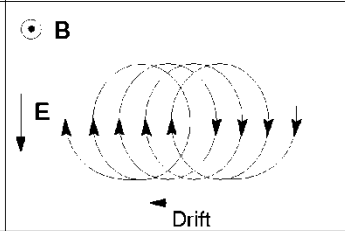
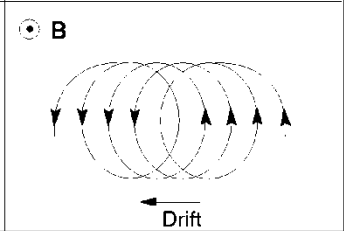
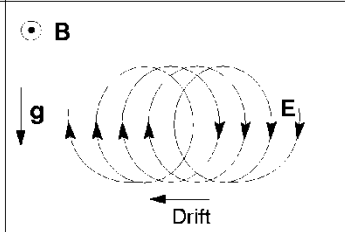
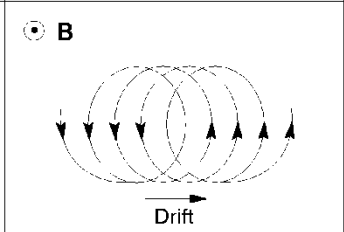
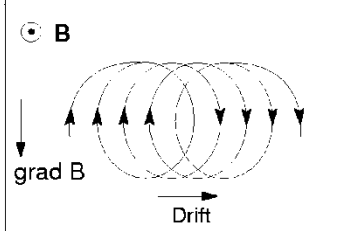
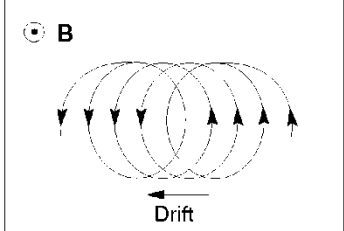
$$n_e = \left( \frac{5 \cdot 10^6}{9} \right)^2 = 3 \cdot 10^{11} \text{ m}^{-3}$$

$$h = 150 \text{ km}$$

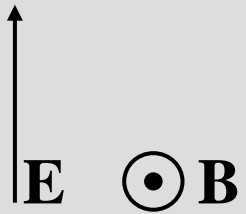
$$t = \frac{2h}{c} = \frac{300 \cdot 10^3}{3 \cdot 10^8} = 10^{-3} \text{ s}$$

# Drift motion

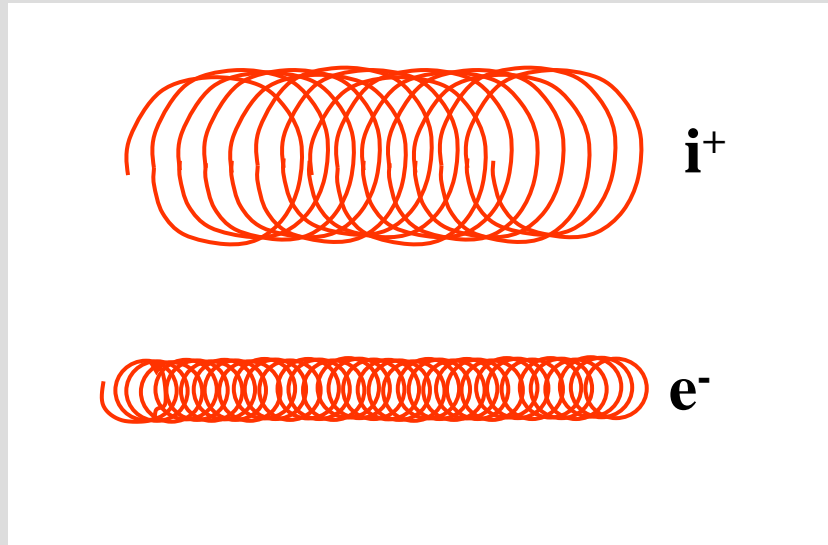
$$\mathbf{u}_{drift} = \frac{\mathbf{F} \times \mathbf{B}}{qB^2}$$

	Positive particles	Negative particles
Homogeneous magnetic field No disturbing force $\mathbf{F} = 0$		
Homogeneous magnetic field Homogeneous electric field $\mathbf{F} = q\mathbf{E}$		
Homogeneous magnetic field Gravitation $\mathbf{F} = m\mathbf{g}$		
Inhomogeneous magnetic field $\mathbf{F} = -\mu \text{grad } B$		

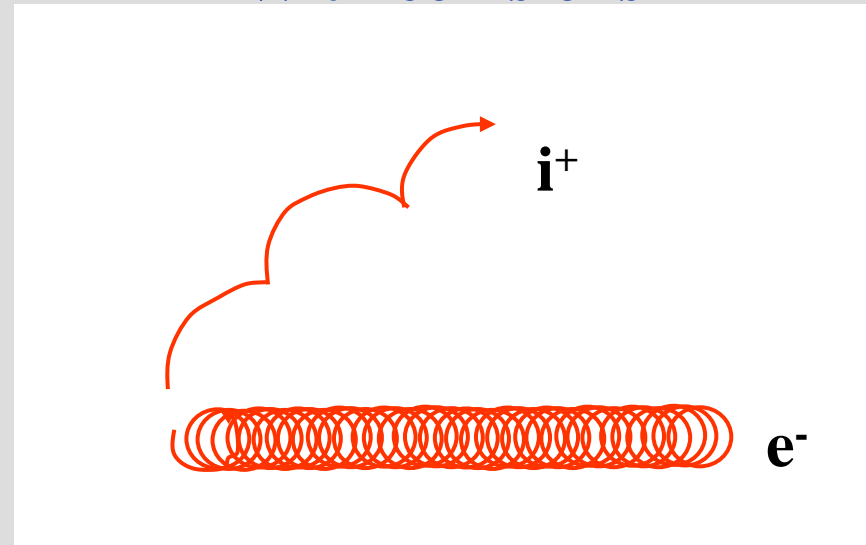
# ExB-drift



Without collisions

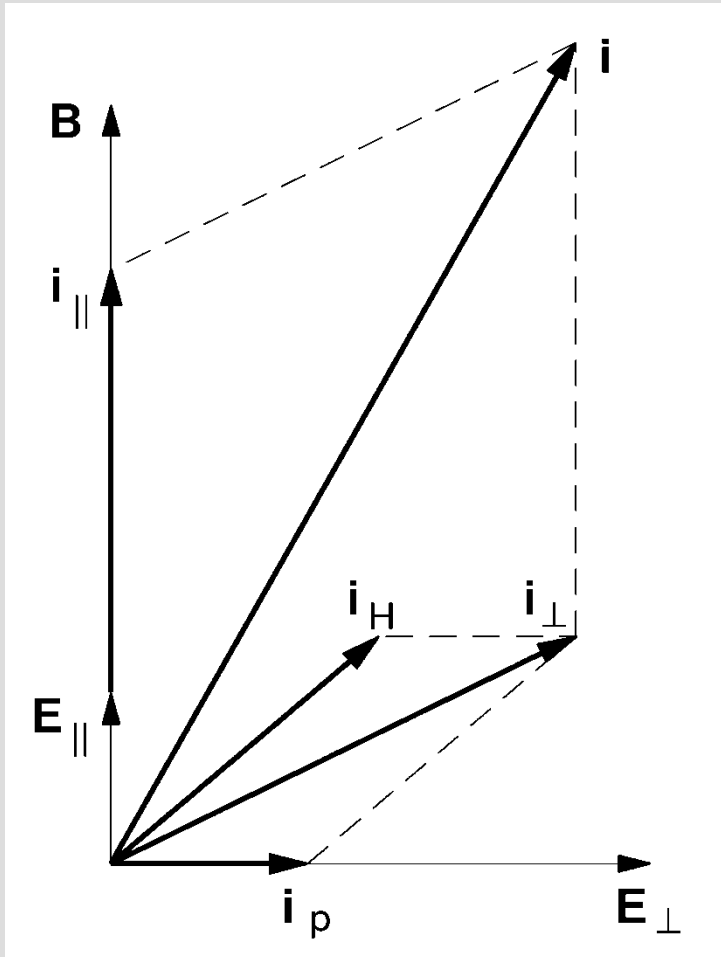


With collisions



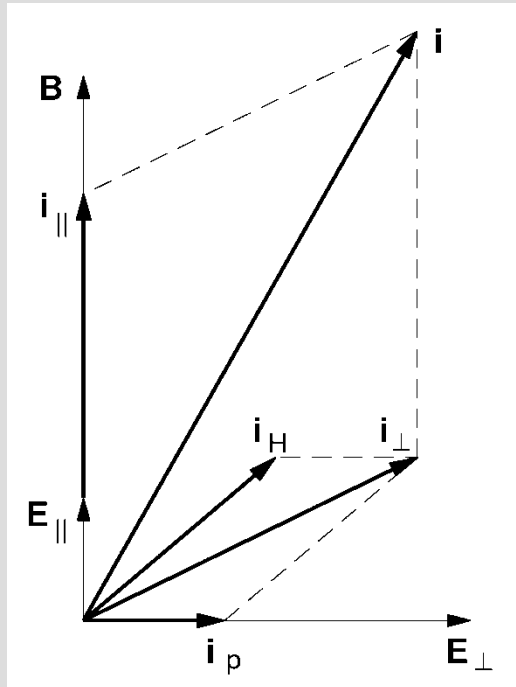


# Electric conductivity in a magnetized plasma



- $i_{||}$  = parallel current
- $i_p$  = Pedersen current
- $i_H$  = Hall current

# Electric conductivity in a magnetized plasma II



$$\sigma_P = \sigma_e \frac{1}{1 + \omega_{ge}^2 \tau_e^2} + \sigma_i \frac{1}{1 + \omega_{gi}^2 \tau_i^2}$$

$$\sigma_H = \sigma_e \frac{\omega_{ge} \tau_e}{1 + \omega_{ge}^2 \tau_e^2} - \sigma_i \frac{\omega_{gi} \tau_i}{1 + \omega_{gi}^2 \tau_i^2}$$

$$\sigma_{||} = \sigma_e + \sigma_i$$

$$\sigma_e = e^2 n \tau_e / m_e$$

$$\sigma_i = e^2 n \tau_i / m_i$$

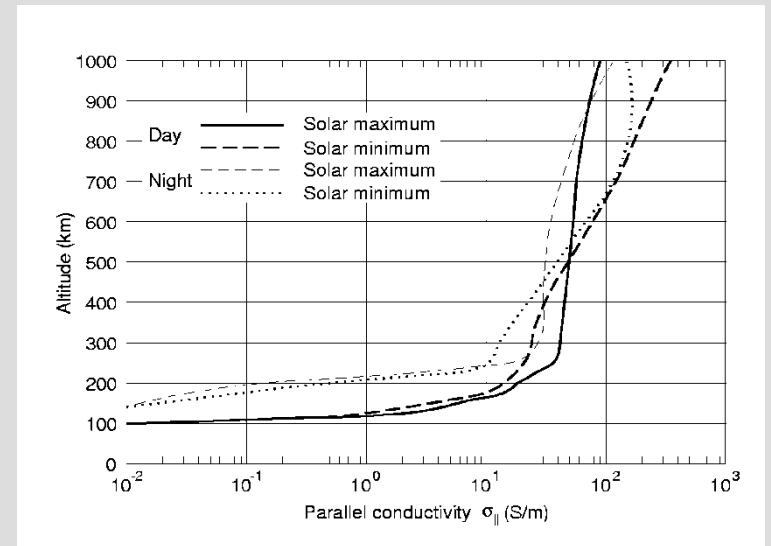
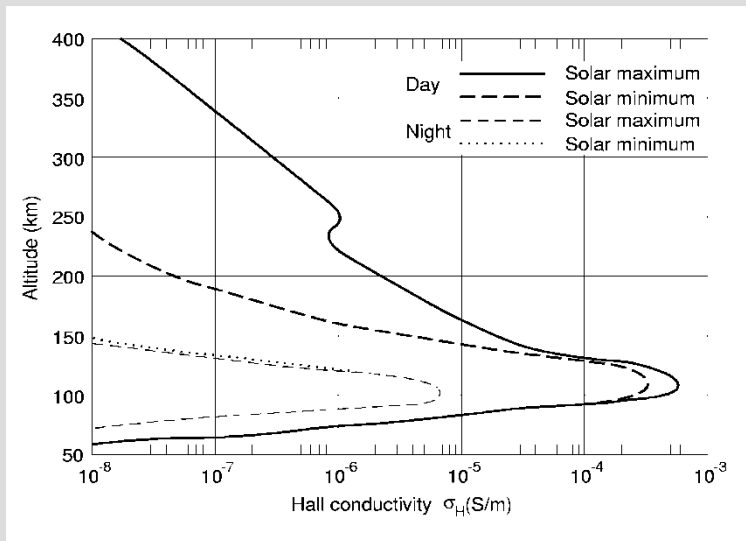
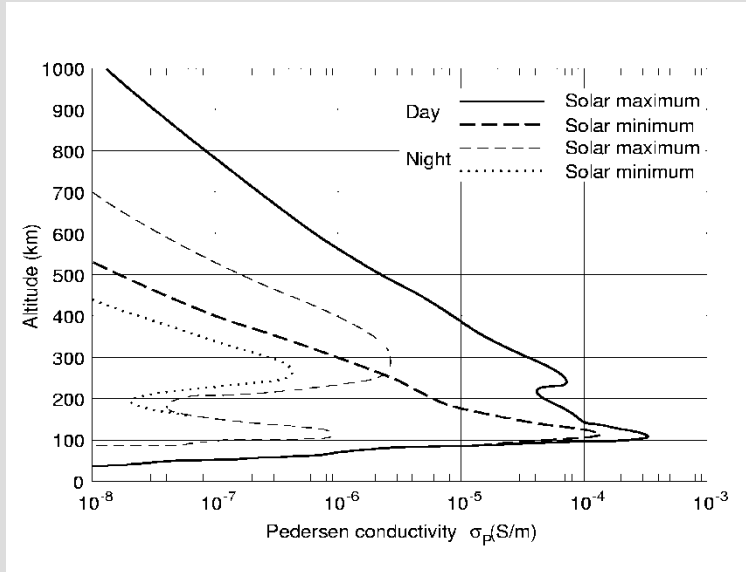
$$i_{||} = \sigma_{||} E_{||}$$

$$i_P = \sigma_P E_{\perp}$$

$$i_H = \sigma_H E_{\perp}$$

$$\left. \begin{array}{l} i_P = \sigma_P E_{\perp} \\ i_H = \sigma_H E_{\perp} \end{array} \right\} \text{ or } \mathbf{i}_{\perp} = \sigma_P \mathbf{E}_{\perp} + \sigma_H \frac{\mathbf{B} \times \mathbf{E}_{\perp}}{B}$$

# Ionospheric conductivities



# Geomagnetic field

Approximated by a dipole close to Earth.

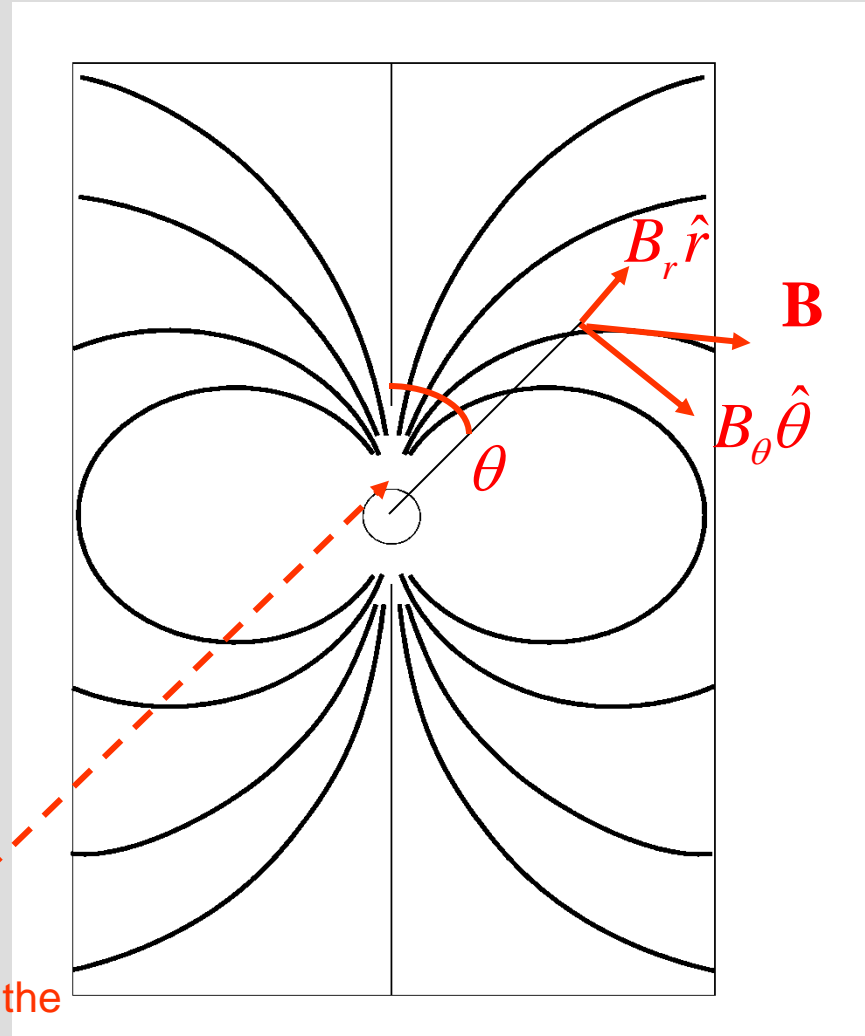
$$B_r = B_p \left(\frac{R_E}{r}\right)^3 \cos \theta$$

$$B_\theta = \frac{B_p}{2} \left(\frac{R_E}{r}\right)^3 \sin \theta$$

$$a = \frac{2\pi R_E^3 B_p}{\mu_0}$$

magnetic dipole moment

Magnetic field at the "north pole"



# Geomagnetic field

Alternative formulation of dipole field

$$B_r = B_p \left(\frac{R_E}{r}\right)^3 \cos \theta$$

$$B_\theta = \frac{B_p}{2} \left(\frac{R_E}{r}\right)^3 \sin \theta$$

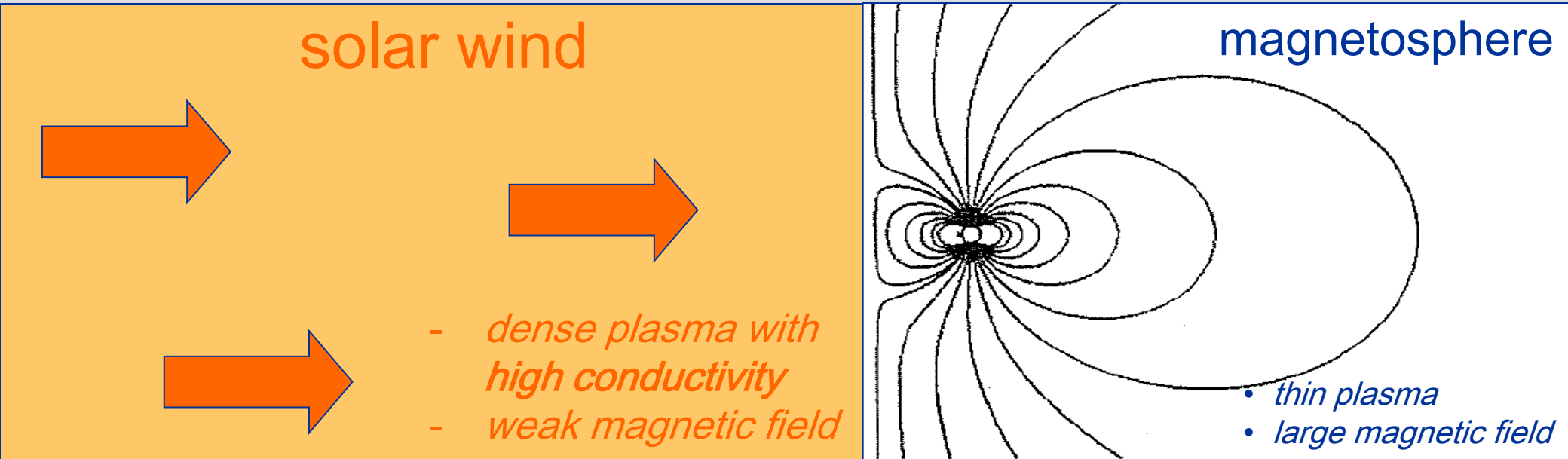
$$B_r = \frac{\mu_0 a}{2\pi} \frac{1}{r^3} \cos \theta$$

$$B_\theta = \frac{\mu_0 a}{2\pi} \cdot \frac{1}{2} \cdot \frac{1}{r^3} \sin \theta$$

$$a = \frac{2\pi R_E^3 B_p}{\mu_0}$$

 magnetic dipole moment

# Stand-off distance from pressure balance



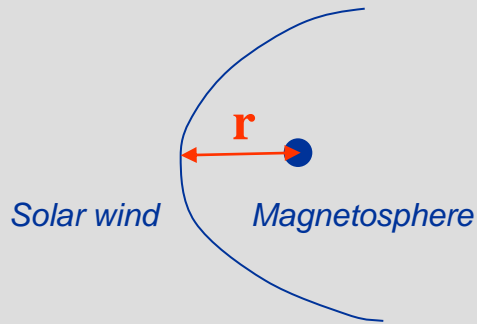
Dynamic pressure:

$$p_d = \rho_{SW} v_{SW}^2$$

Magnetic pressure:

$$p_B = \frac{B^2}{2\mu_0}$$

# Magnetopause “stand-off distance”



Dynamic pressure:  $p_d = \rho_{SW} v_{SW}^2$

Magnetic pressure:  $p_B = \frac{1}{2\mu_0} B^2$

Dipole field strength  
(in equatorial plane):  $B = \frac{\mu_0 a}{4\pi} \frac{1}{r^3}$

$$p_d = p_B \Rightarrow \rho_{SW} v_{SW}^2 = \left[ \frac{\mu_0 a}{4\pi} \frac{1}{r^3} \right]^2 / 2\mu_0 \Rightarrow$$

$$r = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

$a = 8 \times 10^{22} \text{ Am}^2$ ,  $v = 500 \text{ km/s}$ ,  $\rho_{SW} = 10^7 \times 1.7 \times 10^{-27} \text{ kg/m}^3$ :

$r = 7 R_e$  (1  $R_e = 6378 \text{ km}$ )

# Particle motion in magnetic field

## gyro radius

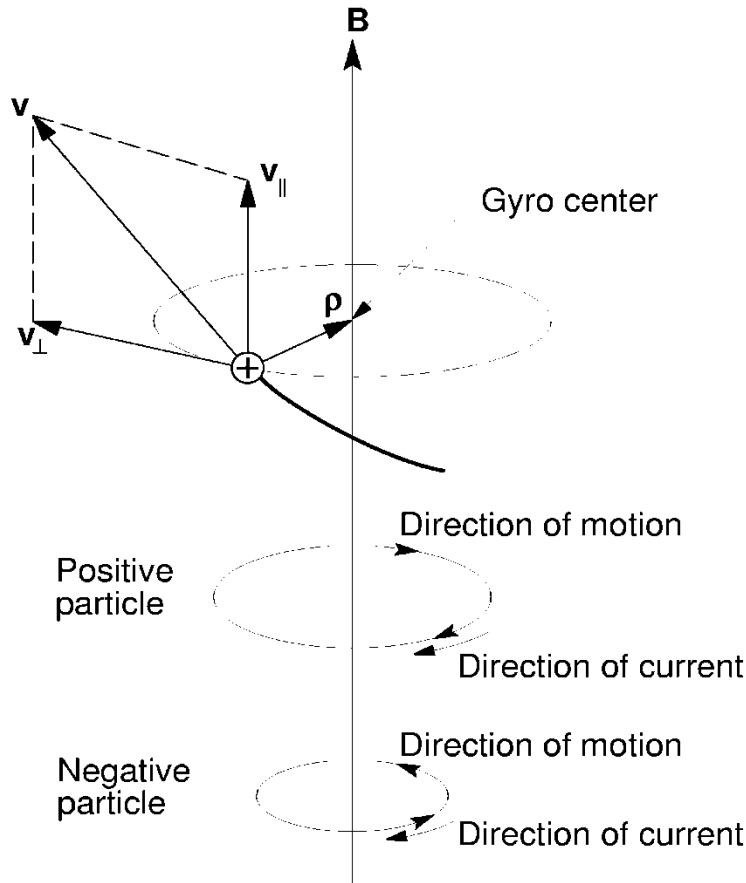
$$\rho = \frac{mv_{\perp}}{qB}$$

## gyro frequency

$$\omega_g = \frac{qB}{m}$$

## magnetic moment

$$\mu = IA = q f_g \pi \rho^2 = mv_{\perp}^2 / 2B$$







# Adiabatic invariant

## DEFINITION:

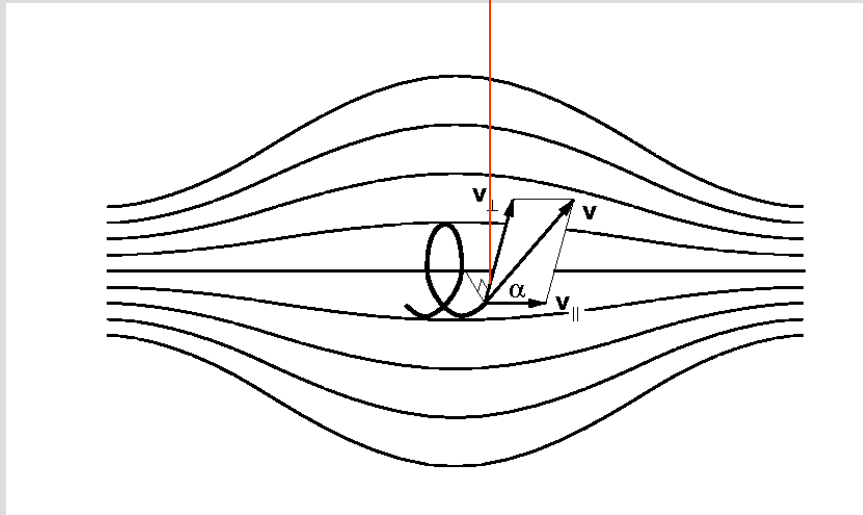
An **adiabatic invariant** is a property of a physical system which stays constant when changes are made slowly.

*By 'slowly' in the context of charged particle motion in magnetic fields, we mean much slower than the gyroperiod.*

'First adiabatic invariant' of particle drift:

$$\mu = \frac{mv_{\perp}^2}{2B}$$

# Magnetic mirror



$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

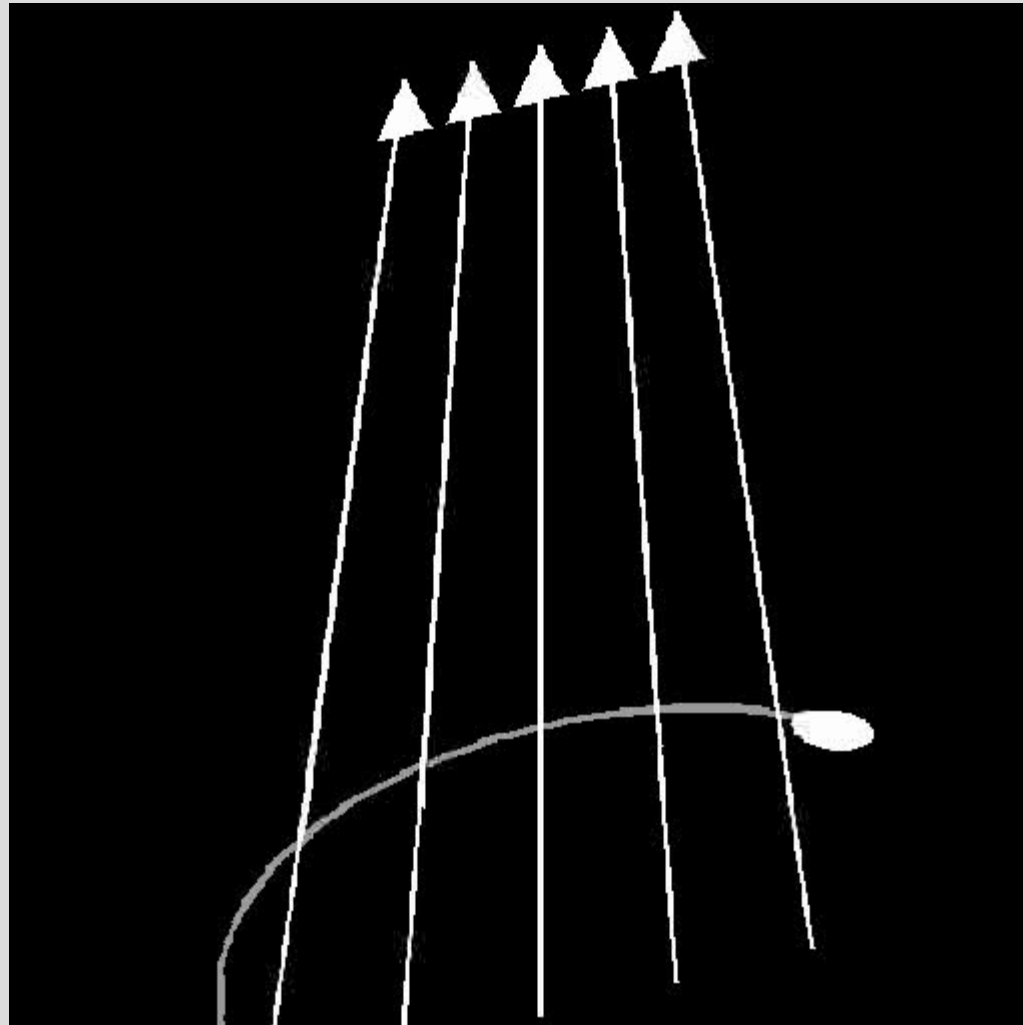
$$\frac{B_{\text{turn}}}{\sin^2 90^\circ} = \frac{B_0}{\sin^2 \alpha} \rightarrow$$

$$B_{\text{turn}} = \frac{B_0}{\sin^2 \alpha}$$

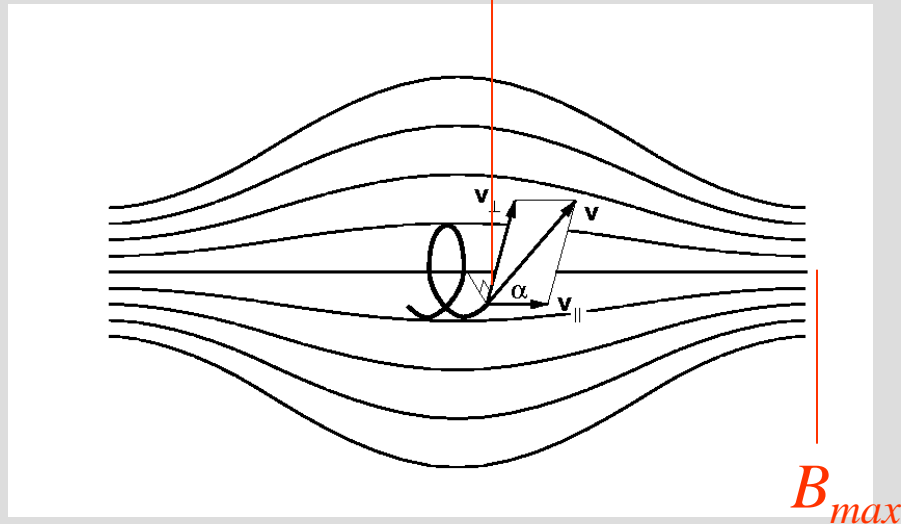
The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

# Magnetic mirror



# Magnetic mirror



$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{\text{turn}} = B_0 / \sin^2 \alpha$$

If maximal  $B$ -field is  $B_{\text{max}}$  a particle with pitch angle  $\alpha$  can only be turned around if

$$B_{\text{turn}} = B_0 / \sin^2 \alpha \leq B_{\text{max}} \rightarrow$$

$$\alpha > \alpha_{lc} = \arcsin \sqrt{B_0 / B_{\text{max}}}$$

Particles in  
loss cone :

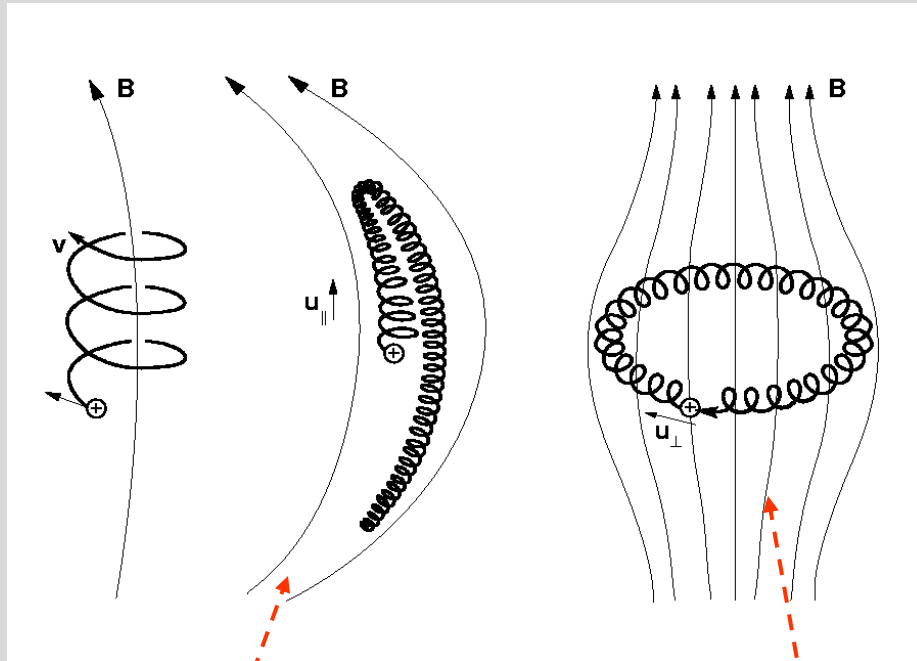
$$\alpha < \alpha_{lc}$$

The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

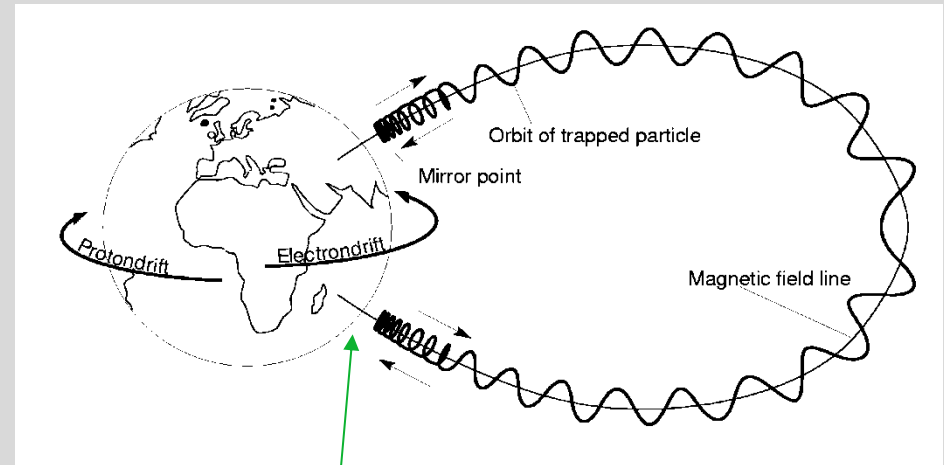
# Particle motion in geomagnetic field

longitudinal gyration      oscillation      azimuthal drift



Magnetic mirror

grad B drift

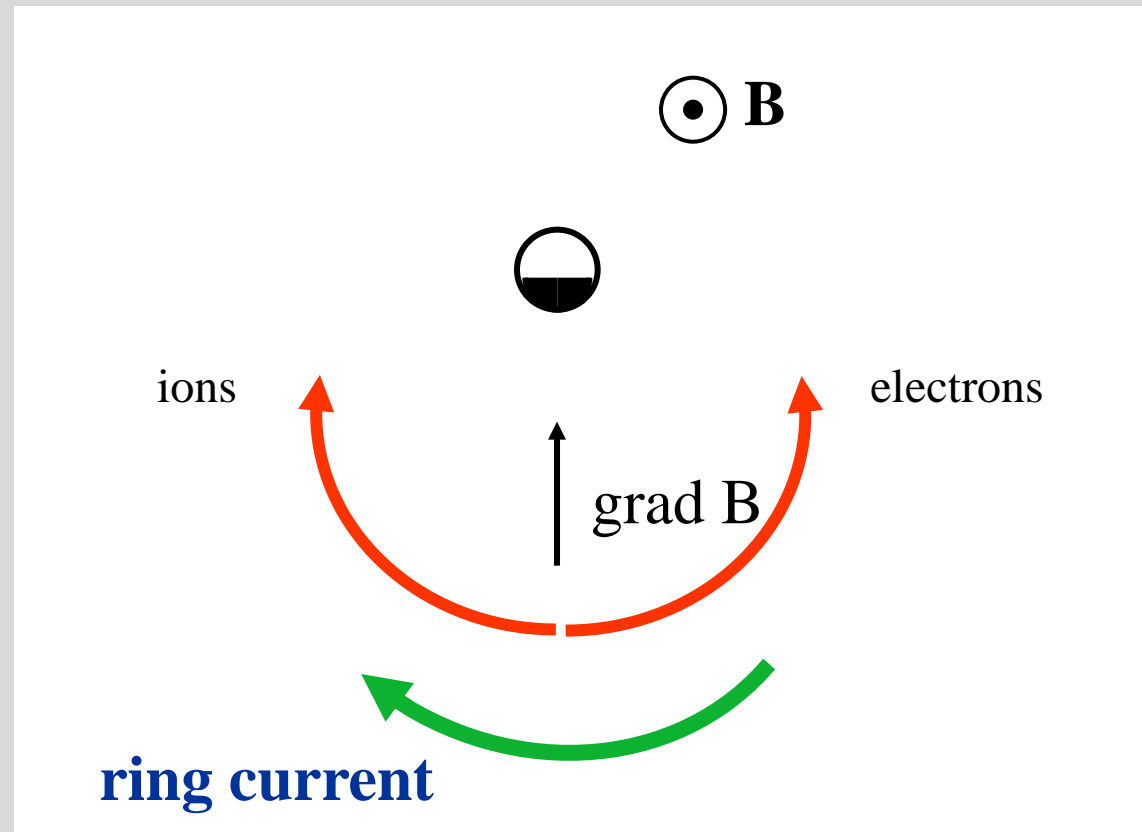


Particles in the loss cone create the aurora!

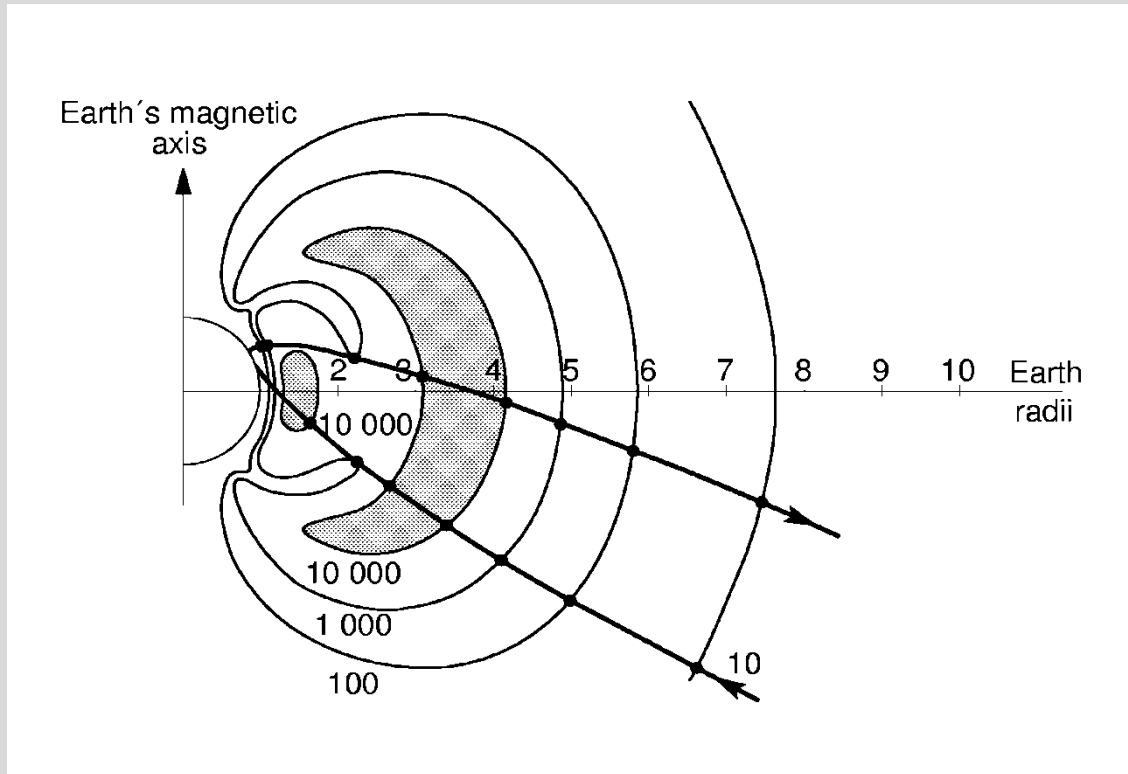
# Ring current and particle motion

$$\mathbf{u} = -\frac{\mu \nabla B \times \mathbf{B}}{qB^2}$$

$$\mu = \frac{mv_{\perp}^2}{2B}$$



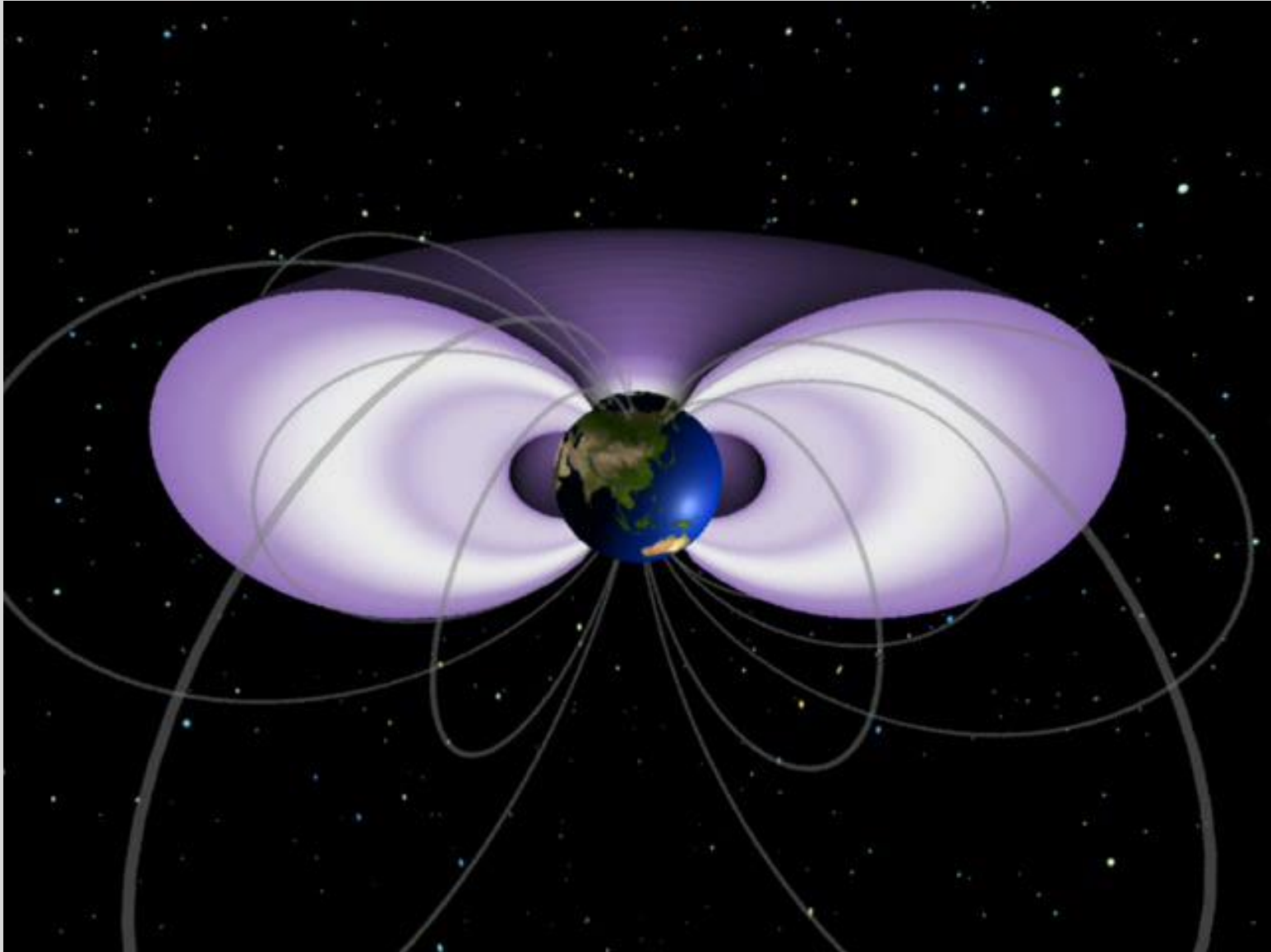
# Radiation belts



## I. Van Allen belts

- Discovered in the 50s , Explorer 1
- Inner belt contains protons with energies of  $\sim 30$  MeV
- Outer belt (Explorer IV, Pioneer III): electrons,  $W > 1.5$  MeV

# Radiation belts



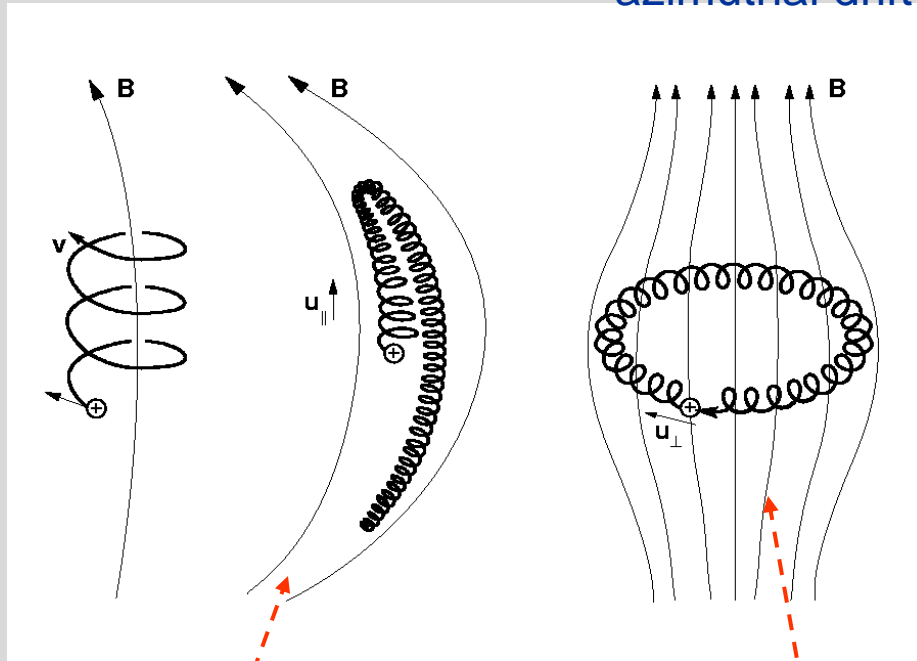


# Particle motion in geomagnetic field

longitudinal oscillation

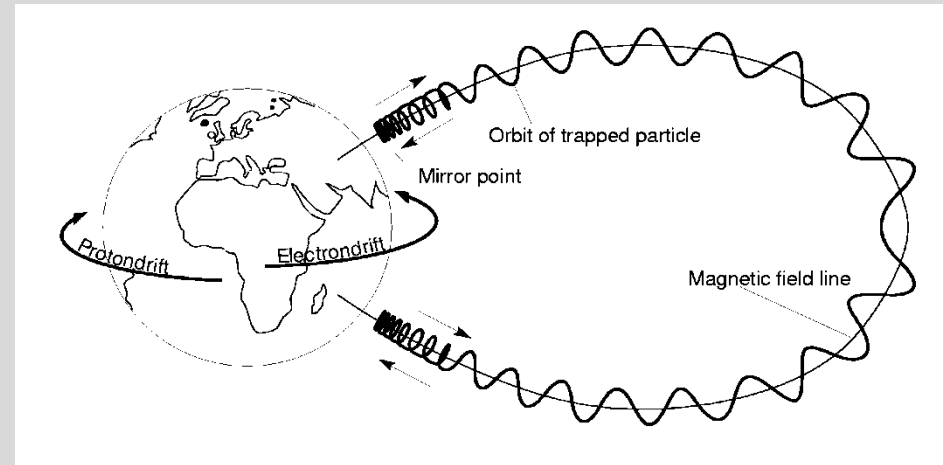
gyration

azimuthal drift



Magnetic mirror

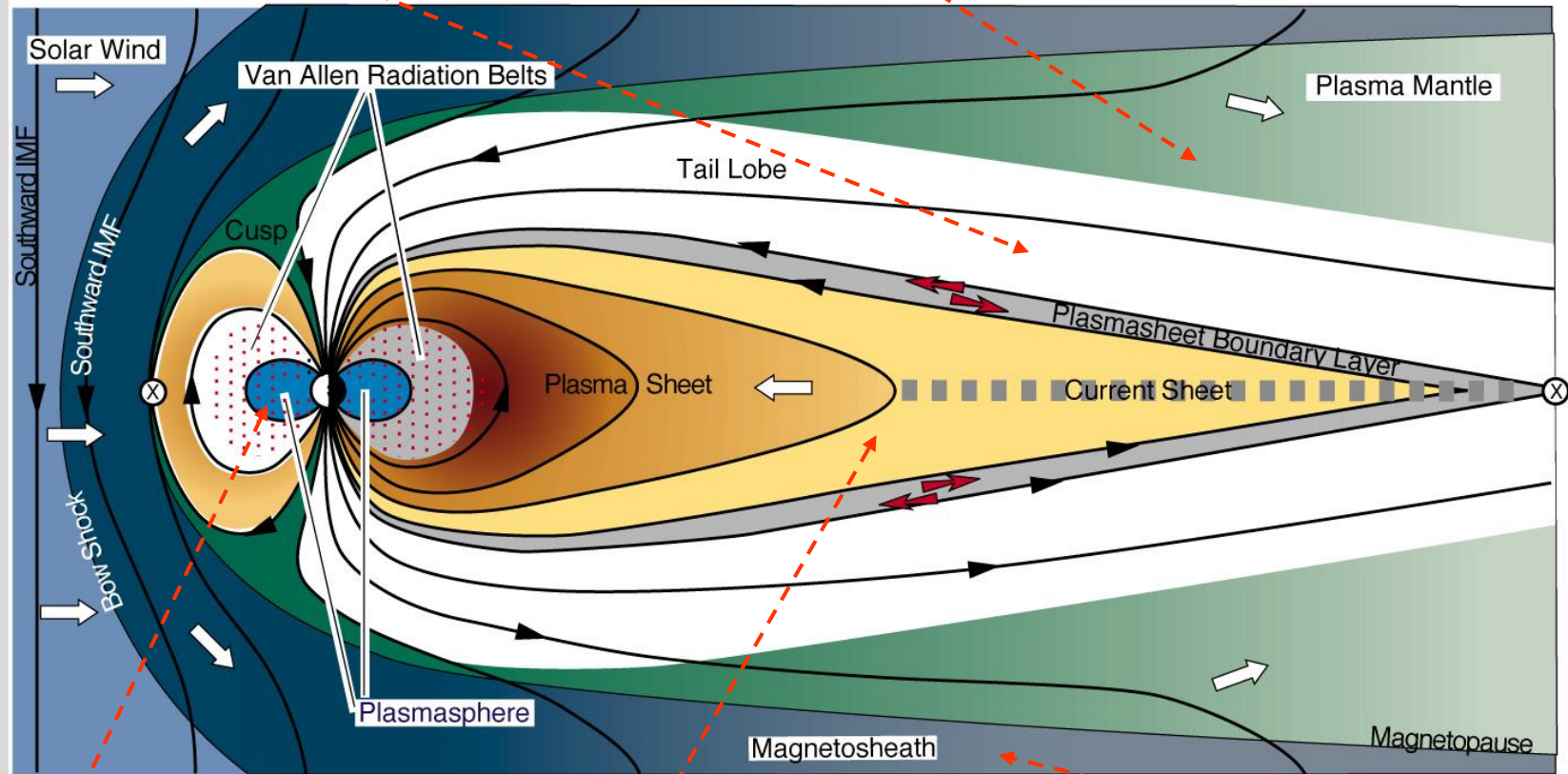
grad B drift



# Magnetospheric structure

polar plumes = tail lobe  
 $n_e \sim 0,01 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

plasma mantle  
 $n_e \sim 0,1-1 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$



plasmasphere:  
 $n_e \sim 10-100 \text{ cm}^{-3}$ ,  $T_e \sim 1000 \text{ K}$

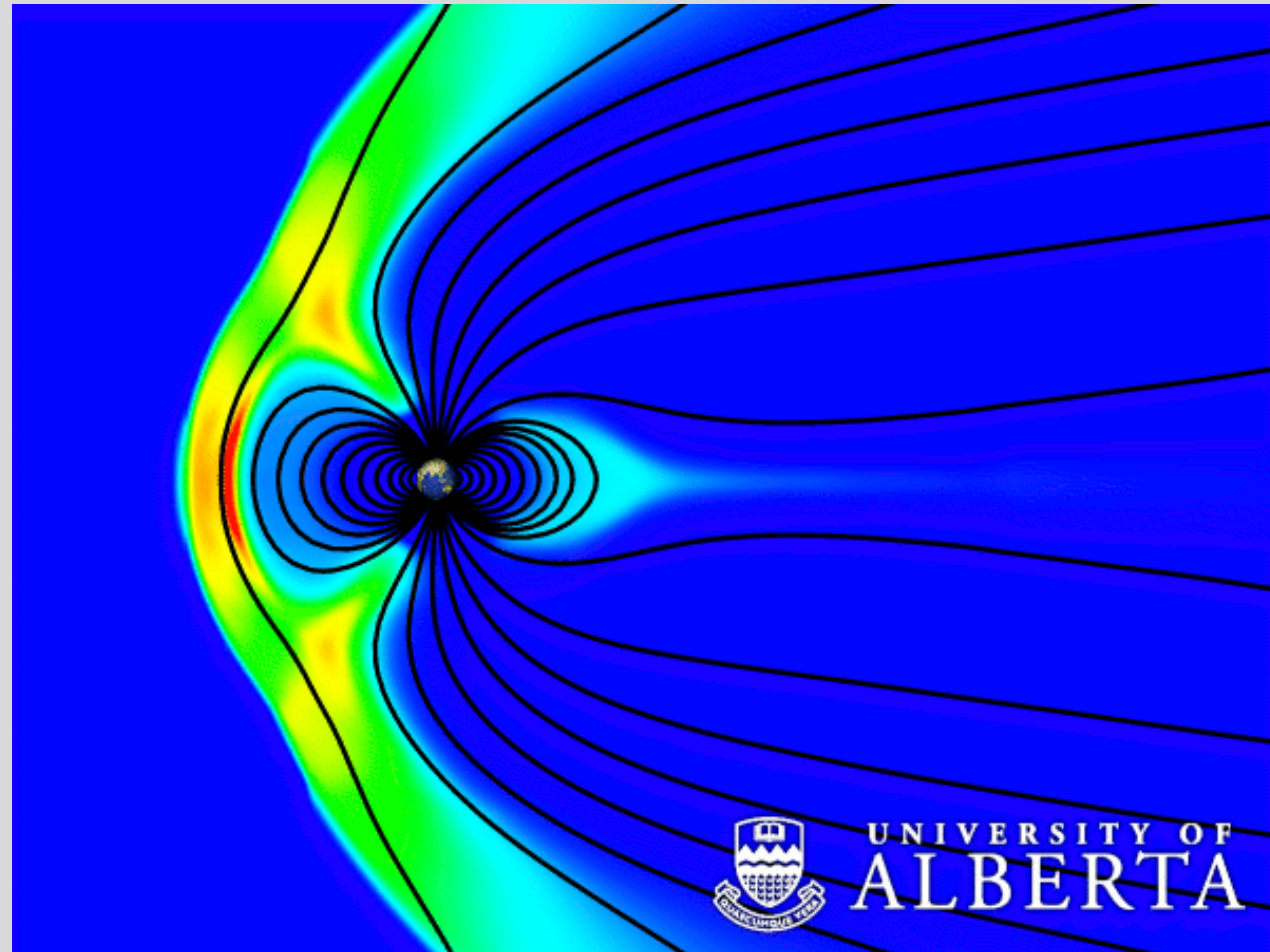
plasma sheet:  
 $n_e \sim 1 \text{ cm}^{-3}$ ,  $T_e \sim 10^7 \text{ K}$

magnetosheath:  
 $n_e \sim 5 \text{ cm}^{-3}$ ,  $T_e \sim 10^6 \text{ K}$

# Reconnection and plasma convection

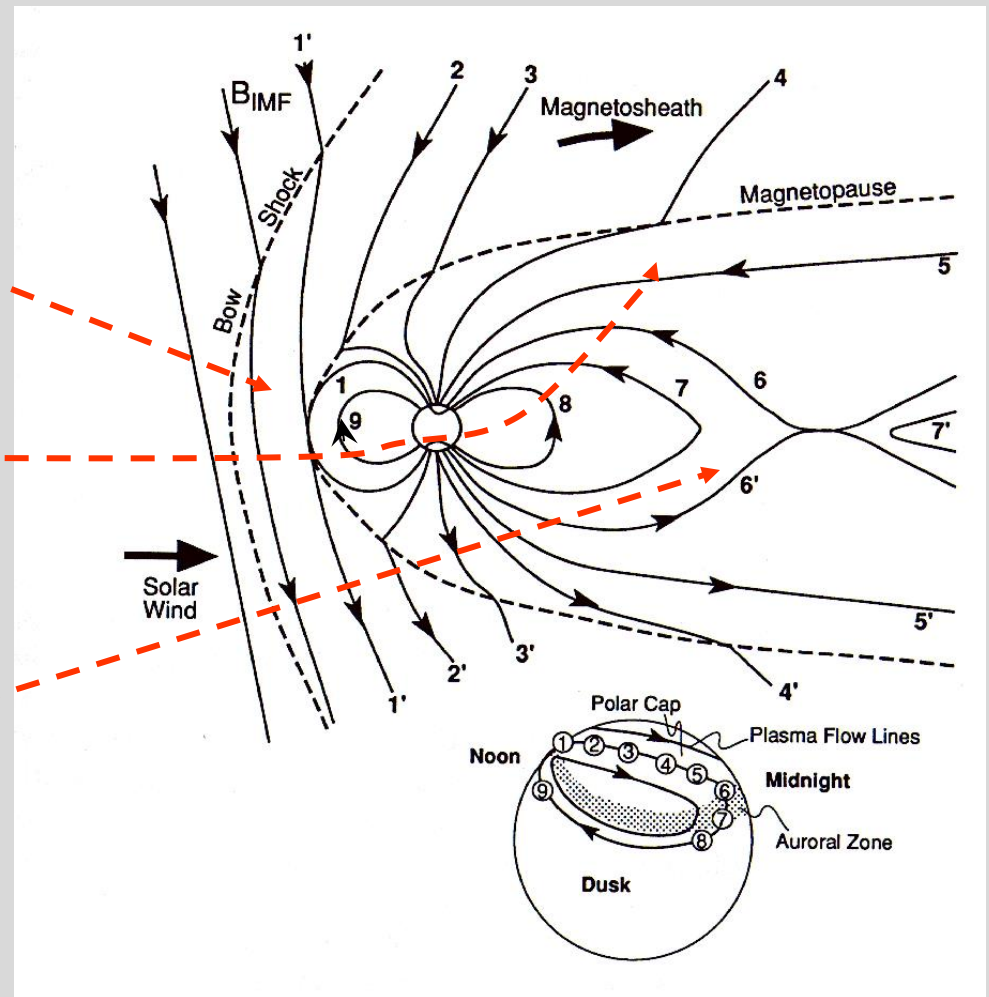


Solar wind

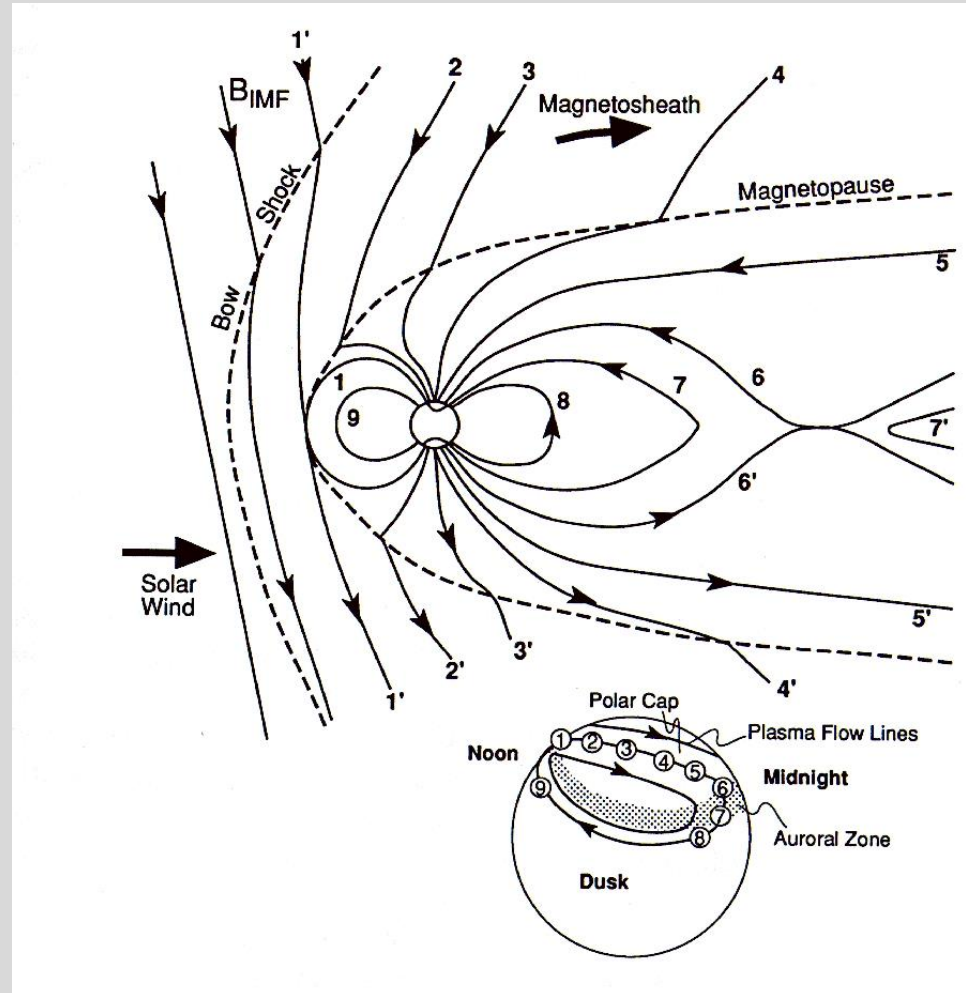


# Reconnection och plasma convection

- Reconnection on the dayside “re-connects” the solar wind magnetic field and the geomagnetic field
- In this way the plasma convection in the outer magnetosphere is driven
- In the night side a second reconnection region drives the convection in the inner magnetosphere. The reconnection also heats the plasmashet plasma.

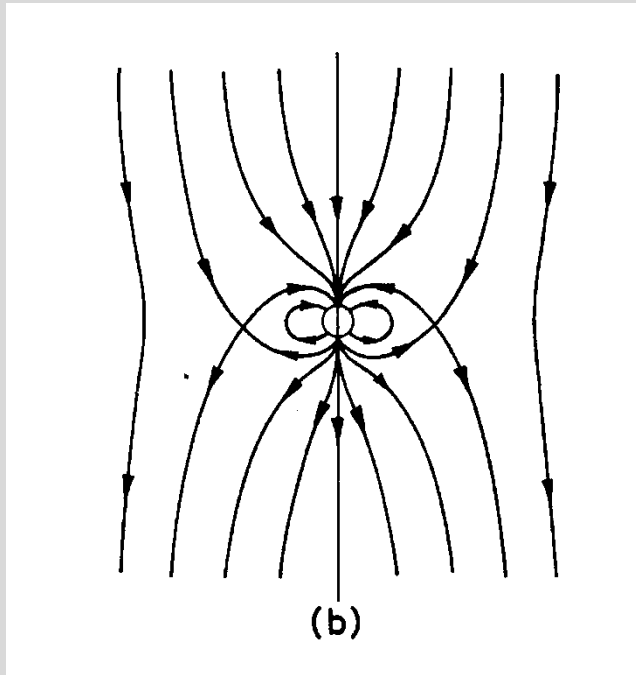


# What happens if IMF is northward instead?

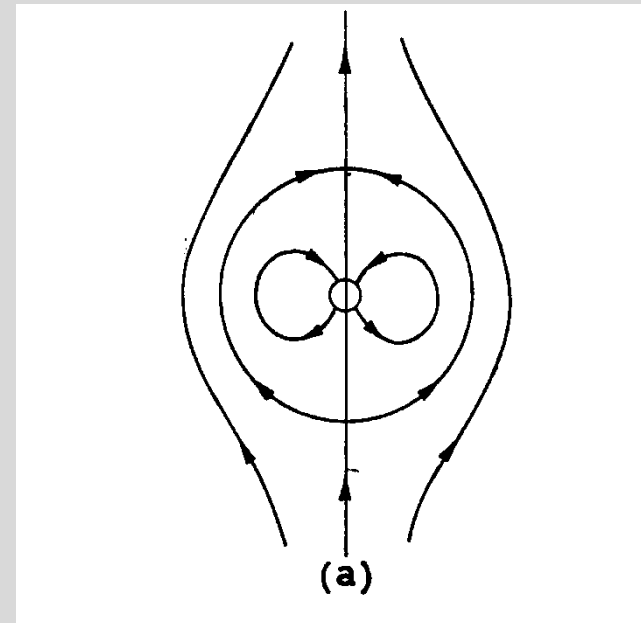


# Magnetospheric dynamics

*open magnetosphere*



*closed magnetosphere*



**southward** 

**Interplanetary  
magnetic field (IMF)**

 **northward**



# What do the magnetospheres of the other planets look like?

# Planetary magnetospheres

	Radius Earth radii	Spin period (days)	Equatorial field strength ( $\mu\text{T}$ )	Magnetic axis direction relative to spin axis	Polarity relative to Earth's	Typical magnetopause distance (planetary radii)
Mercury	0.38	58.6	0.35	$10^\circ$	Same	1.1
Venus	0.95	243	< 0.03	-	-	1.1
Earth	1.0	1	31	$11.5^\circ$	Same	10
Mars	0.53	1.02	0.065	-	Opposite	?
Jupiter	11.18	0.41	410	$10^\circ$	Opposite	60-100
Saturn	9.42	0.44	40	$<1^\circ$	Opposite	20-25
Uranus	3.84	0.72	23	$60^\circ$	Opposite	18-25
Neptune	3.93	0.74	20-150 <sup>*)</sup>	$47^\circ$	Opposite	26 <sup>**)</sup>

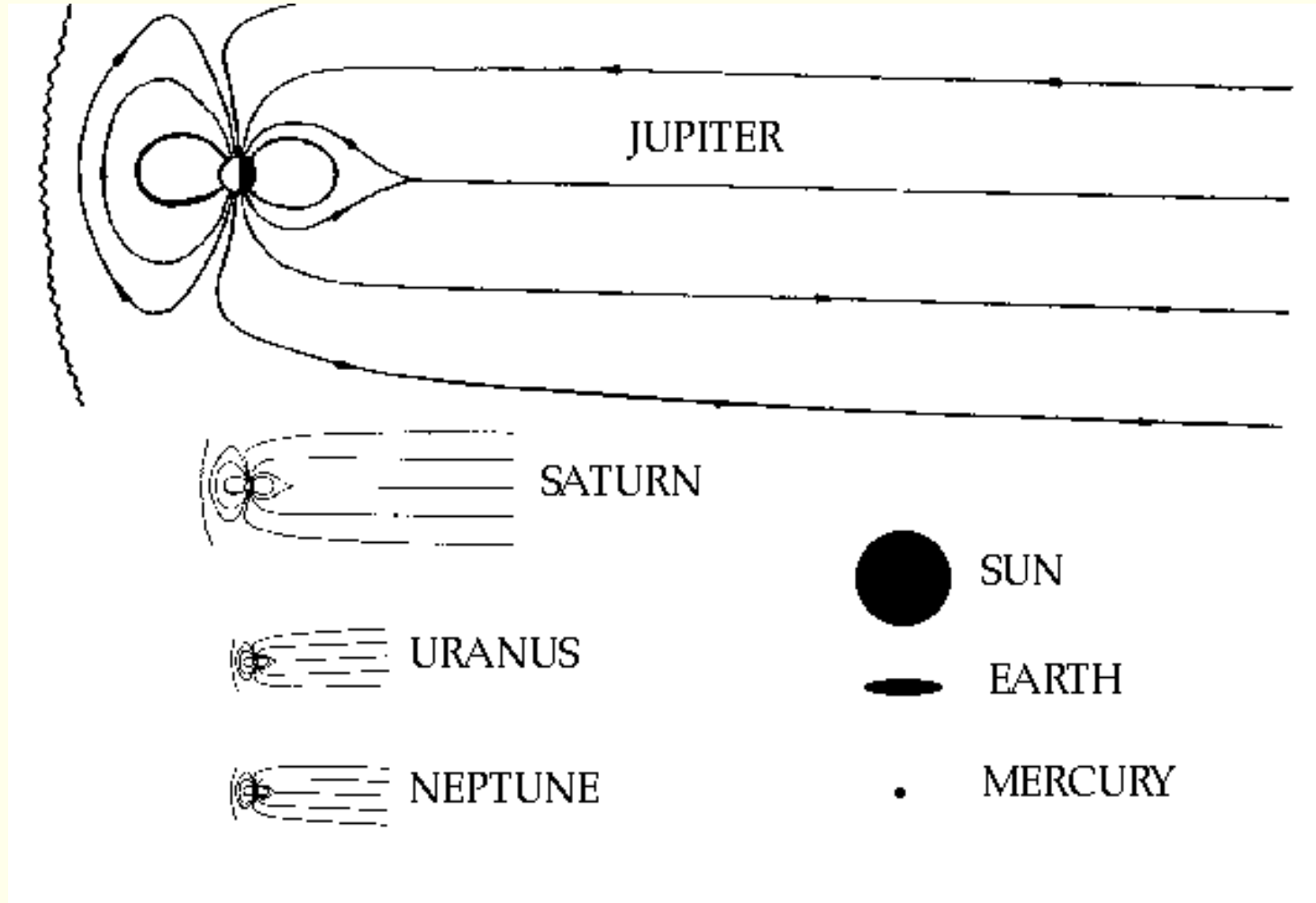
\*) The magnetic field differs greatly from a dipole field. The numbers represent maximum and minimum strength at the planetary surface

\*\*\*) Based on single passage

Very weak magnetic fields



# Relative size of the magnetospheres



# Comparative magnetospheres

## In situ observations

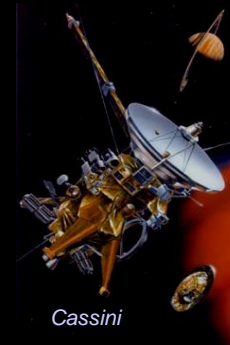
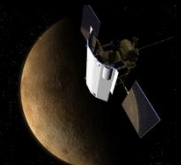
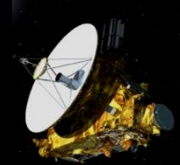
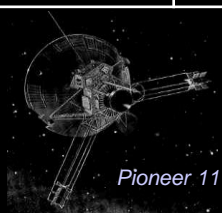
*Space probe*

*Celestial body*

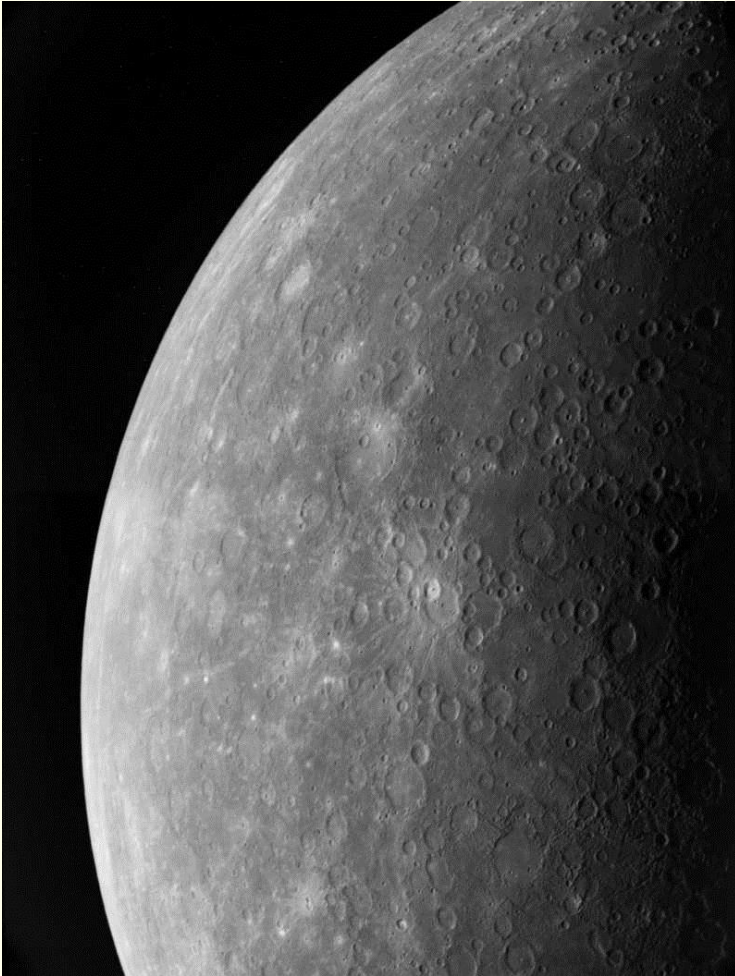
*Observations*

<i>Mariner 10</i>	Mercury	1974 – 1975
<i>Messenger *</i>	Mercury	2008 – 2015
<i>Pioneer 10,11</i>	Jupiter, Saturn	1973 – 1979
<i>Voyager 1,2</i>	Jupiter, Saturn, Uranus, Neptune	1977 – 1989
<i>Ulysses</i>	Jupiter	1992
<i>Galileo*</i>	Jupiter	1995 – 2003
<i>Cassini*</i>	Jupiter, Saturn	2004 –
<i>New Horizons</i>	Jupiter	2007
<i>Rosetta</i>	Churymov-Gerasimenko	2014 - 2016

\* *Orbiters*



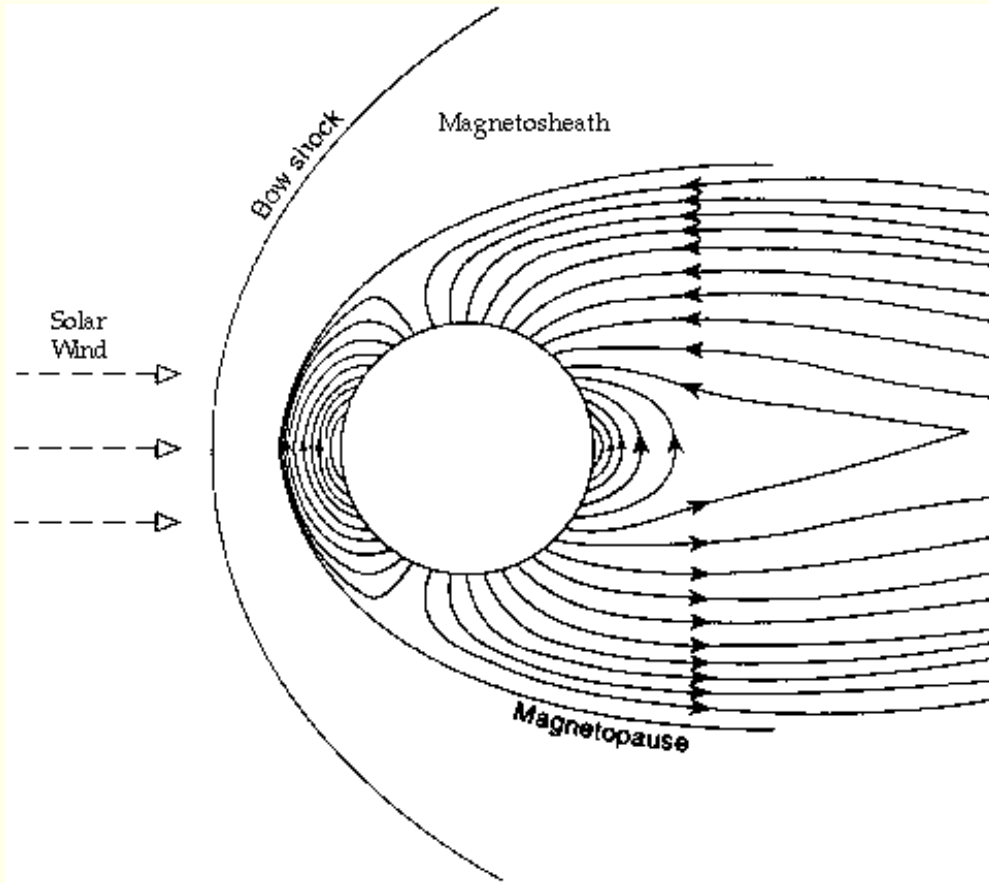
# Mercury



*Photo from Mariner 10*

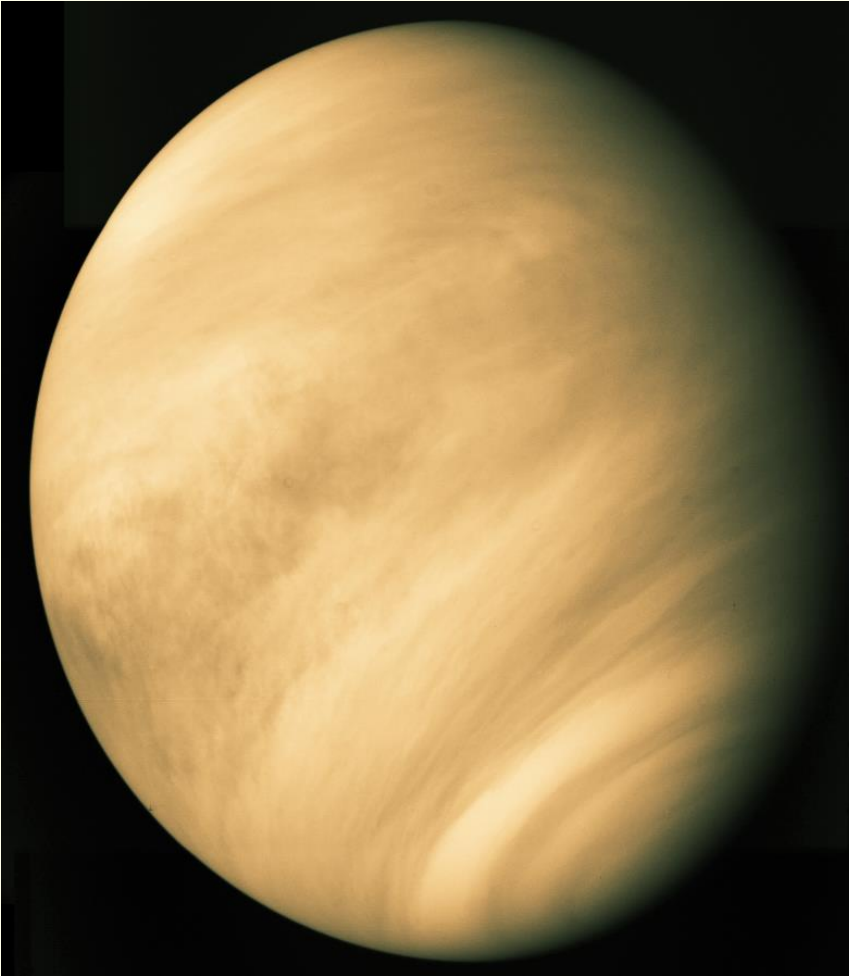
- $r_M = 0,38 r_E$
- $m_M = 0,06 m_E$
- distance from sun: 0,39 AU
- no or extremely thin atmosphere

# Mercury's magnetosphere



- rather large magnetic field
- the high solar wind density close to the sun makes the magnetosphere very small
- no ionosphere

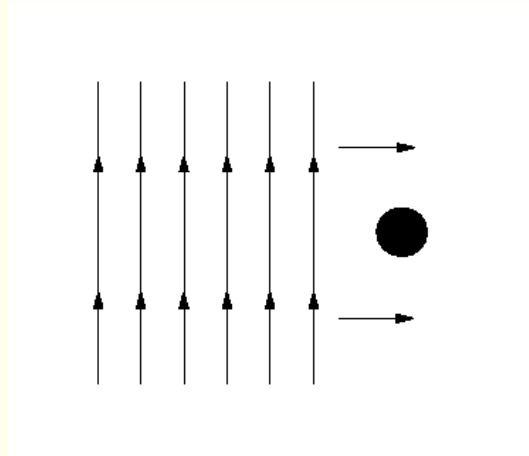
# Venus



*Photo from Galileo*

- $r_V = 0,95 r_E$
- $m_V = 0,82 m_E$
- distance from sun : 0,72 AU
- very dense atmosphere
  - $\sim 90$  atm
  - 96%  $\text{CO}_2$
- very weak magnetic field

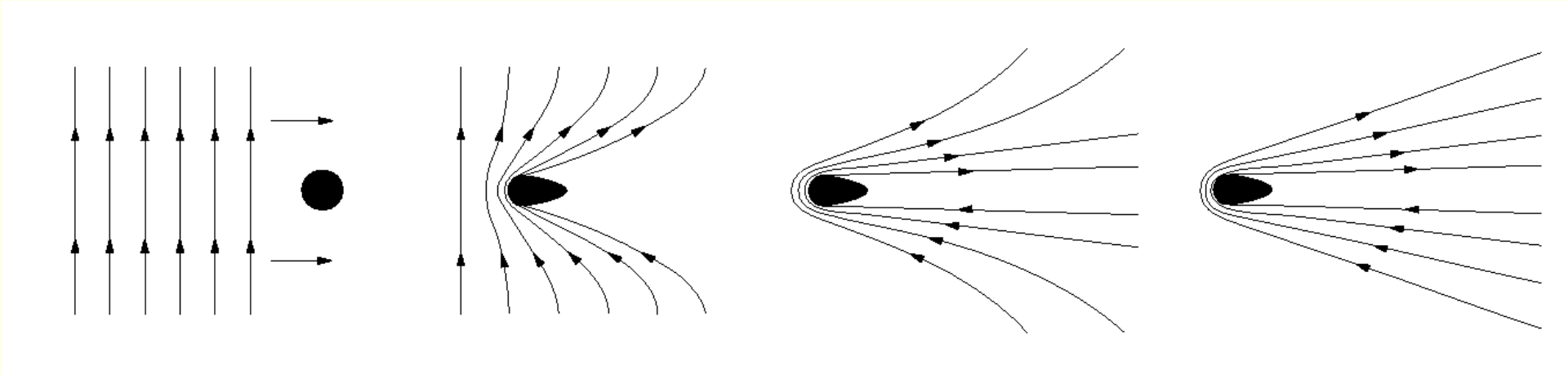
# Comets, induced magnetotail



- The *coma* of the comet is ionized when the comet gets close to sun

**What will happen when the interplanetary magnetic field (which is frozen into the solar wind) hits the coma?**

# Comets, induced magnetotail



- The **coma** of the comet is ionized when the comet gets close to sun
- This plasma stops the field lines from passing the comet, due to the frozen-in magnetic field
- Venus and Mars have similar induced, weak "magnetospheres"

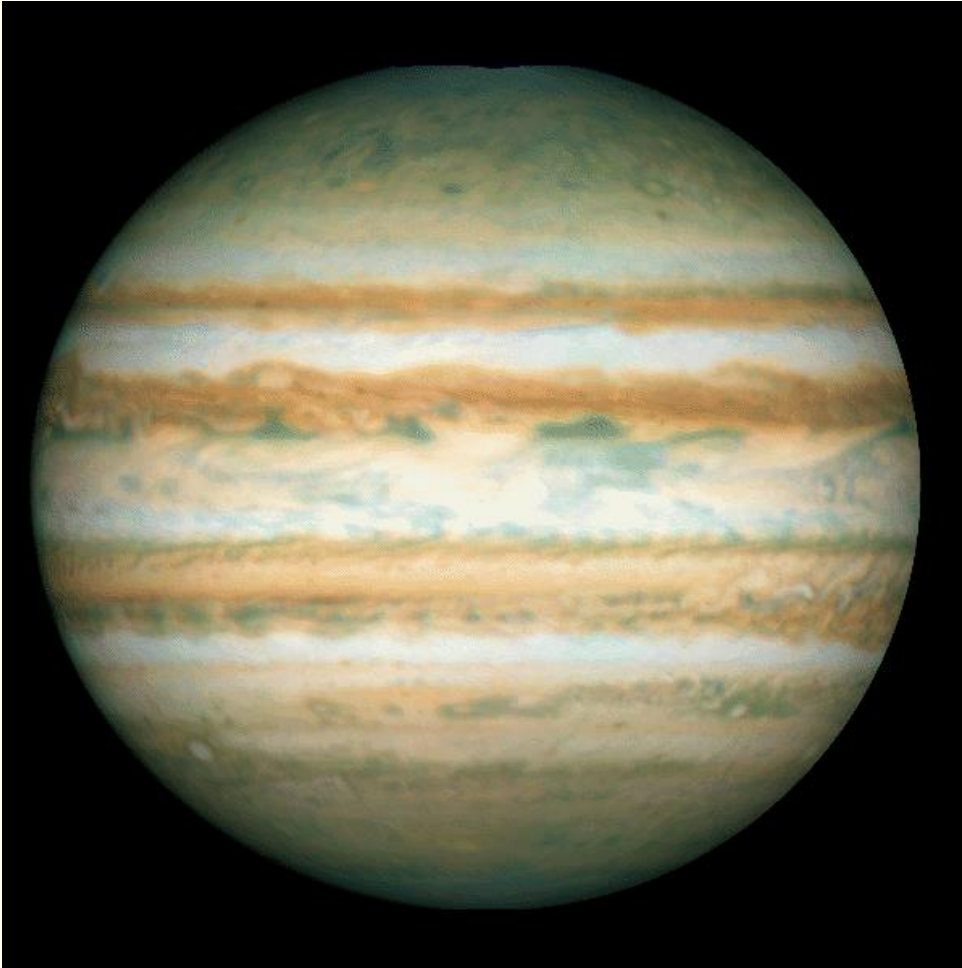


*Photo from Hubble Space Telescope*

# Mars

- $r_M = 0,53 r_E$
- $m_M = 0,11 m_E$
- distance from sun : 1,52 AU
- very thin atmosphere
  - $\sim 0.01$  atm.
  - 95%  $\text{CO}_2$
- very weak magnetic field



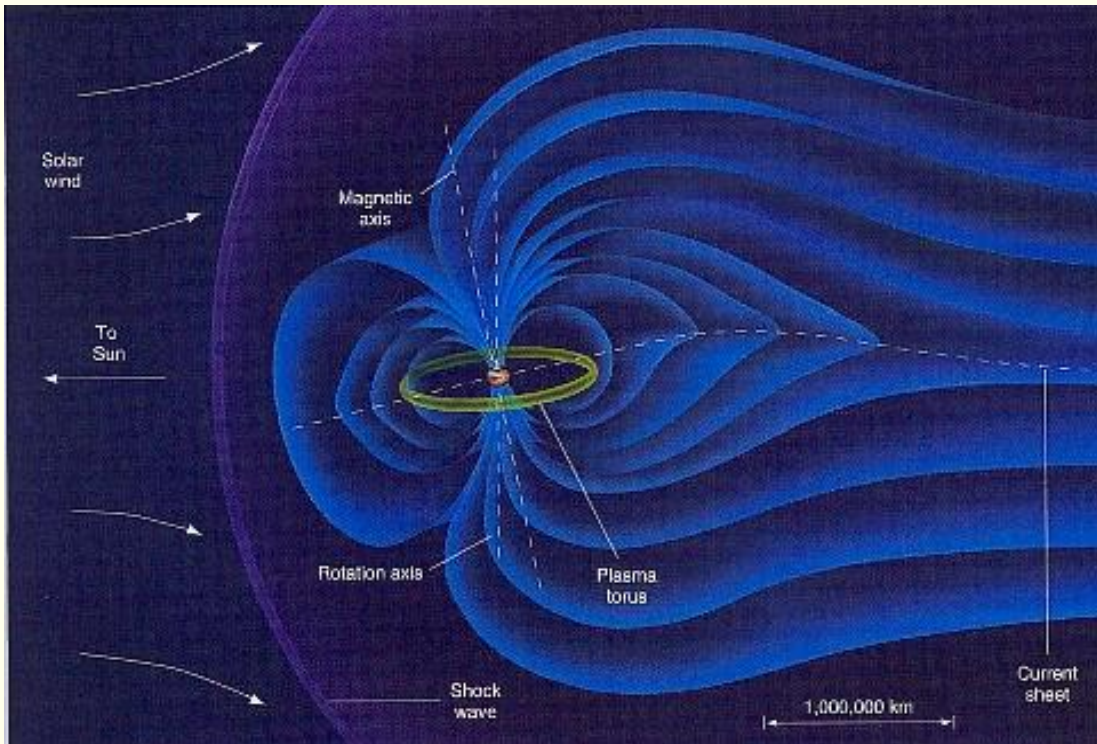


*Photo from Hubble Space Telescope*

# Jupiter

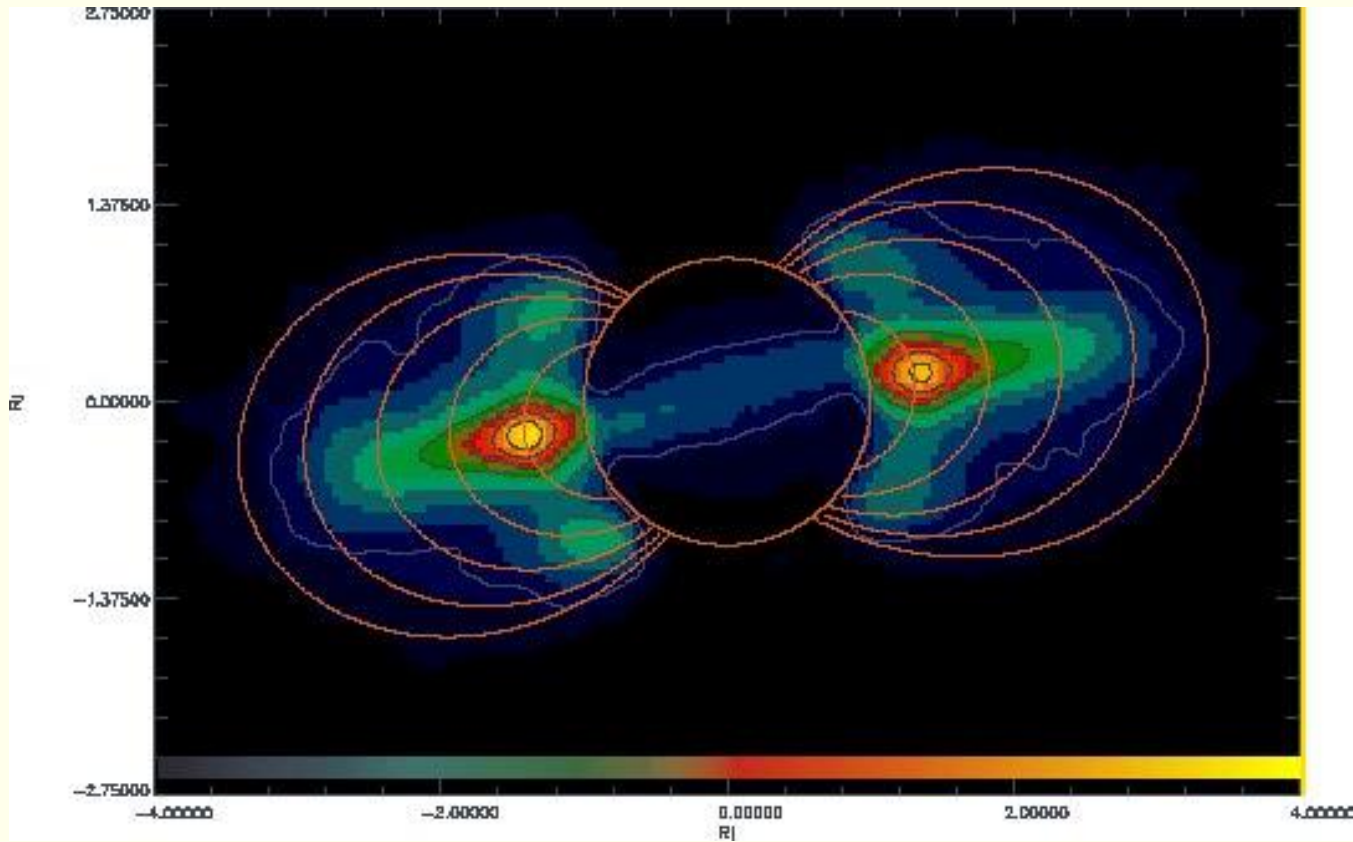
- $r_J = 11,2 r_E$
- $m_J = 318 m_E$
- distance from sun: 5,20 AU
- gas giant with very dense atmosphere containing hydrogen, helium, ammonium, methane, etc.
- ~ 60 moons (+ weak ring system)

# Jupiter's magnetosphere



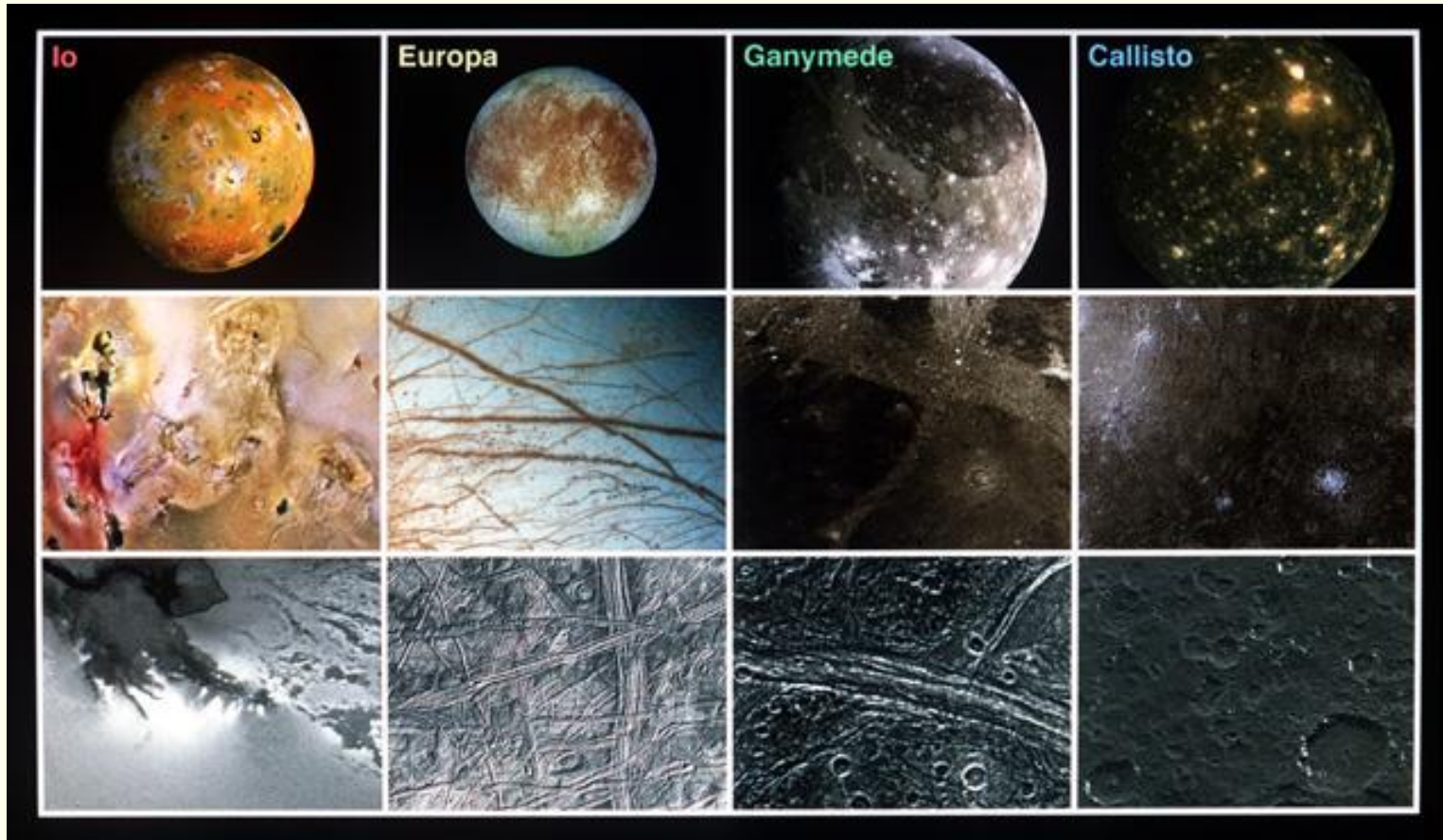
- high plasma density, Io is an important source
- plasma pressure thus becomes an important factor for balancing the solar wind pressure
- the plasma co-rotates with Jupiter, which gives the magnetosphere a flattened look

# Synchrotron radiation from Jupiter's radiation belts



- Gyrating electrons emit "synchrotron radiation" with frequencies  $\sim f_{ce} = eB/(2\pi m_e)$
- The emitted power is proportional to the electron temperature:  
$$P = CT_e$$
- In this way you can get a picture of the radiation belts

# Galilean satellites



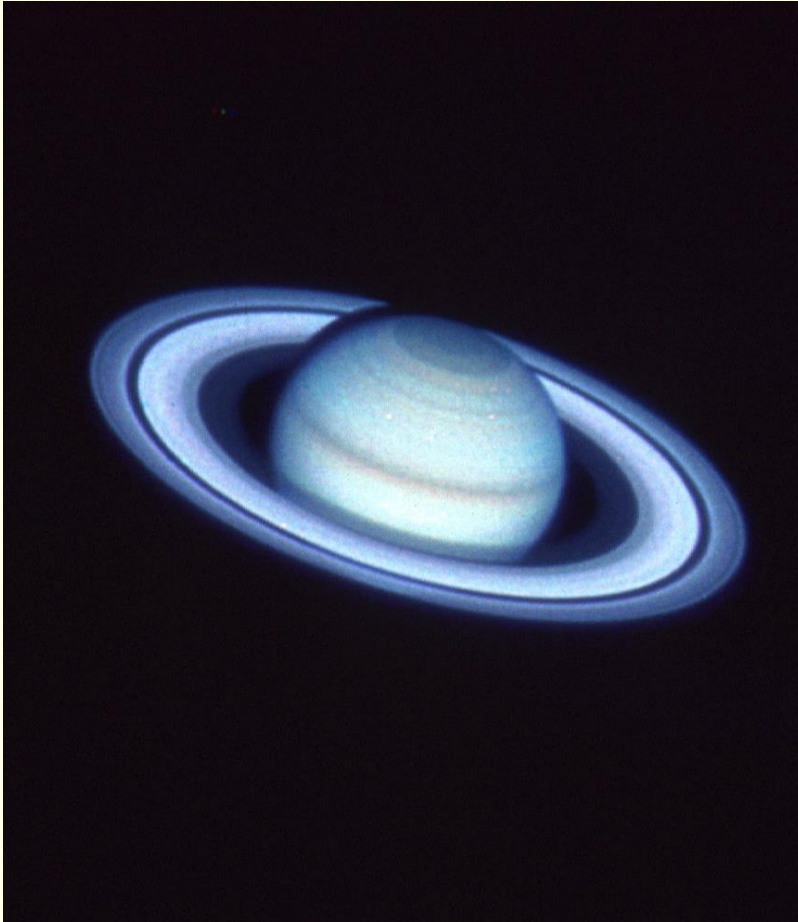
Volcanic activity, source for plasma.

Oceans under the ice?

Has its own magnetosphere the size of Mercury's

Weak magnetic field

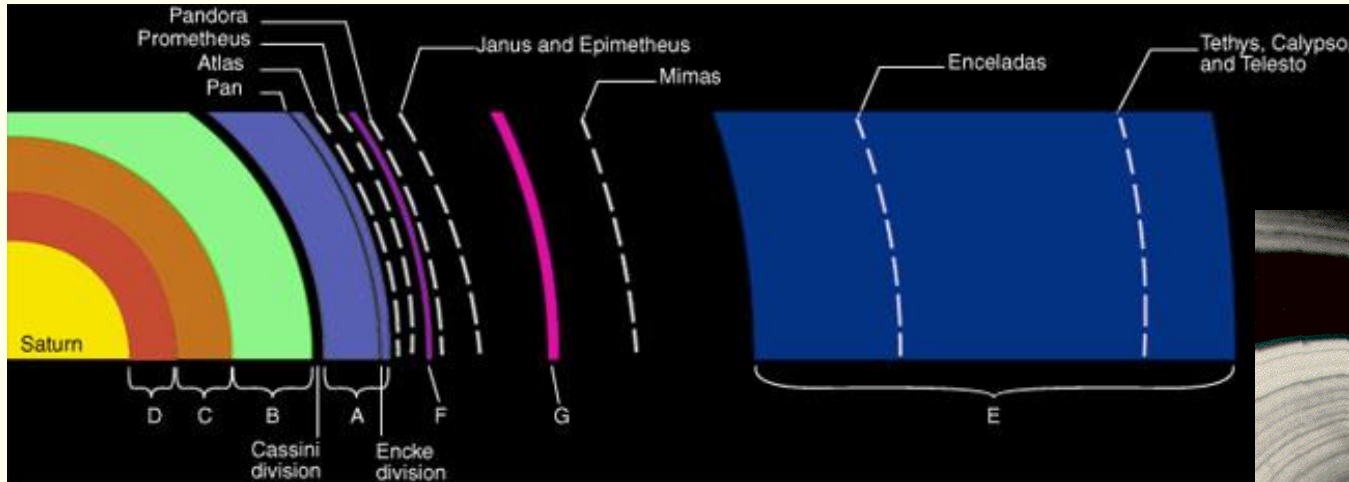
# Saturn



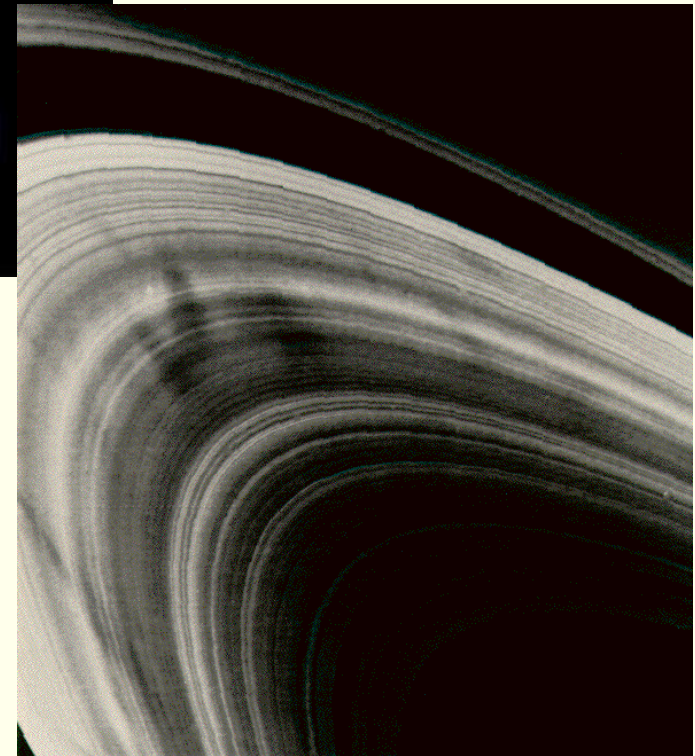
*Photo from Hubble Space Telescope*

- $r_s = 9,42 r_E$
- $m_s = 95 m_E$
- distance from sun: 9.53 AU
- gas giant with very dense atmosphere containing sulphur, hydrogen, helium, ammonium, methane, etc.
- ~ 31 moons + ring system

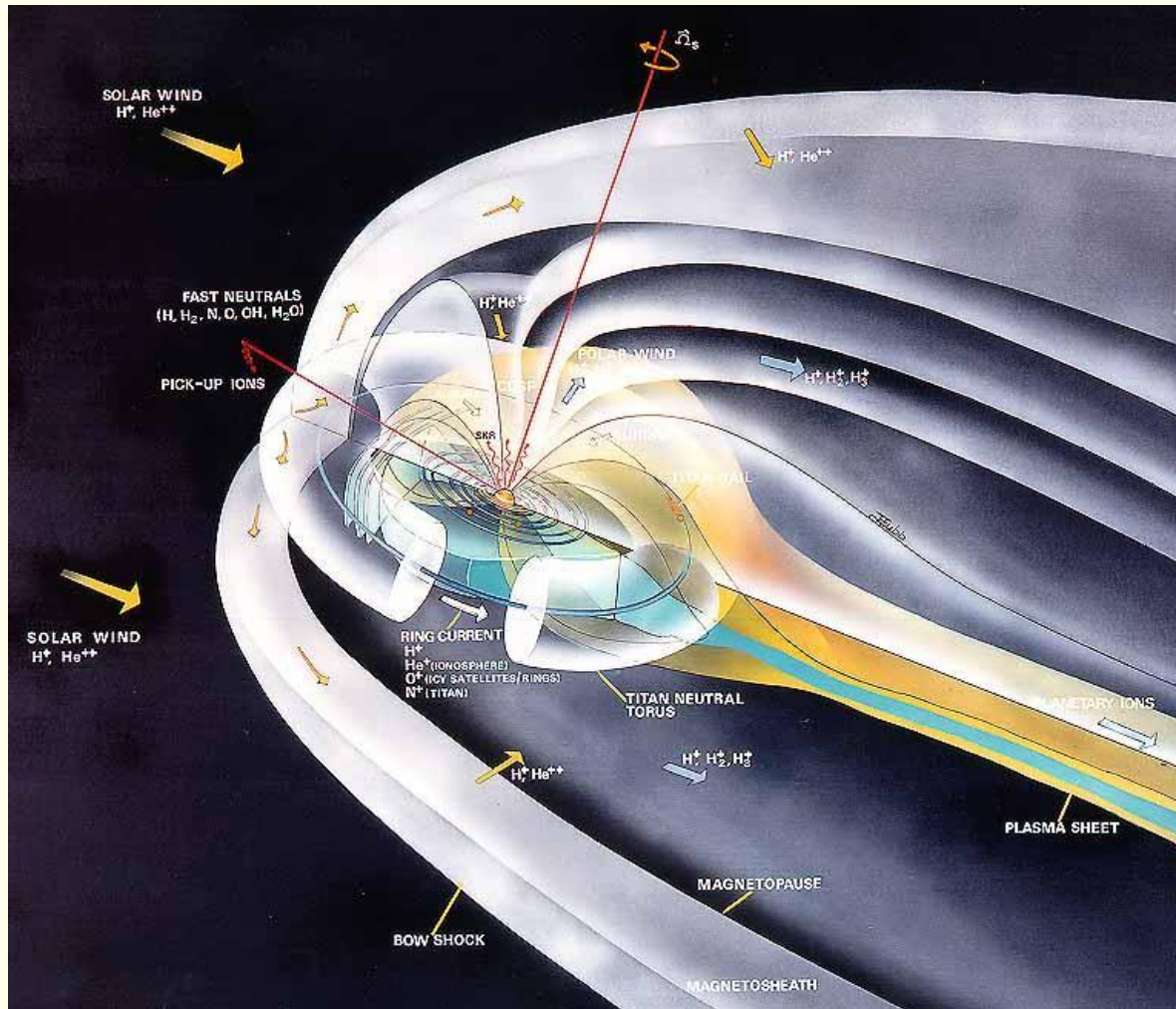
# Saturn's rings



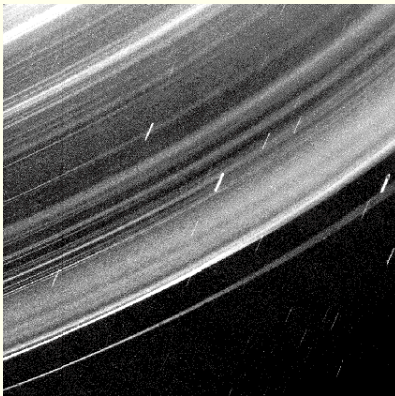
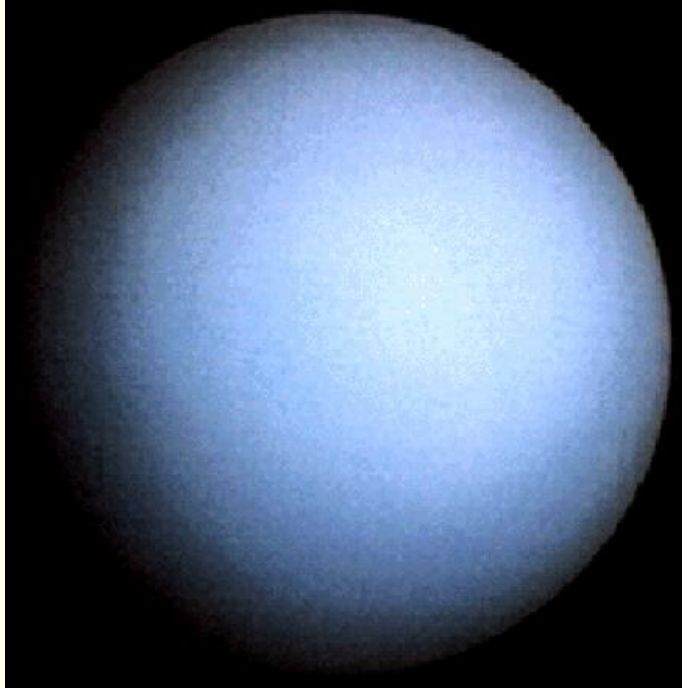
- ring system is made up of ice and mineral particles from  $\sim 1$  cm to  $\sim 1$  km
- rings are only 1.5 km thick



# Saturn's magnetosphere



- ring system is both source and sink for plasma and limits the size of the plasmasphere
- plasma pressure important for balancing solar wind pressure, just as for Jupiter
- Intense radiation belt with 50 MeV protons

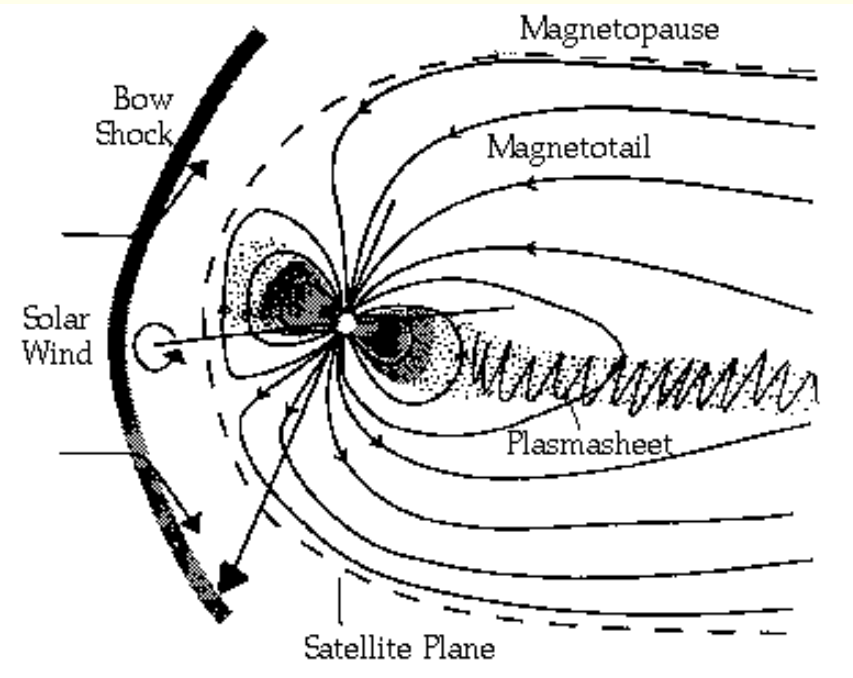
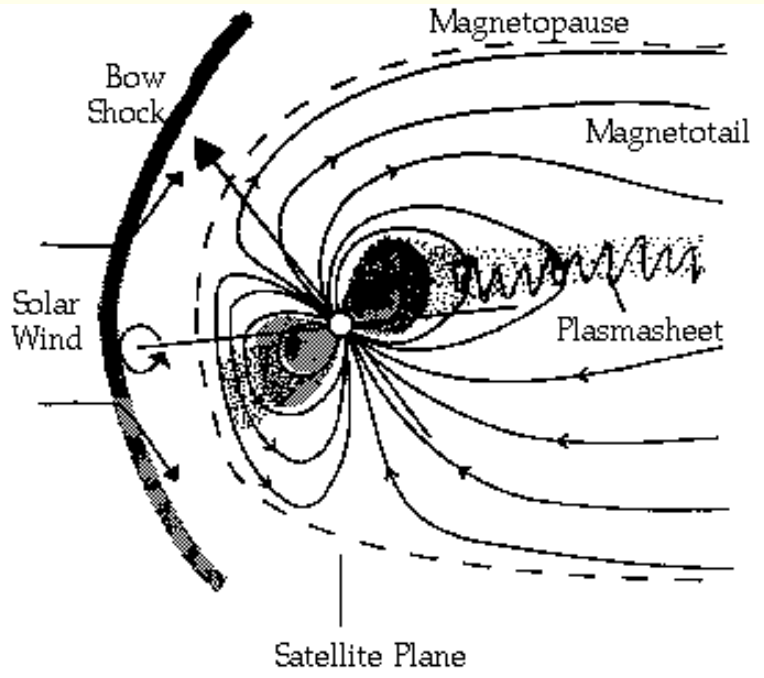


# Uranus

- $r_U = 3,84 r_E$
- $m_U = 14,5 m_E$
- distance from sun: 19,2 AU
- gas giant with very dense atmosphere containing mainly methane
- 20 moons + ring system



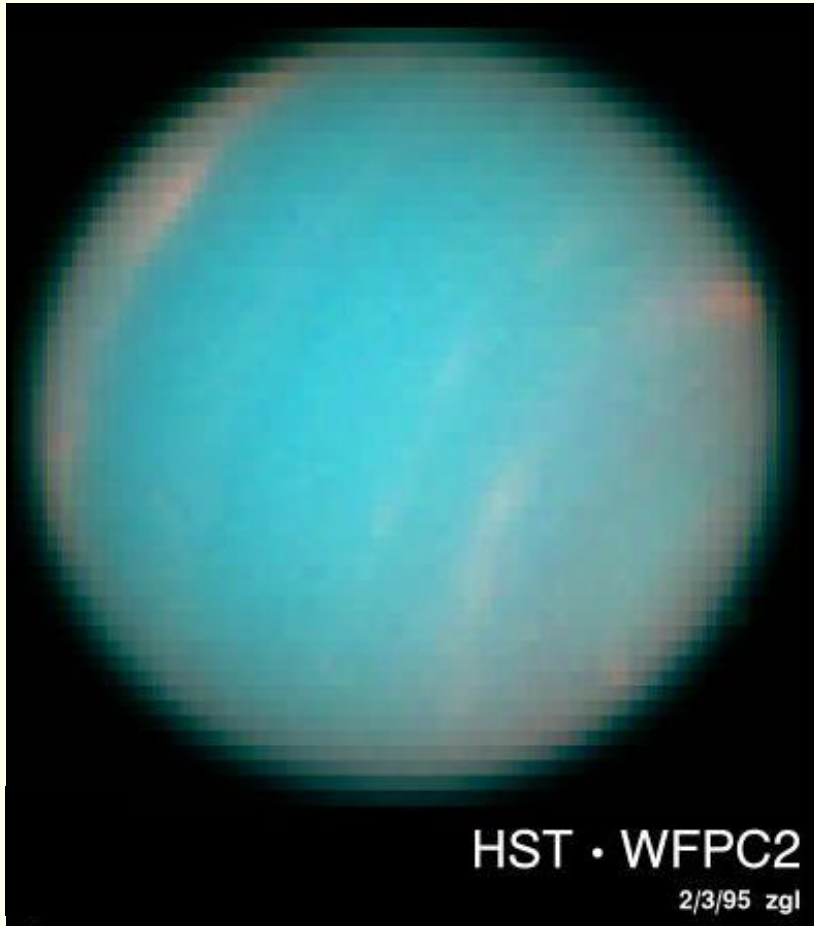
# Uranus



- Uranus' rotational axis almost in ecliptic plane
- magnetic field axis makes an angle of around  $60^\circ$  with rotational axis
- this gives enormous daily variations of the structure of the magnetosphere

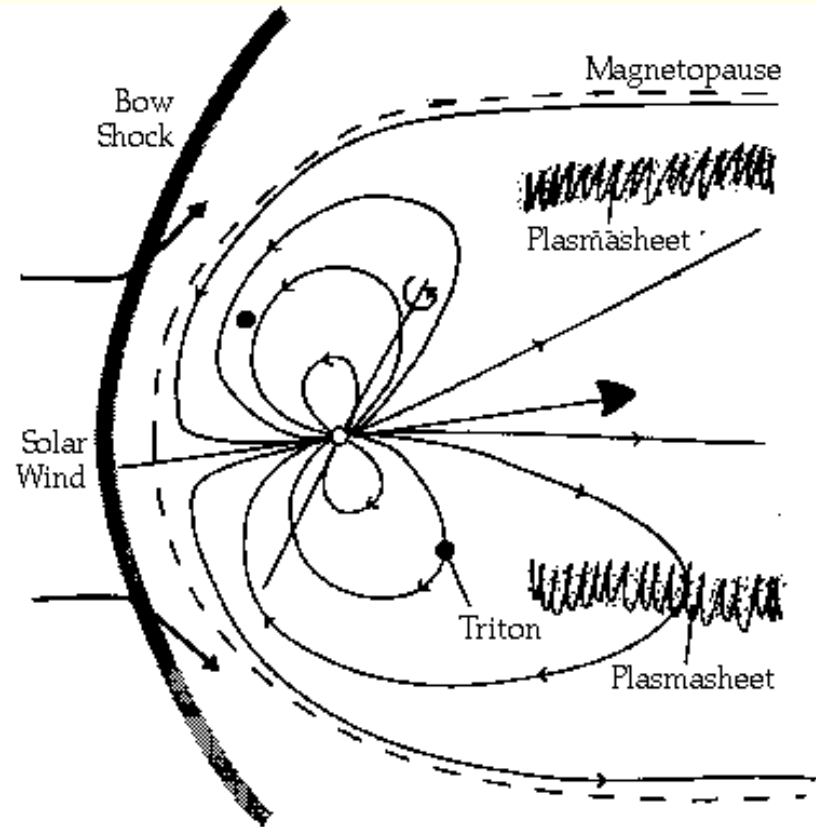
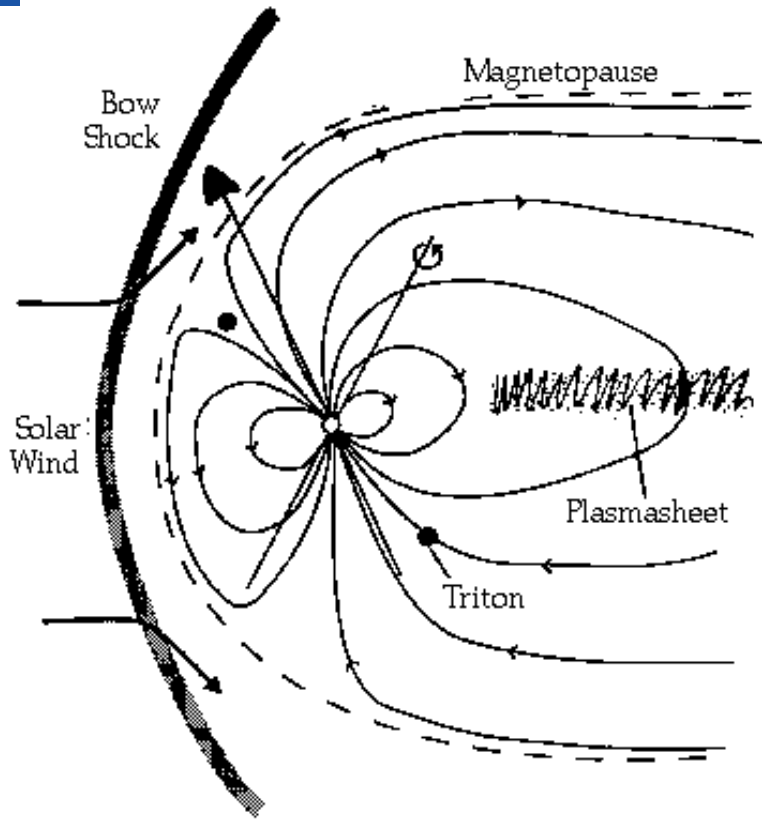
# Neptune

- $r_N = 3,93 r_E$
- $m_N = 17,2 m_E$
- distance from sun : 30.1 AU
- gas giant with very dense atmosphere containing mainly methane
- 11 moons + ring system



*Photo from Hubble Space Telescope*

# Neptune

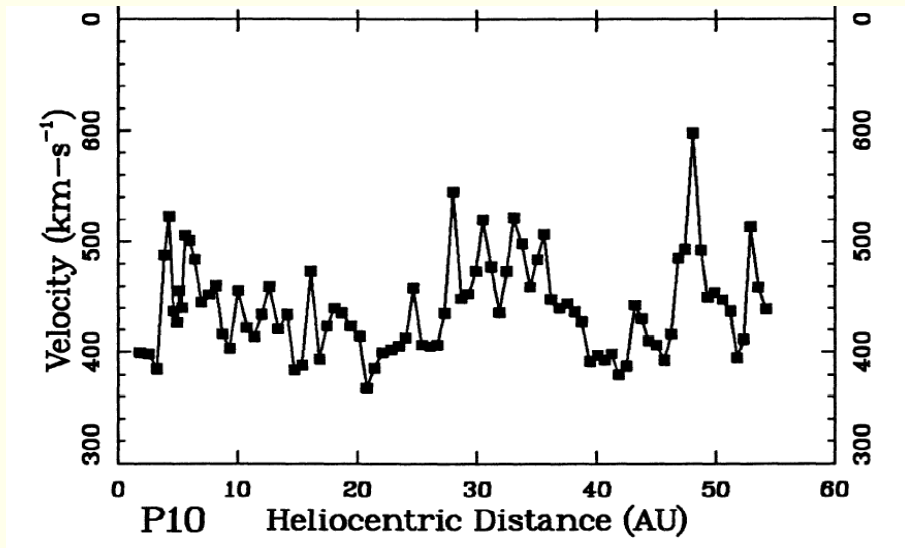


- magnetic field axis makes an angle of around  $43^\circ$  with rotational axis
- this gives enormous daily variations of the structure of the magnetosphere also for Neptune

# Comparative magnetospheres

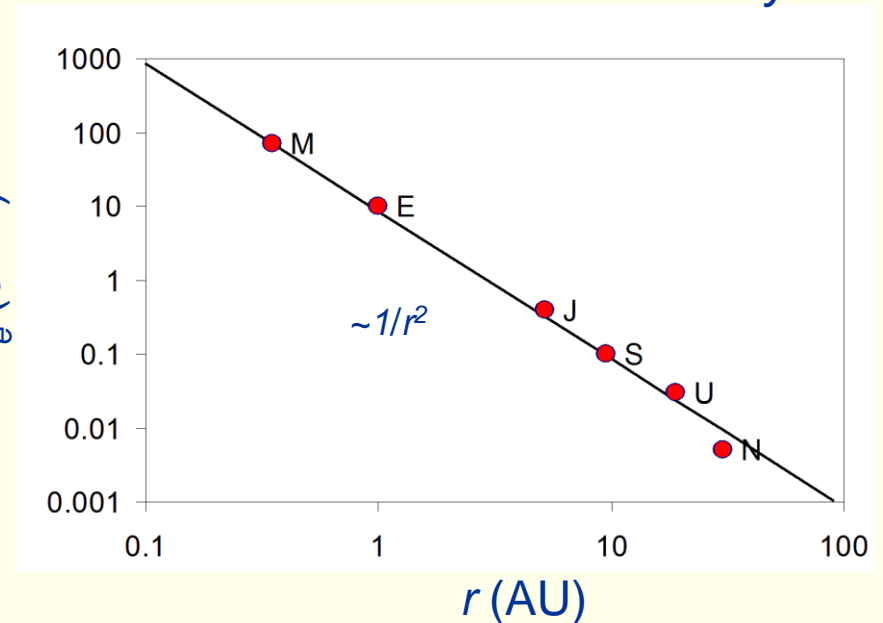
## Solar wind properties

*Solar wind velocity*

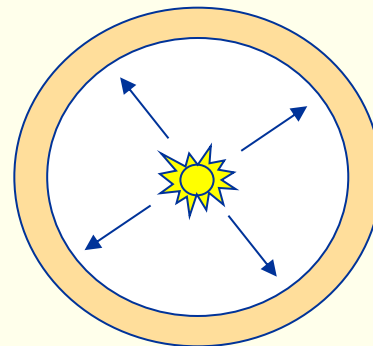


*Pioneer 10, measurements  
[Grazin et al., 1994]*

*Solar wind electron density*



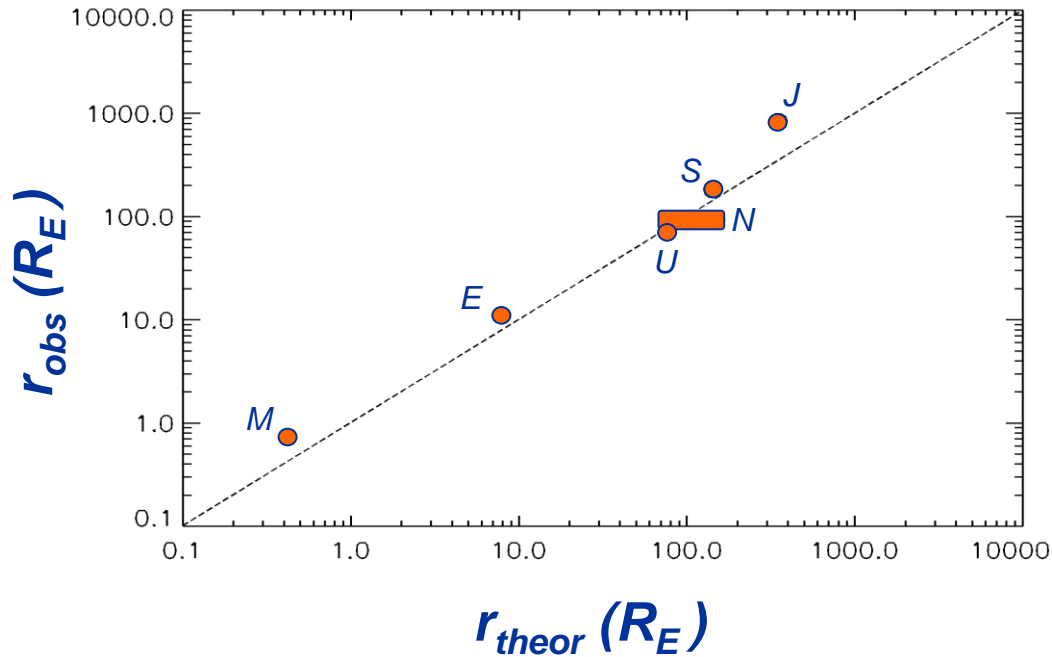
*[Blanc et al., 2005]*



$$dV = 4\pi r^2 dr$$

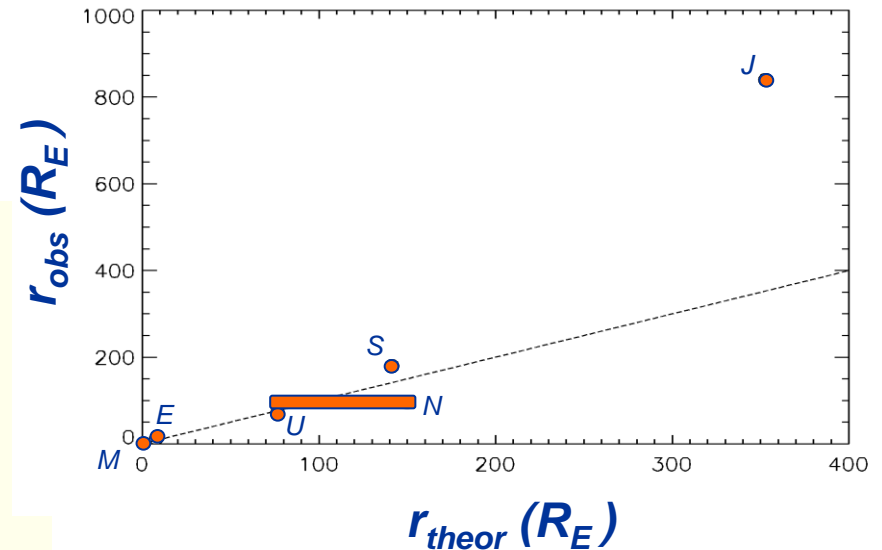
# Comparative magnetospheres

## Observed vs. theoretical standoff-distance



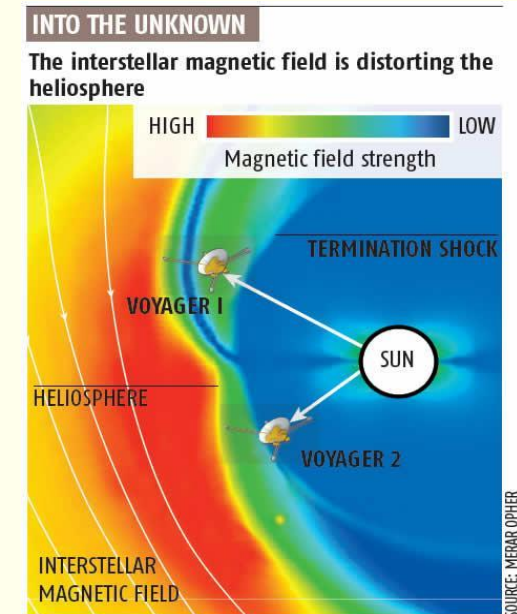
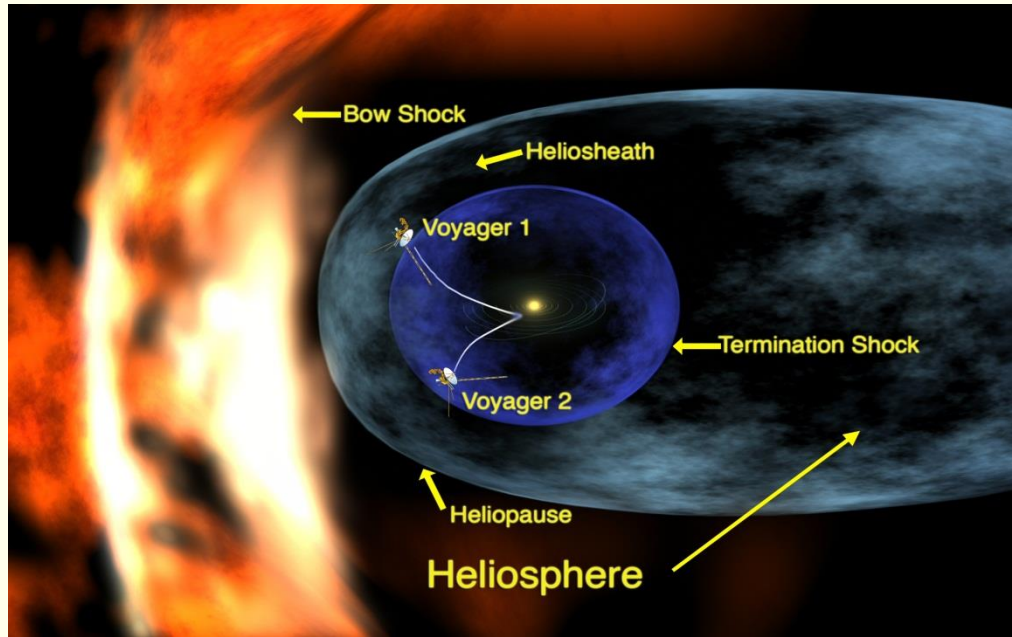
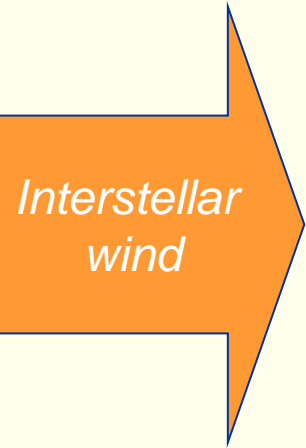
$$r_{theor} = \left( \frac{\mu_0 a}{4\pi} \right)^{1/3} \left( 2\mu_0 \rho_{SW} v_{SW}^2 \right)^{-1/6}$$

- Model reasonably valid over three orders of magnitude
- Size of Jupiter's (and maybe Saturn's) magnetosphere underestimated



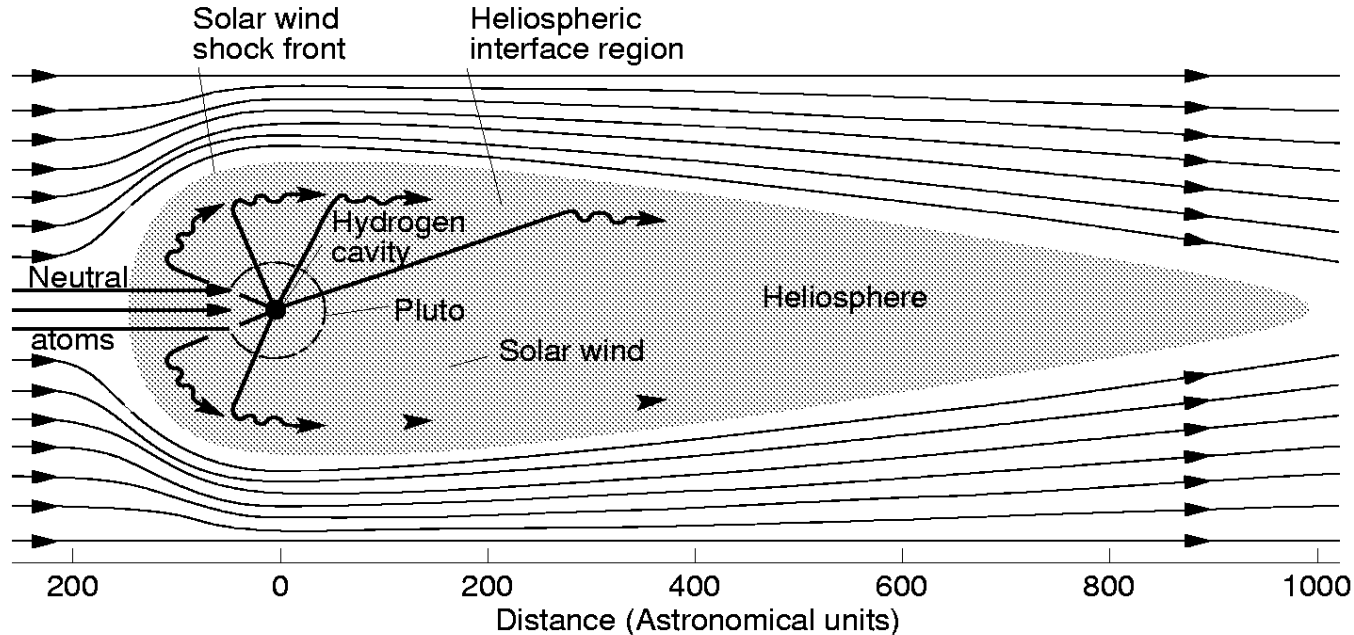
# Other other magnetospheres

## Heliosphere



[Opher, 2007]

# Heliosphere



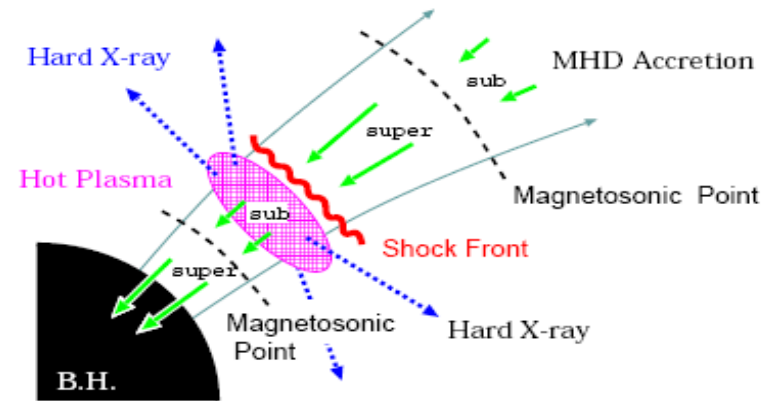
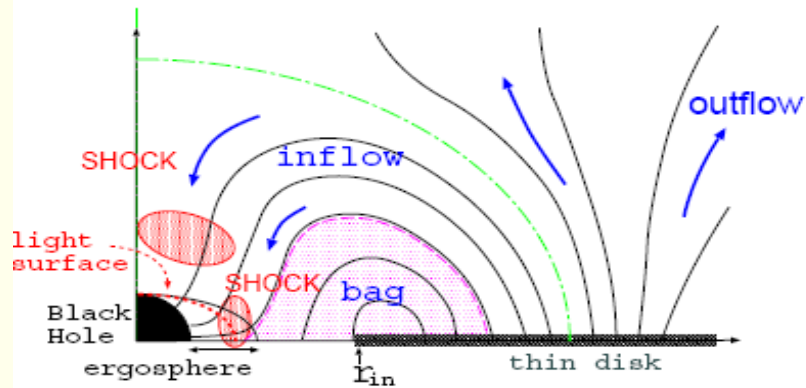
- Reaches approximately 100 AU into space ( $=1.5 \times 10^{13}$  m)
- Voyager sonds are approaching/encountering the heliopause right now

# Other other magnetospheres

## Exotic magnetospheres

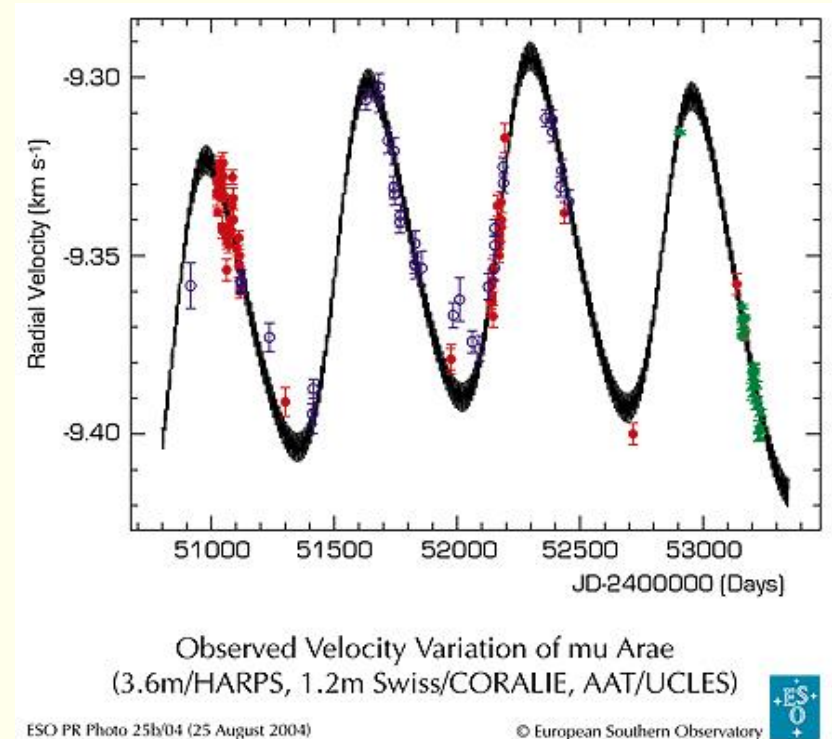
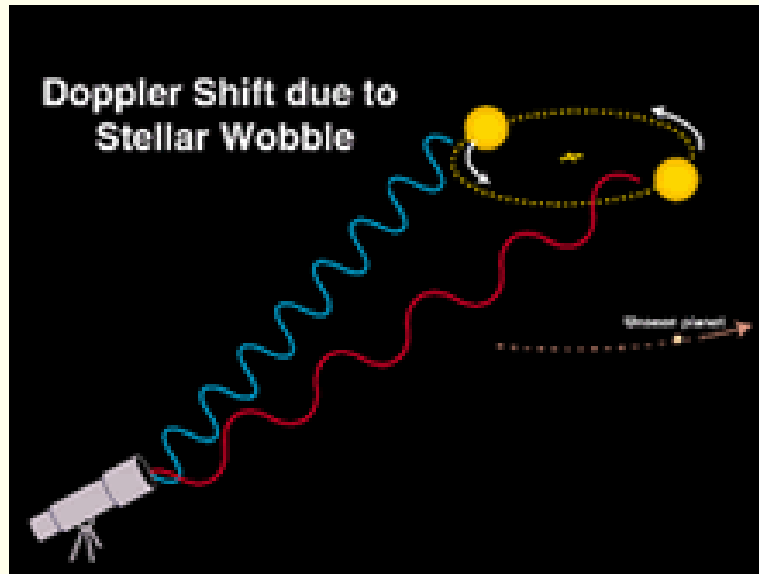
“Black Hole Magnetosphere” =

$$\text{Loop (bag) + Disk-BH (inflow) + BH (Disk) - } r_{\infty} \text{ (outflow)}$$



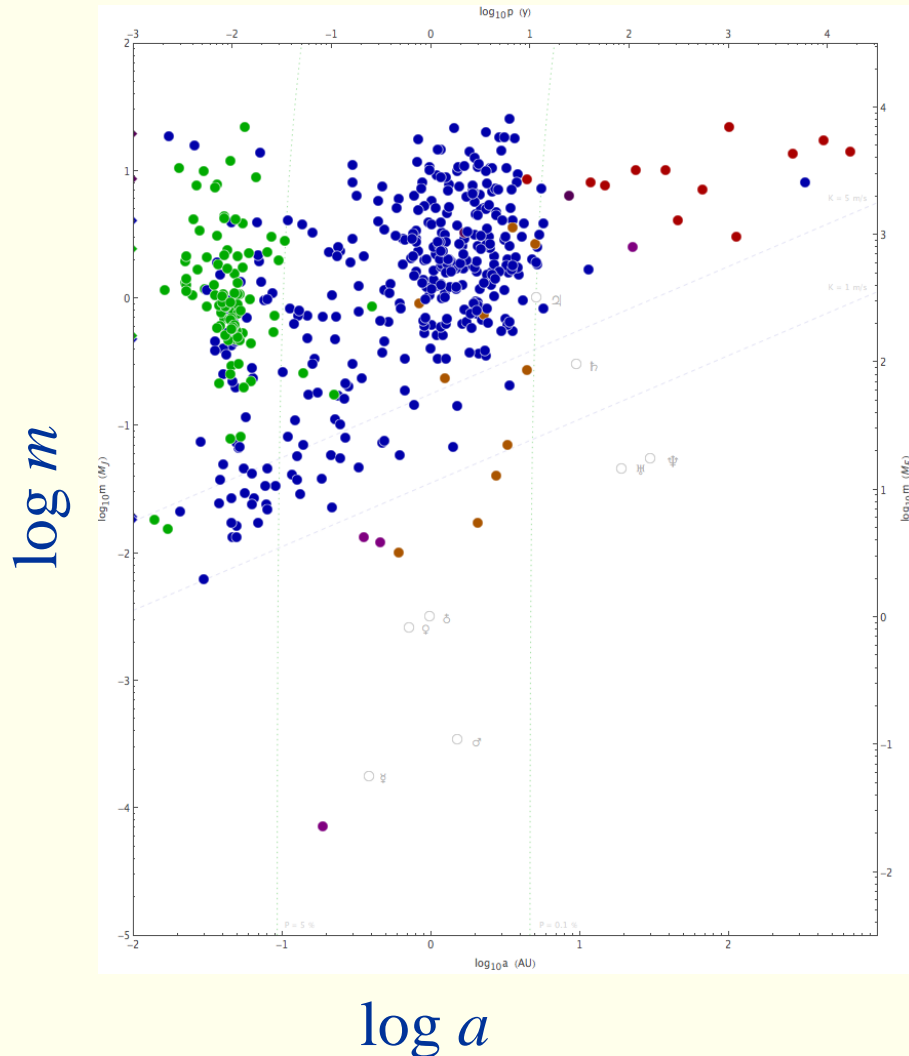


# Exoplanets



Mostly detected by doppler shifts in starlight, or by dimming of the emitted starlight during transit of planet.

# Magnetospheres of exoplanets



- 1958 exoplanets found up to September 24, 2015
- Nothing is known about their atmospheres, ionospheres or magnetospheres
- Can possibly be detected by
  - radio emissions from auroral activity or from radiation belts
  - spectroscopy when the magnetosphere is in front of its sun

# The aurora



# The aurora



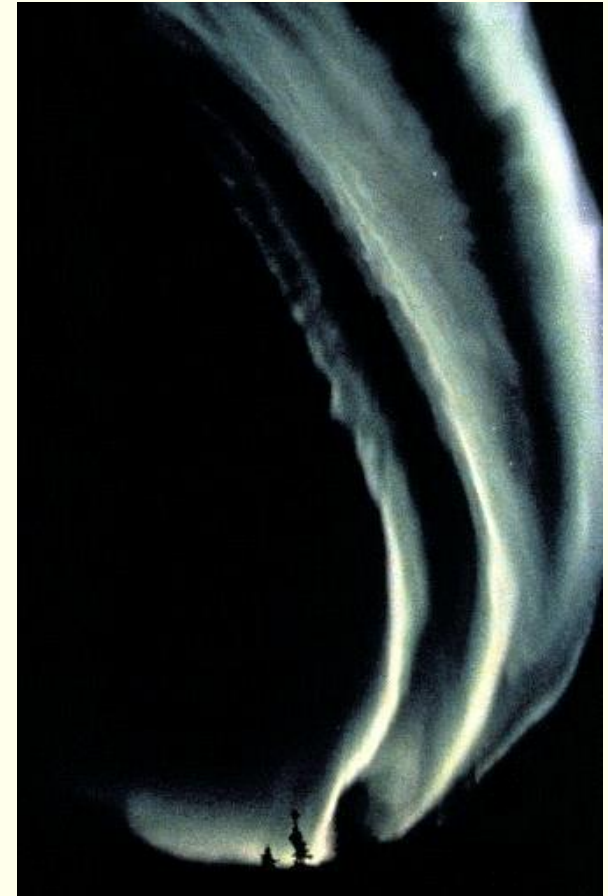
# The aurora



# The aurora



# Homogenous auroral arcs



# Rays, curtains

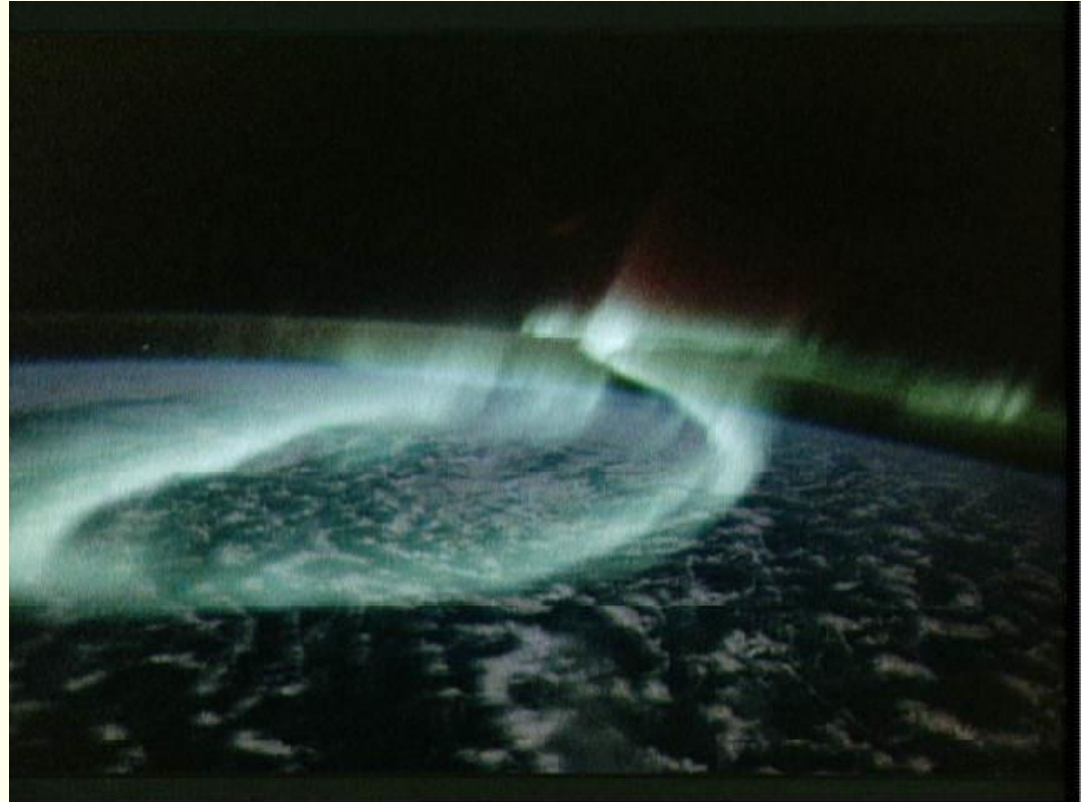
Rays are formed in the direction of the local magnetic field.



Drapes develop from homogenous arcs, often when they increase in intensity.



# Auroral spirals

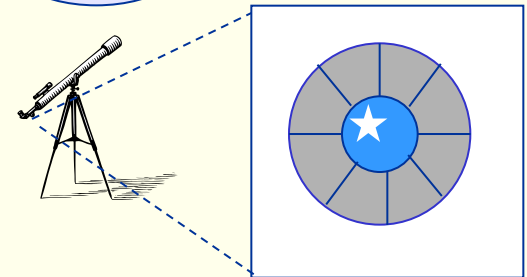
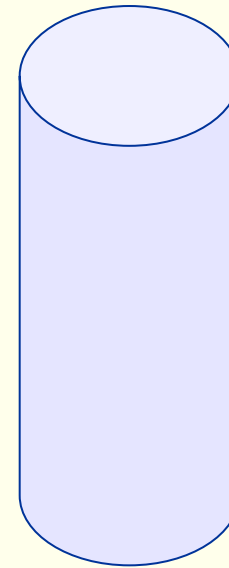


Develop when arcs become unstable

# Auroral corona



Geometric effect of perspective when you look towards magnetic zenith.  
Compare the figure.



# Aurora - altitude



Foto from International Space Station

# Early notions



Woodcut from Böhmen 1570.



Anders Celsius documented that compass needles were strongly affected during auroral activity in 1733.

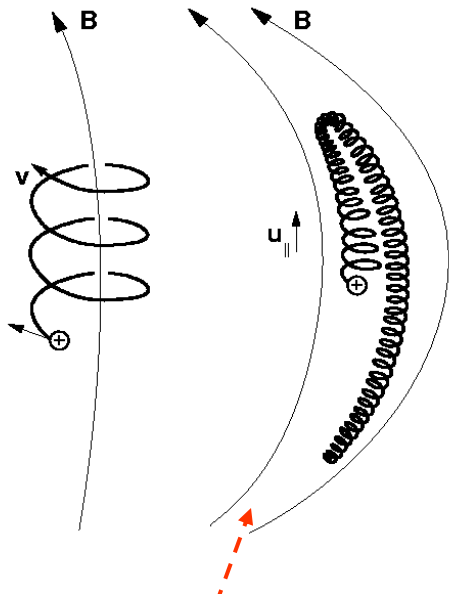


# ***What causes the aurora?***

# Particle motion in geomagnetic field

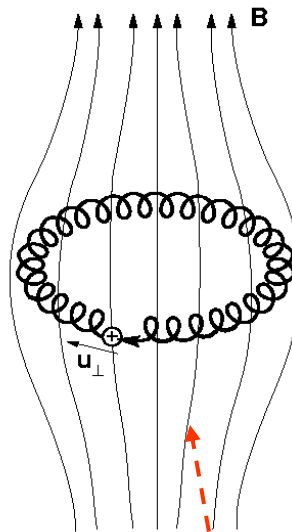
## longitudinal oscillation

### gyration

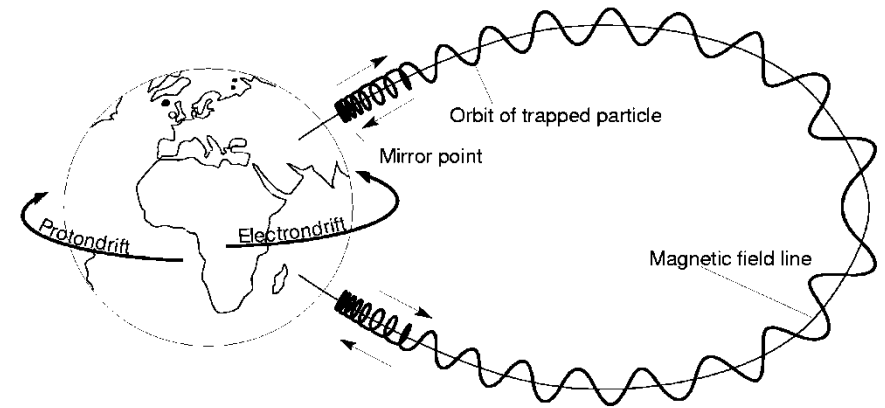


Magnetic mirror

### azimuthal drift



grad B drift



# Magnetic mirror

$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{\text{turn}} = B / \sin^2 \alpha$$

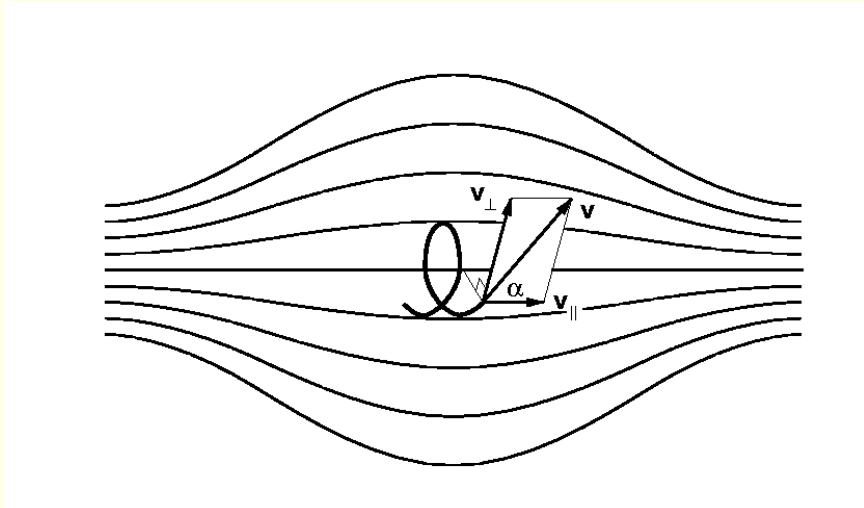
If maximal B-field is  $B_{\text{max}}$  a particle with pitch angle  $\alpha$  can only be turned around if

$$B_{\text{turn}} = B / \sin^2 \alpha \leq B_{\text{max}} \rightarrow$$

$$\alpha > \alpha_{lc} = \arcsin \sqrt{B / B_{\text{max}}}$$

Particles in  
loss cone :

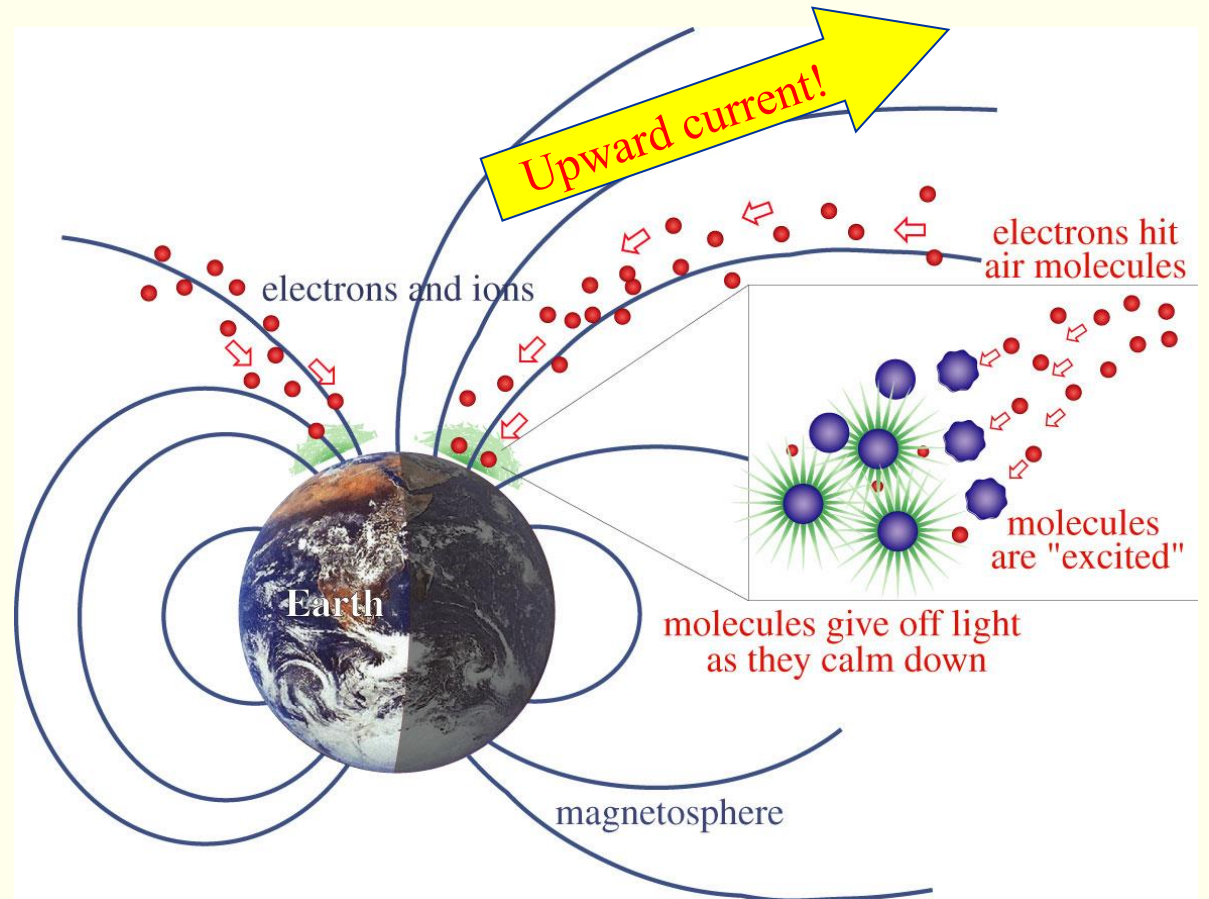
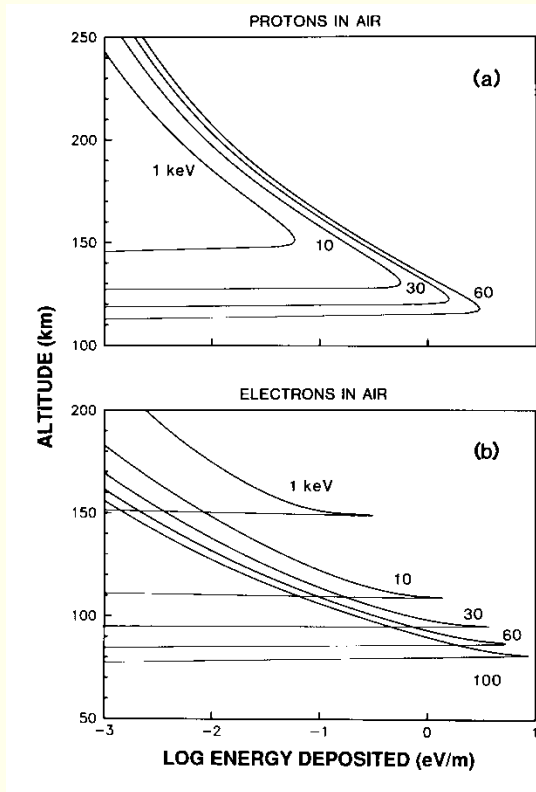
$$\alpha < \alpha_{lc}$$



The magnetic moment  $\mu$  is an *adiabatic invariant*.

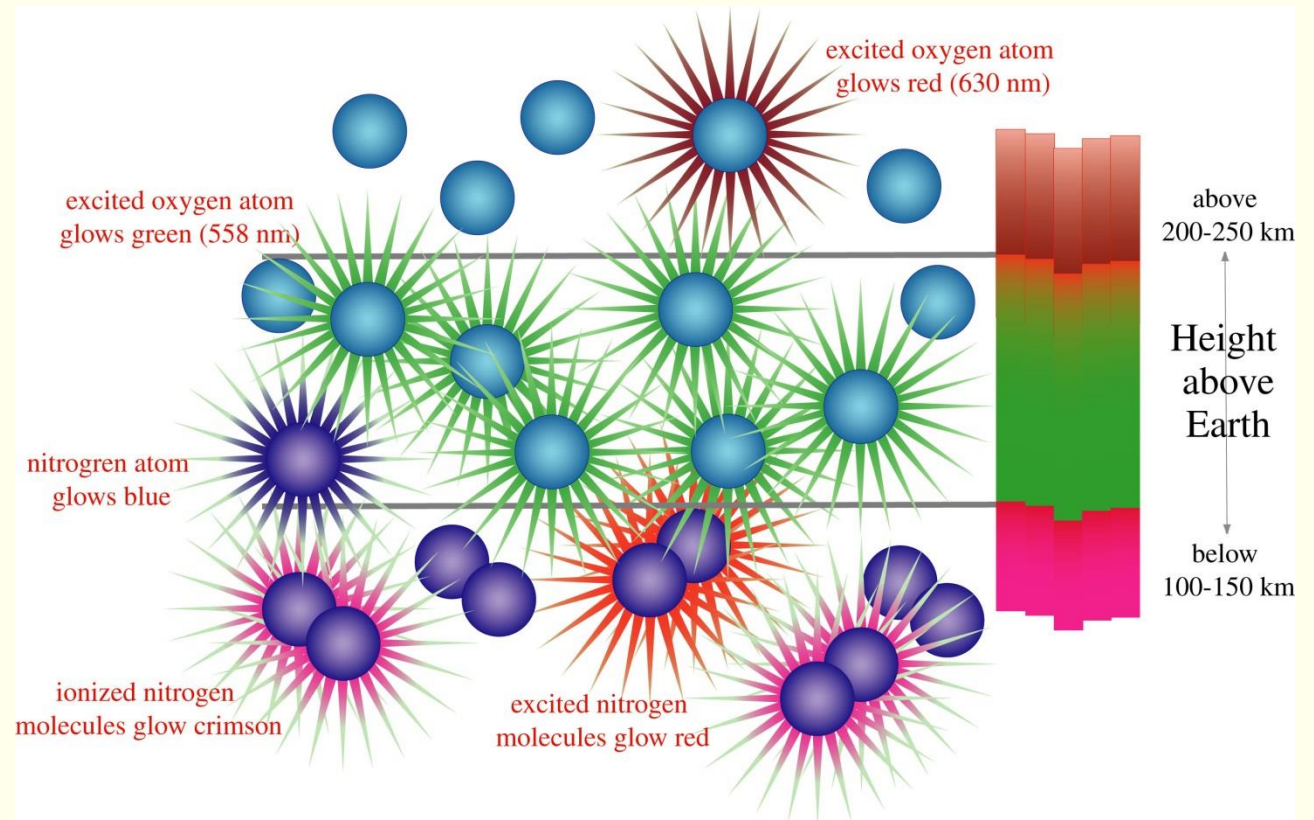
$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$

# Collisions - emissions

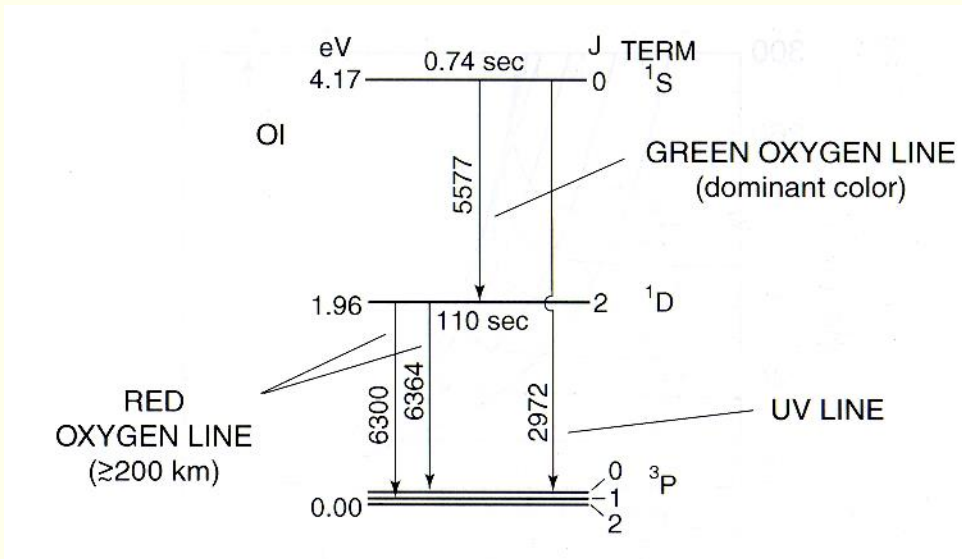




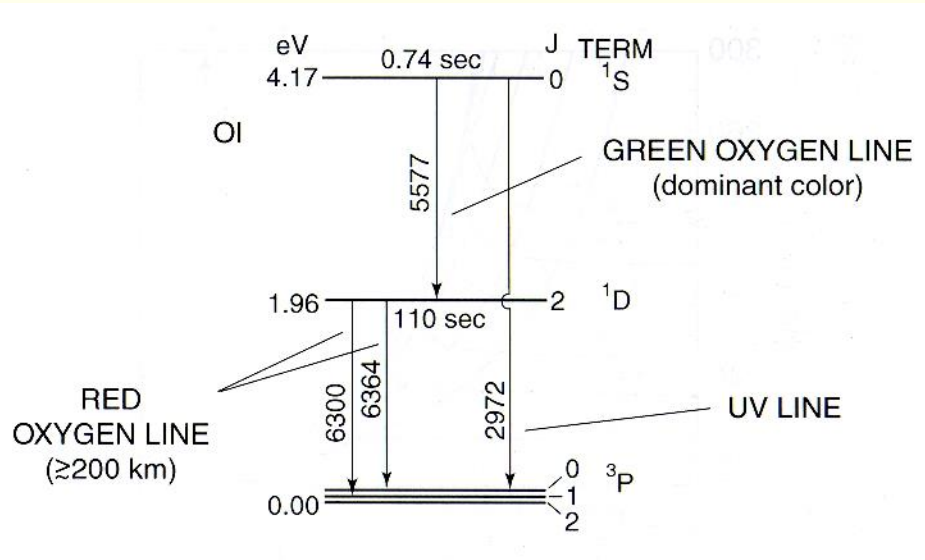
# Emissions



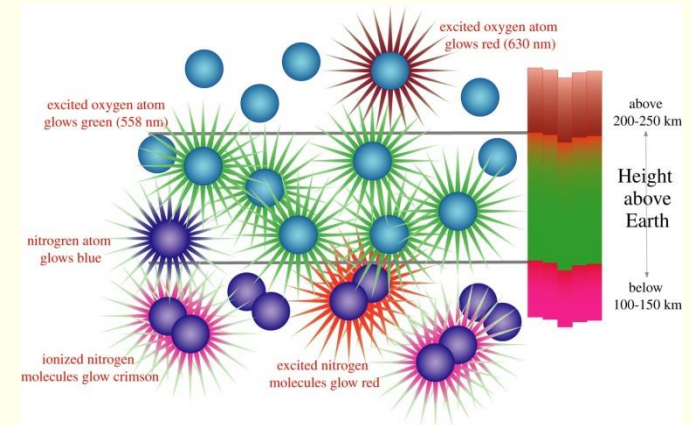
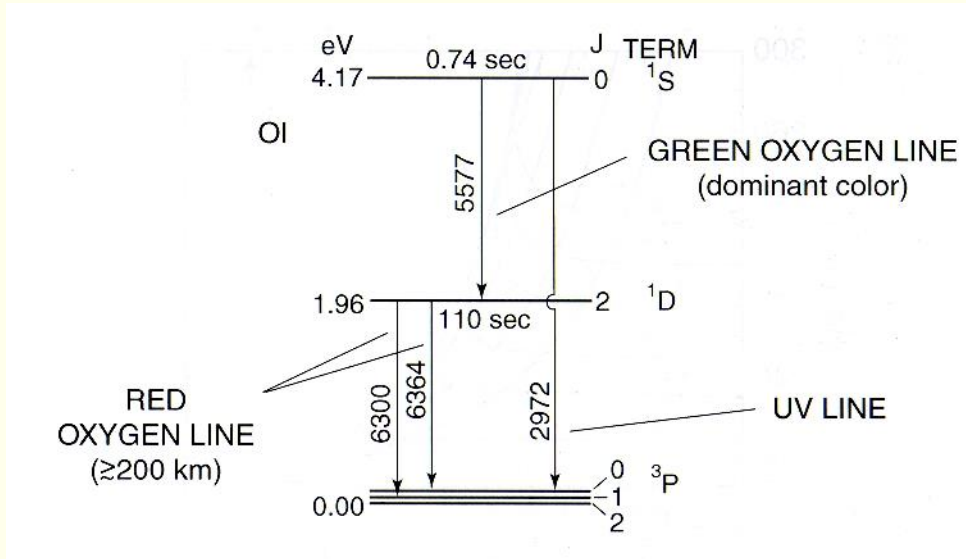
# Oxygen emissions



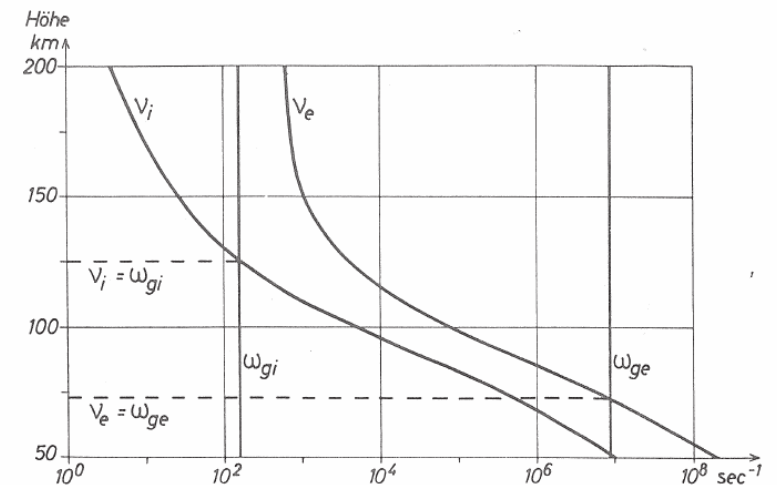
# Why is there no red emissions at lower altitude?



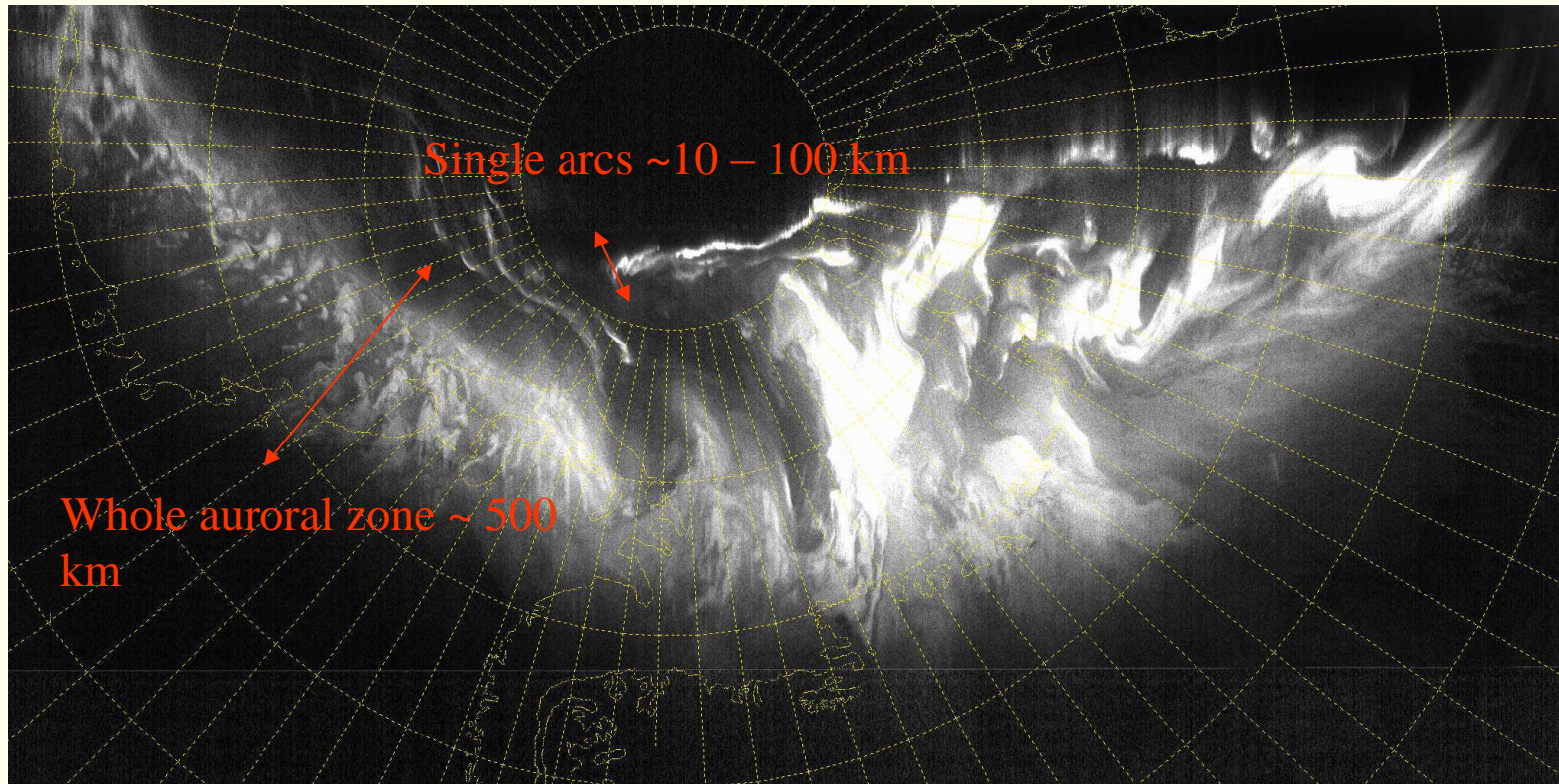
# Oxygen emissions



The red emission line is suppressed by collisions at lower altitudes due to its long transition time. (When an excited atom collides with another atom, it is de-excited without any emission.)



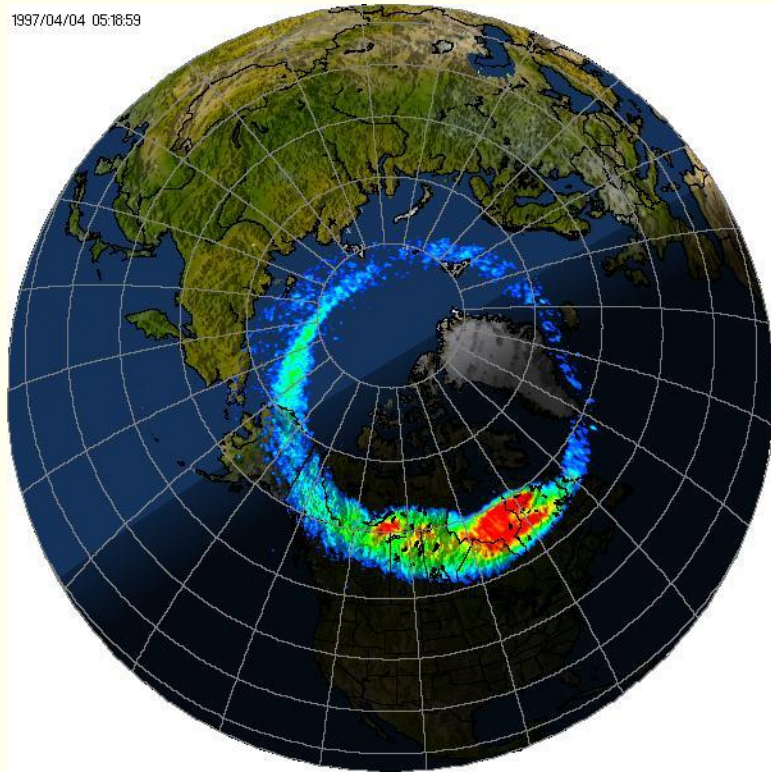
# Larger scales



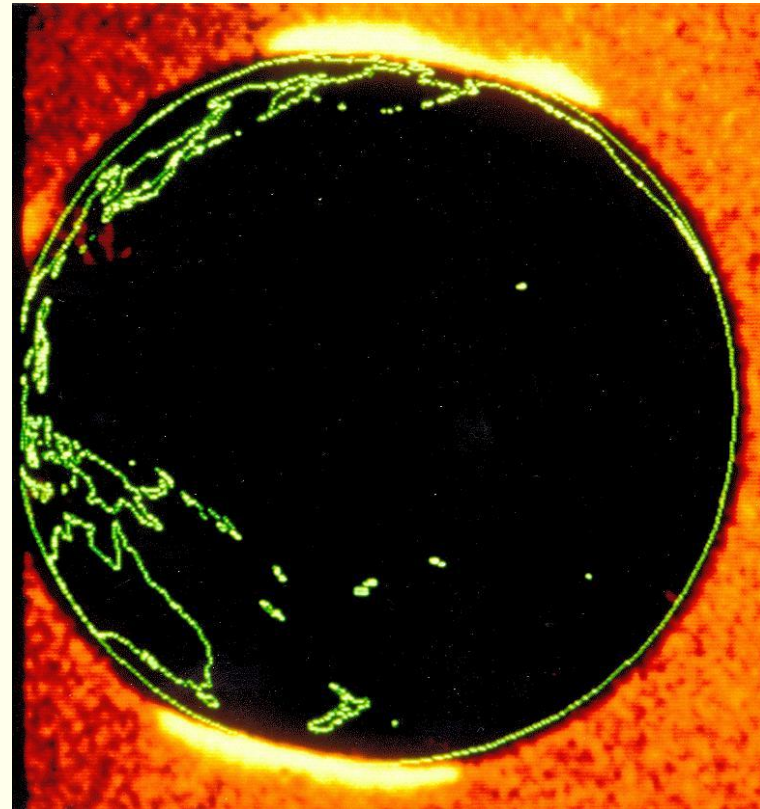
*Foto från DMSP-satelliten*

# Auroral ovals

1997/04/04 05:18:59



Polar

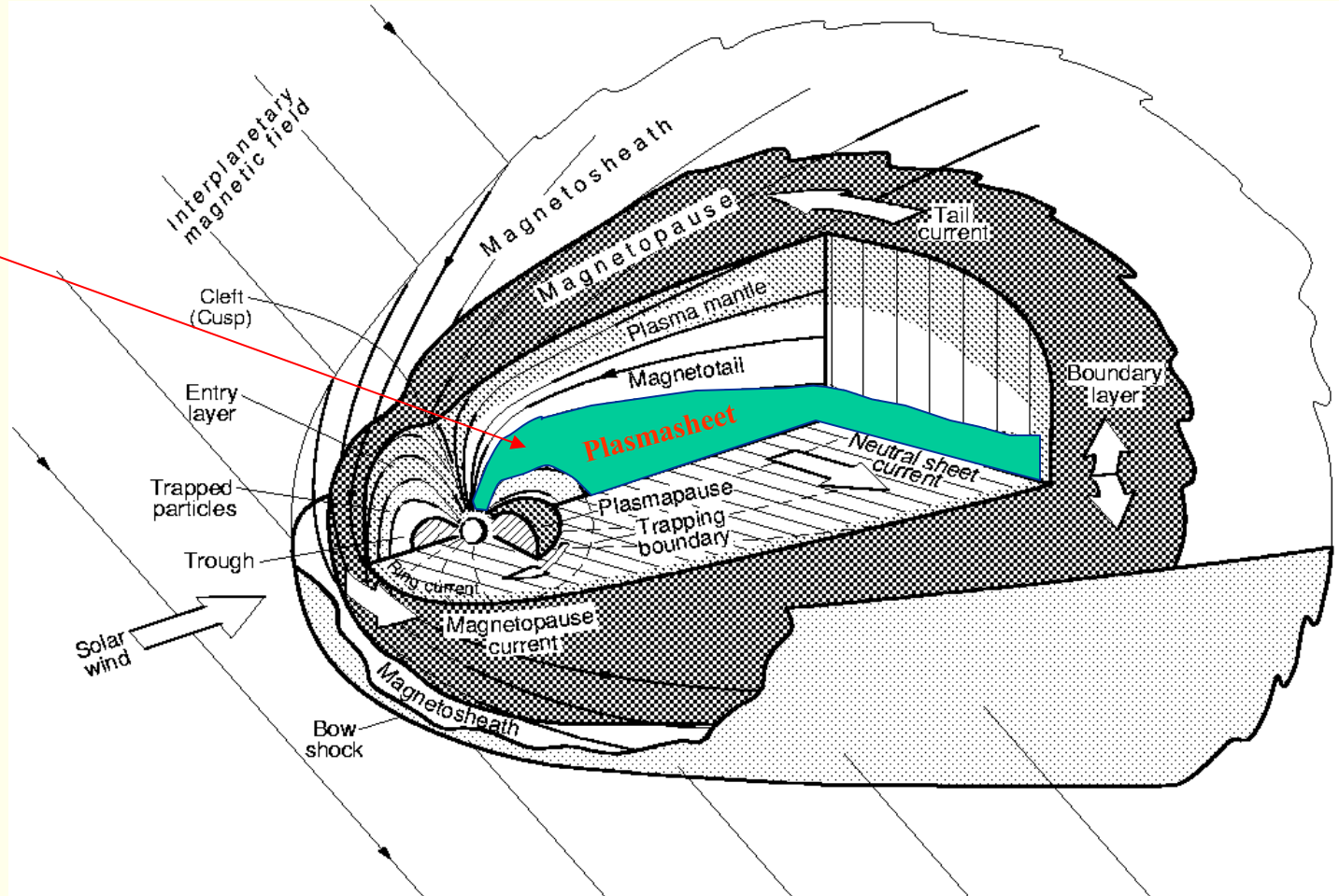


Dynamics Explorer

# The auroral oval is the projection of the plasmasheet onto the atmosphere

## Mystery!

The particles in the plasmasheet do not have high enough energy to create aurora visible to the eye.



# Magnetic mirror

$mv^2/2$  constant (energy conservation) →

$$\frac{\sin^2 \alpha}{B} = \text{konst}$$

particle turns when  $\alpha = 90^\circ$  →

$$B_{\text{turn}} = B / \sin^2 \alpha$$

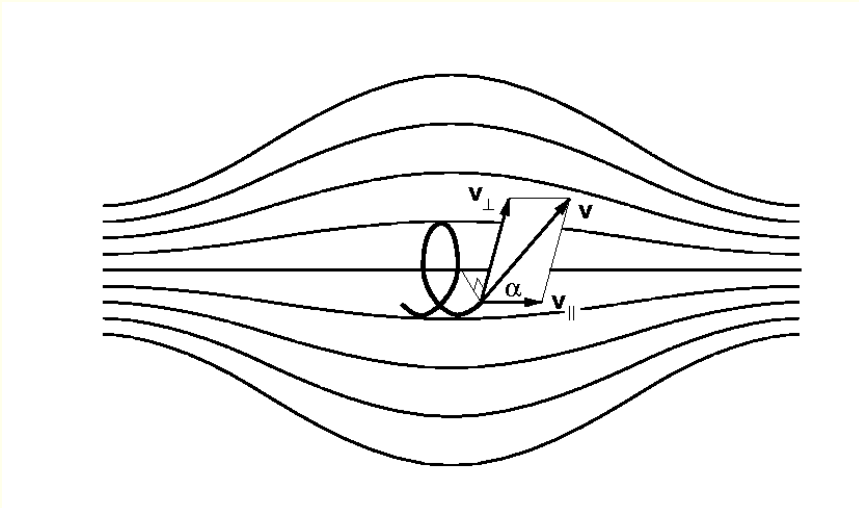
If maximal B-field is  $B_{\text{max}}$  a particle with pitch angle  $\alpha$  can only be turned around if

$$B_{\text{turn}} = B / \sin^2 \alpha \leq B_{\text{max}} \rightarrow$$

$$\alpha > \alpha_{fl} = \arcsin \sqrt{B / B_{\text{max}}}$$

Particles in  
loss cone :

$$\alpha < \alpha_{fl}$$

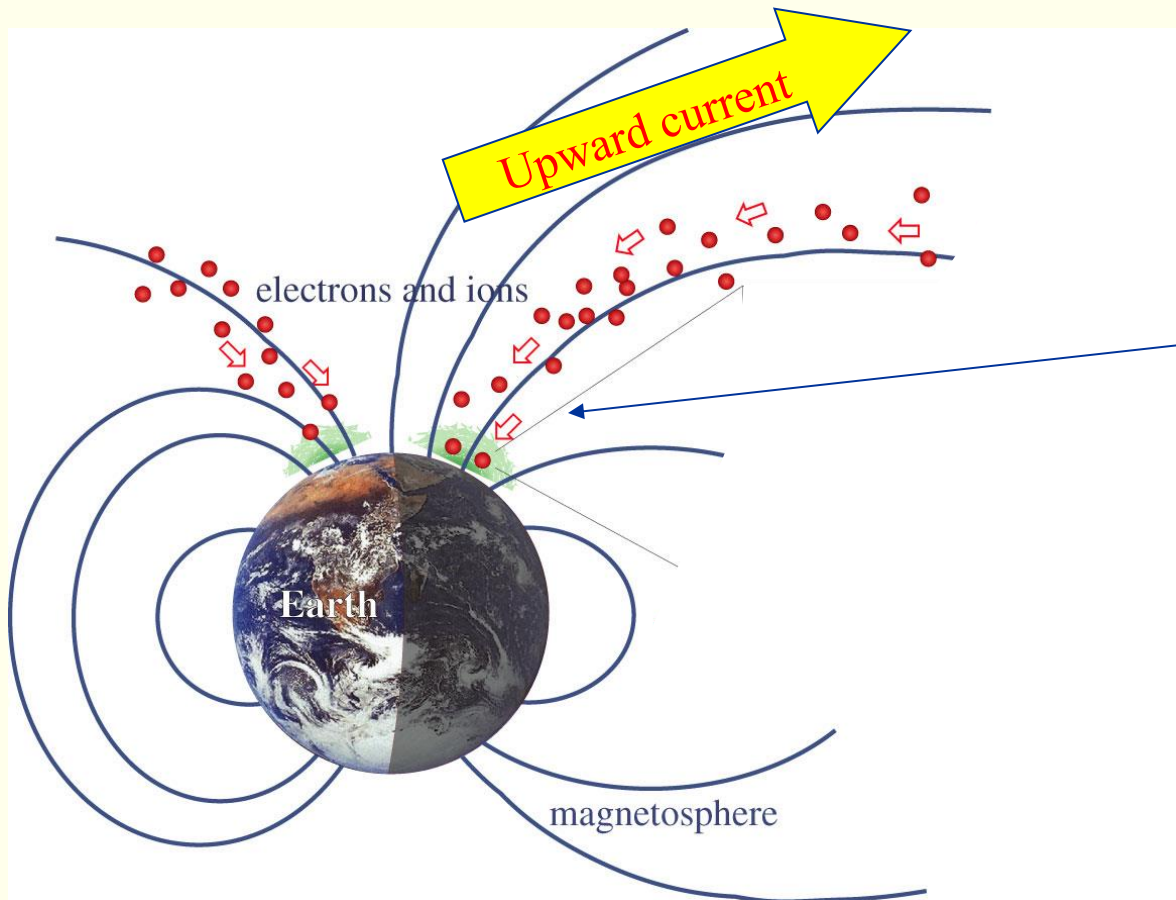


The magnetic moment  $\mu$  is an *adiabatic invariant*.

$$\mu = \frac{mv_{\perp}^2}{2B} = \frac{mv^2 \sin^2 \alpha}{2B}$$



# Why particle acceleration?



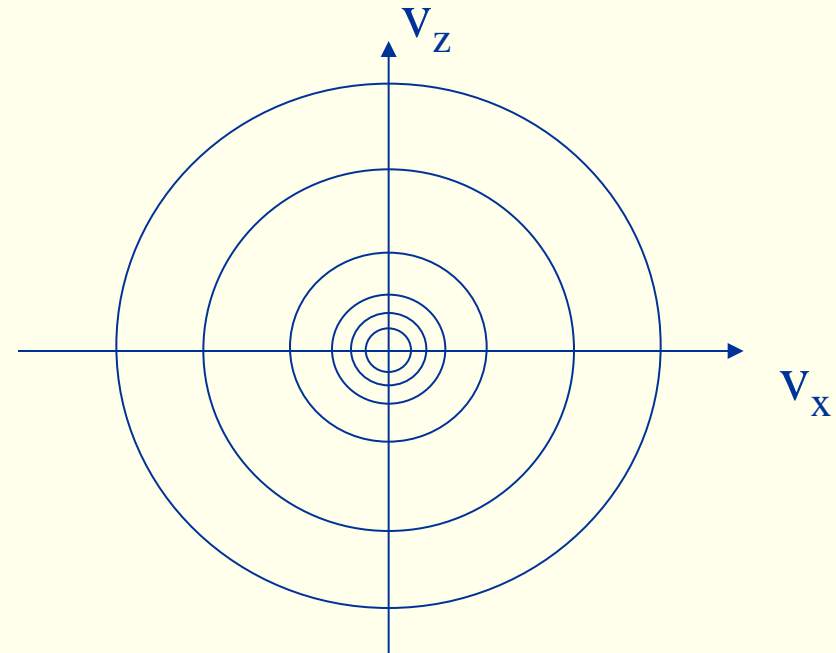
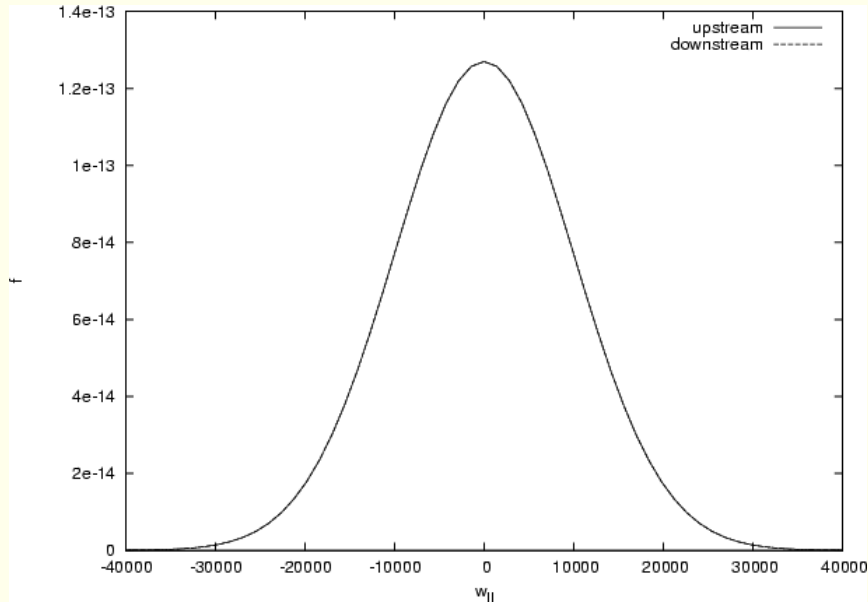
- The magnetosphere often seems to act as a current generator.
- The lower down you are on the field line, the more particles have been reflected by the magnetic mirror.
- At low altitudes there are not enough electrons to carry the current.

# Why particle acceleration?



- Electrons are accelerated downwards by upward E-field.
- This increases the pitch-angle of the electrons, and more electrons can reach the ionosphere, where the current can be closed.

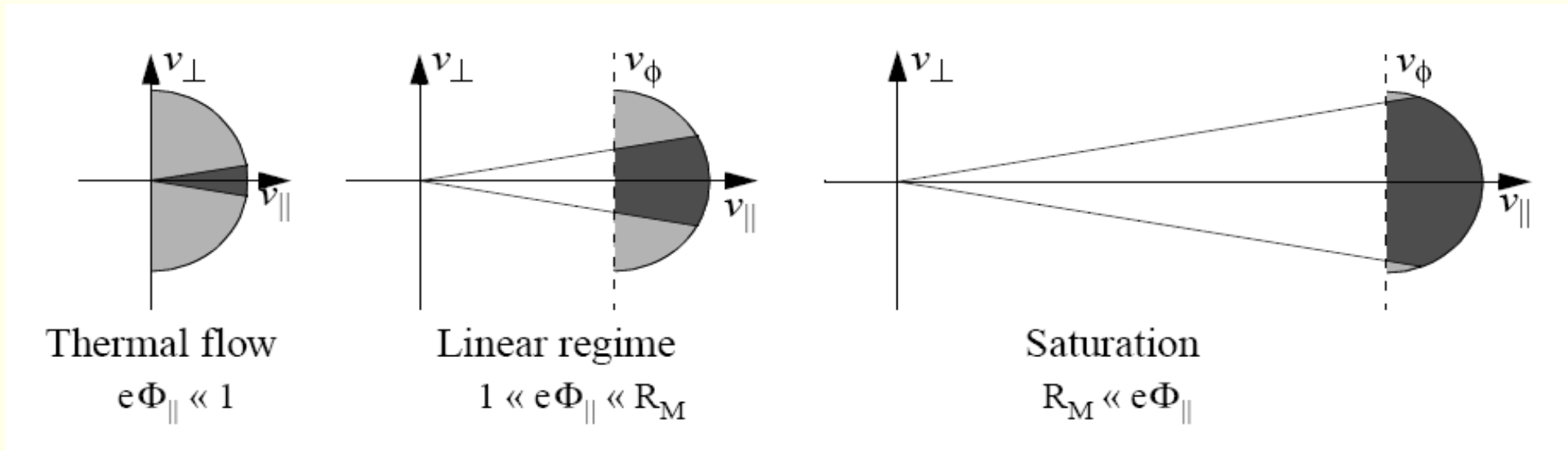
# Distribution function



Example:  
Maxwellian  
distribution

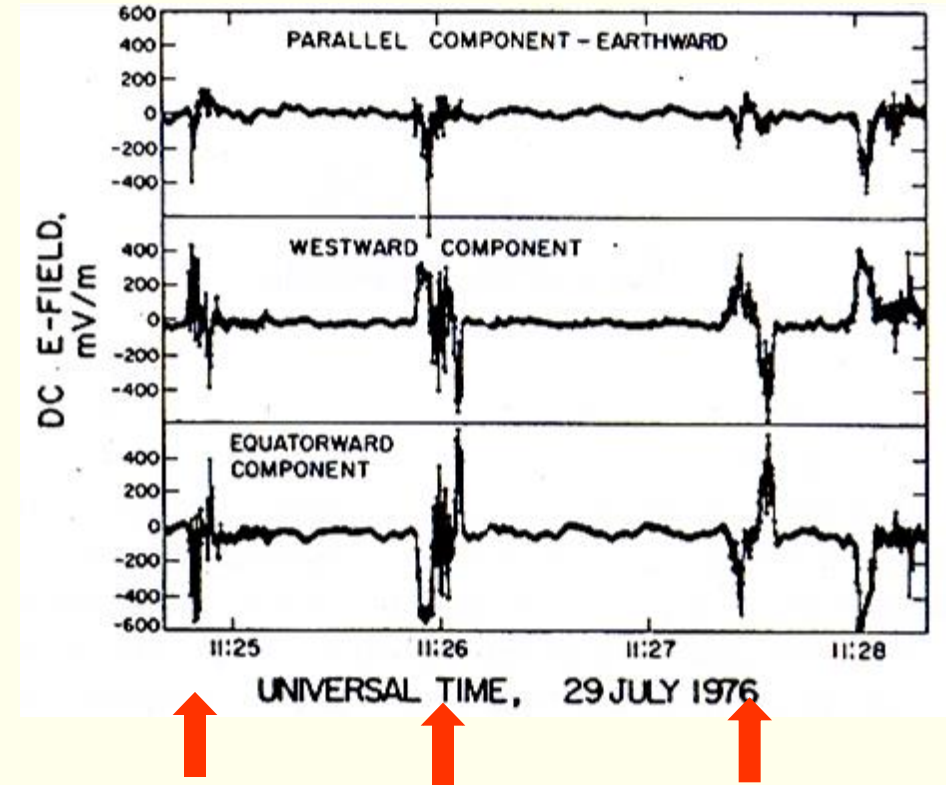
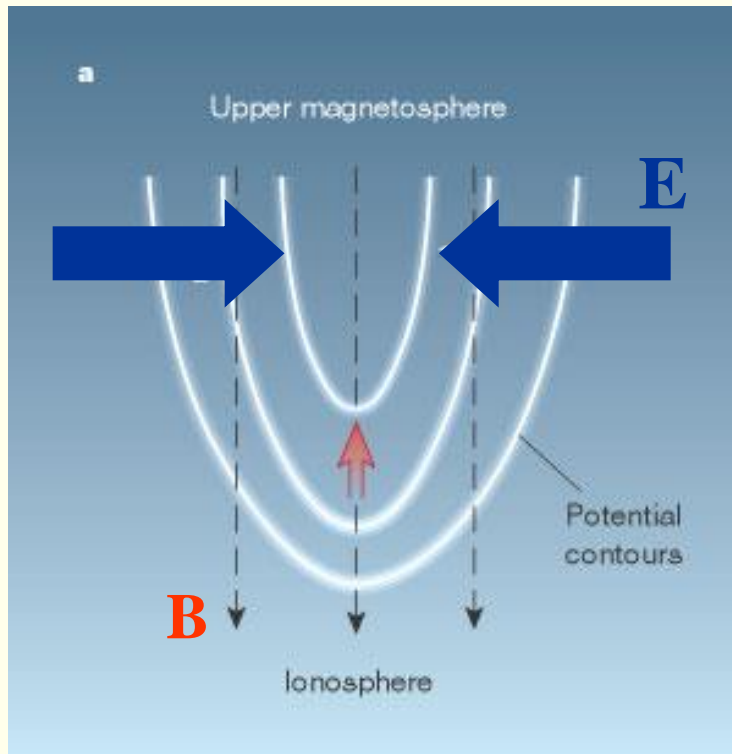
$$f = \frac{n}{\sqrt{(2\pi RT)^3}} \exp\left(-\frac{m(v_x^2 + v_y^2 + v_z^2)}{2kT}\right)$$

# Why particle acceleration?



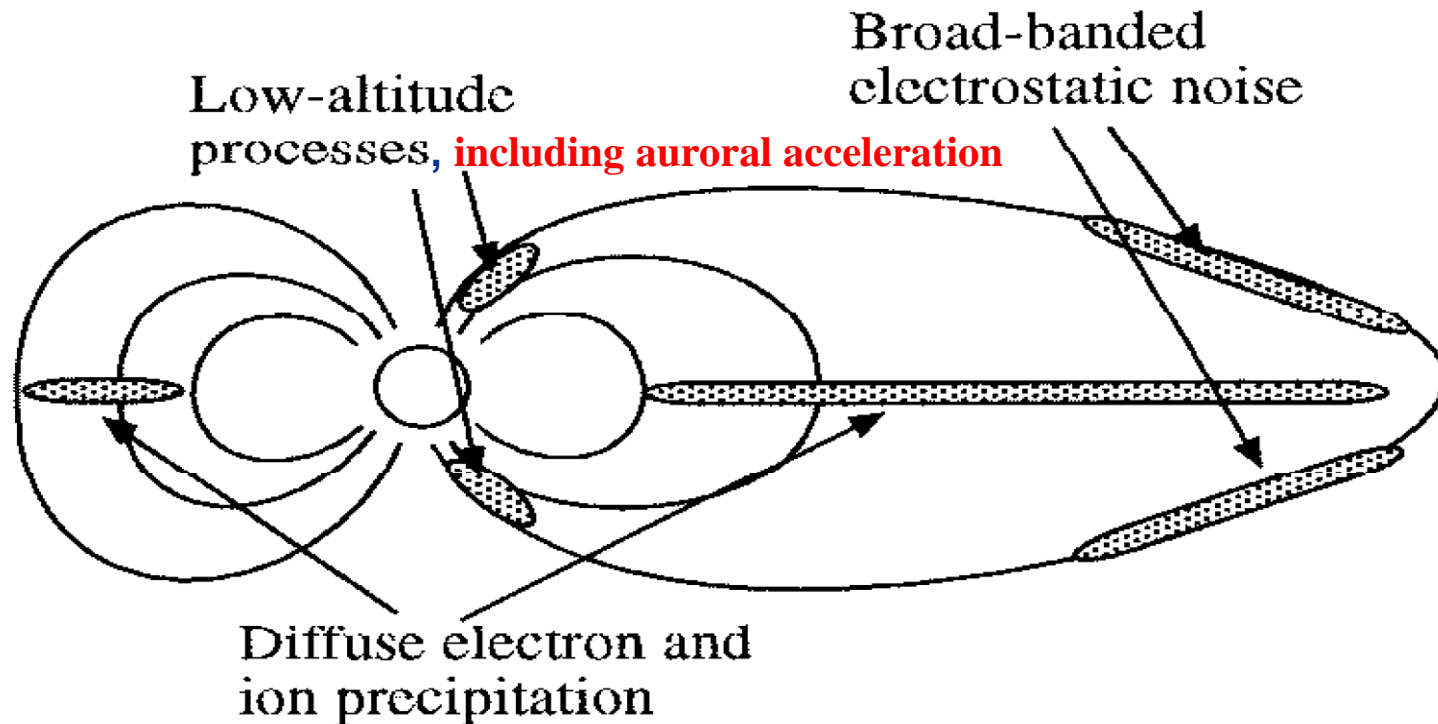
- Electrons are accelerated downwards by upward E-field.
- This increases the pitch-angle of the electrons, and more electrons can reach the ionosphere, where the current can be closed.

# Satellite signatures of U potential



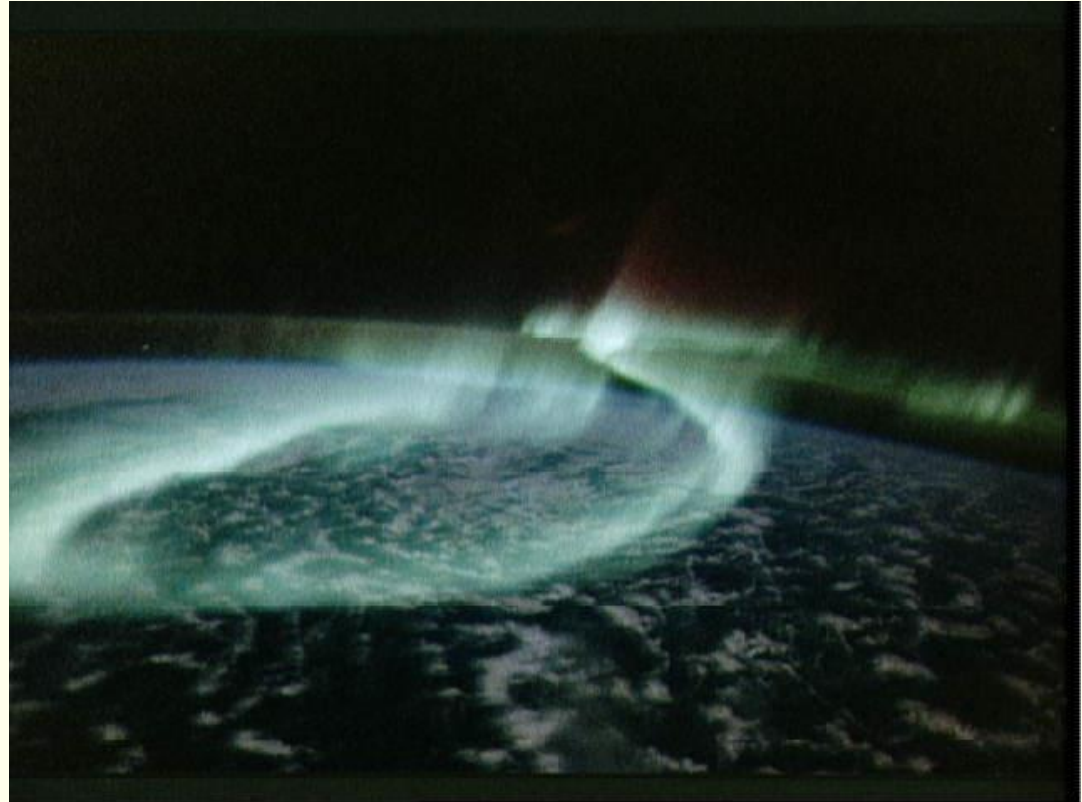
Measurements made by the ISEE satellite  
(Mozer et al., 1977)

# Acceleration regions



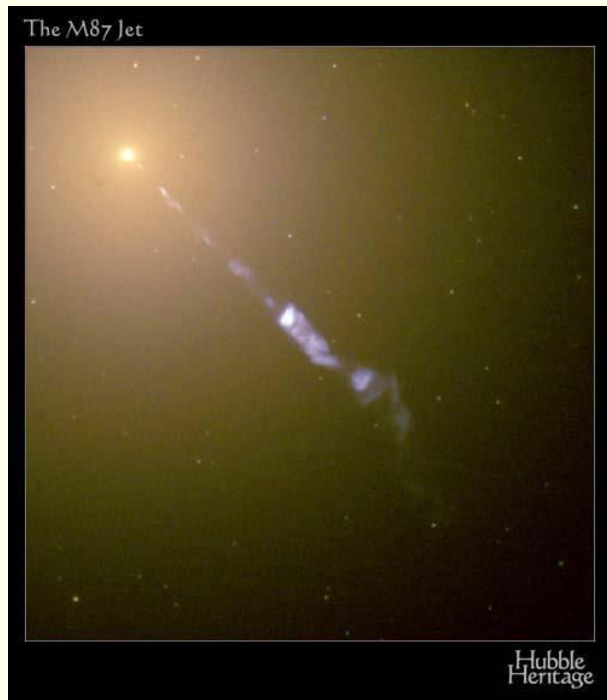
Auroral acceleration region typically situated at altitude of 1-3  $R_E$

# Auroral spirals

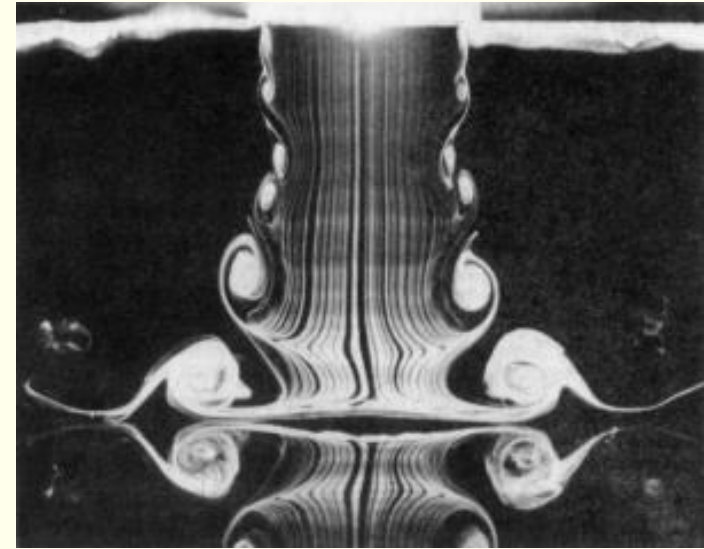


Develop when arcs become unstable

# Kelvin-Helmholtz- instability – a general phenomenon



Extragalactic jet (M87)



Aero- and fluid dynamics

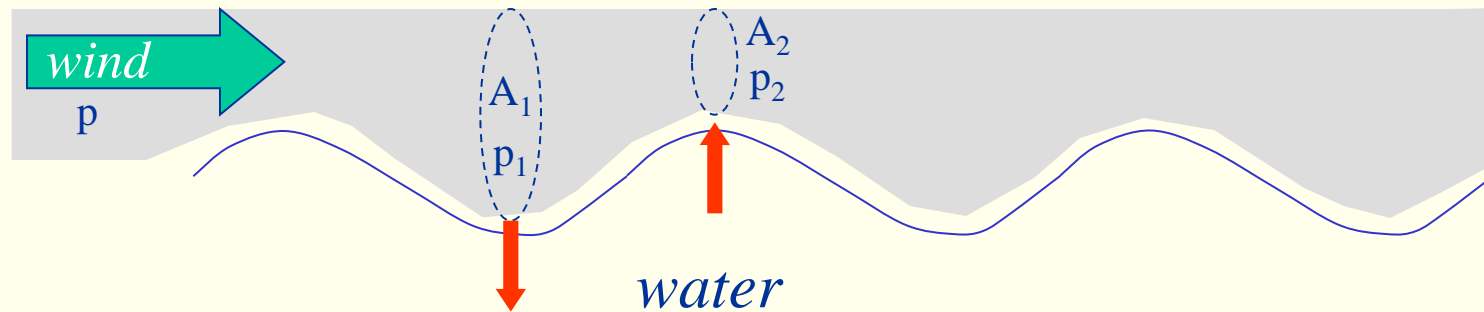


Cluds



# Kelvin-Helmholtz instability

## Example: water waves



Continuity equation:

$$A_1 v_1 = A_2 v_2$$

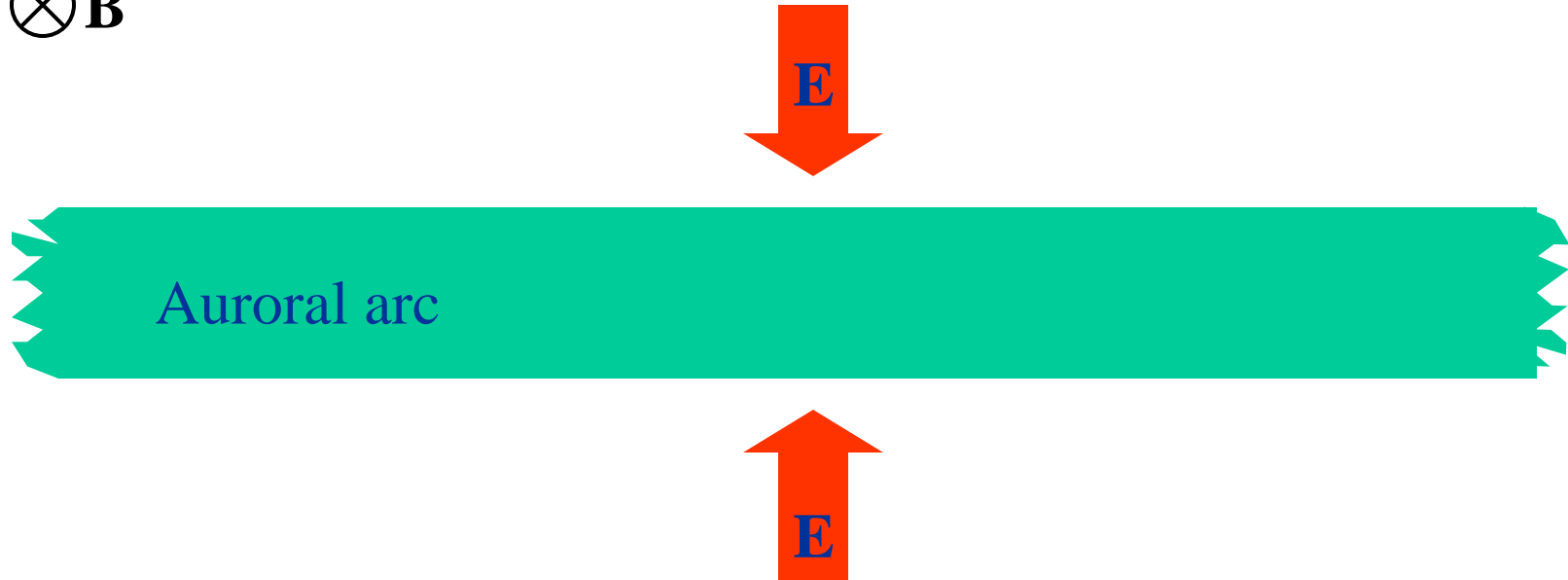
Bernoulli's equation:

$$p_1 + \rho v_1^2 = p_2 + \rho v_2^2 = \text{const.}$$

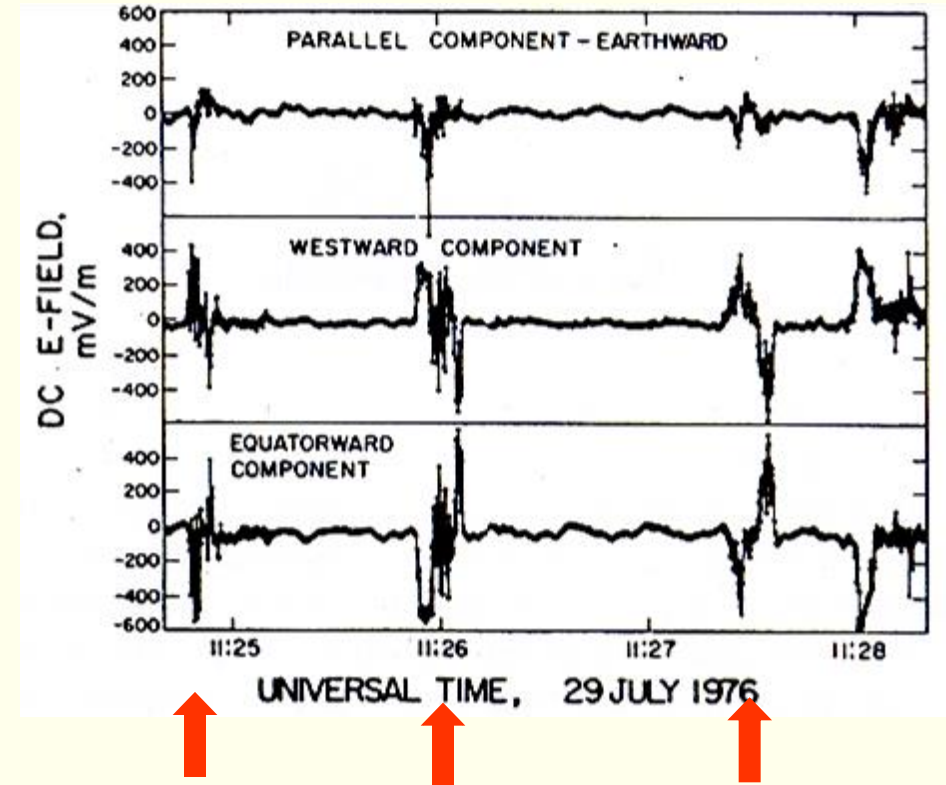
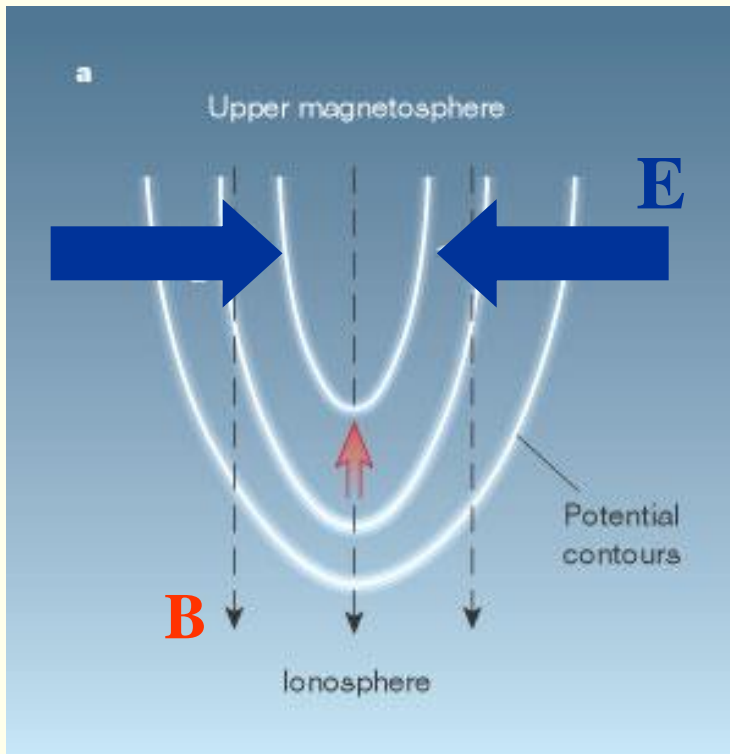
$$\therefore p_1 > p > p_2$$

# Spirals – Kelvin-Helmholtz instability

$\otimes$  B

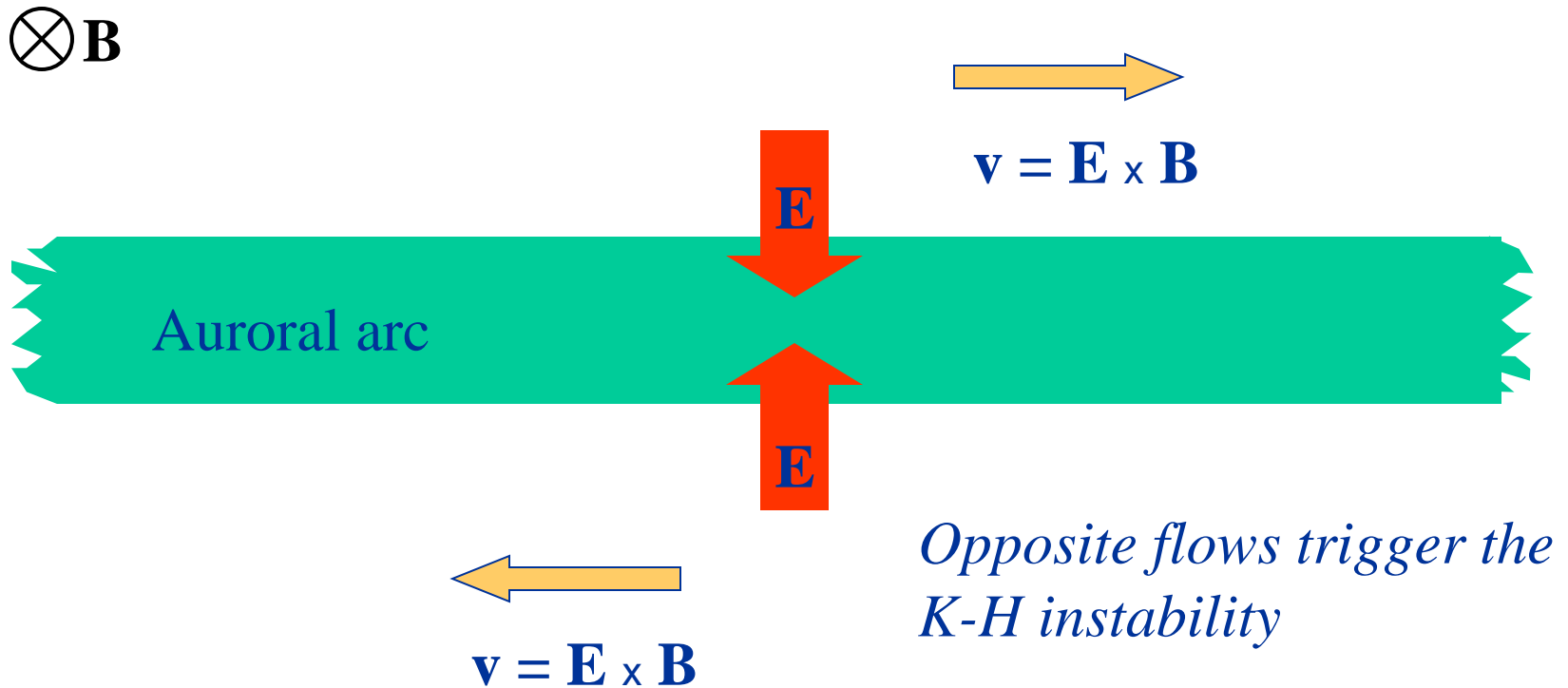


# Satellite signatures of U potential

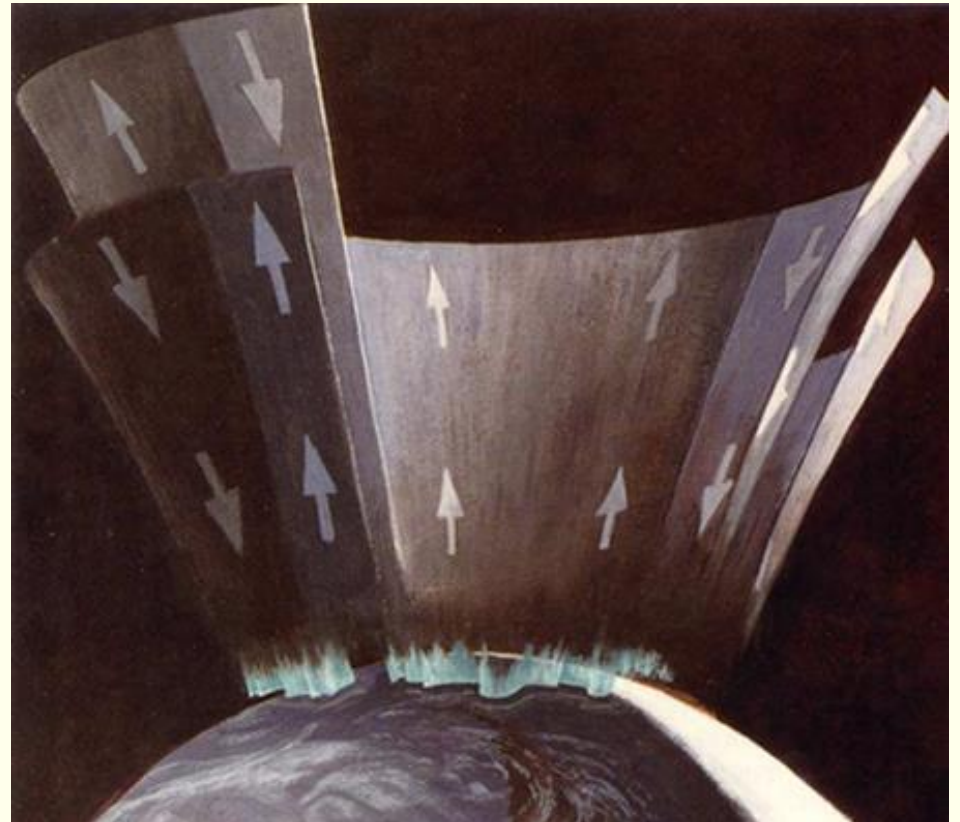
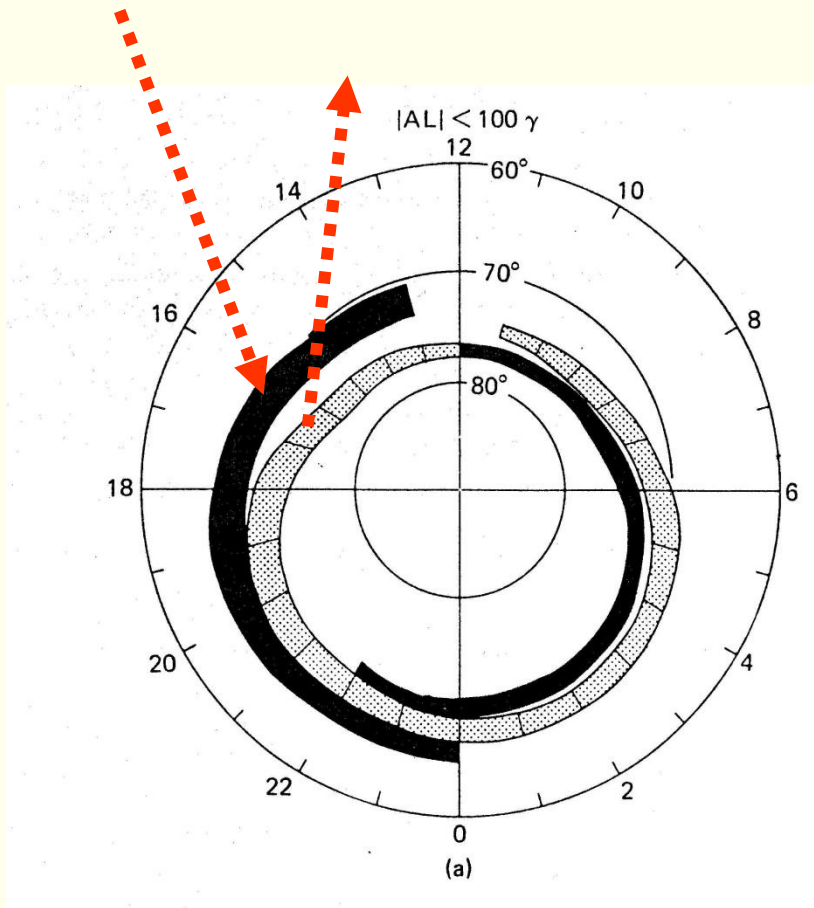


Measurements made by the ISEE satellite  
(Mozer et al., 1977)

# Spirals – Kelvin-Helmholz instability



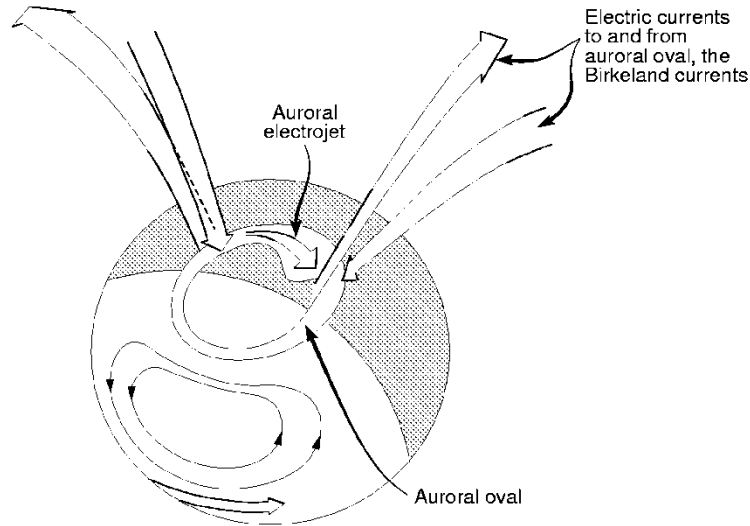
# Birkeland currents in the auroral oval



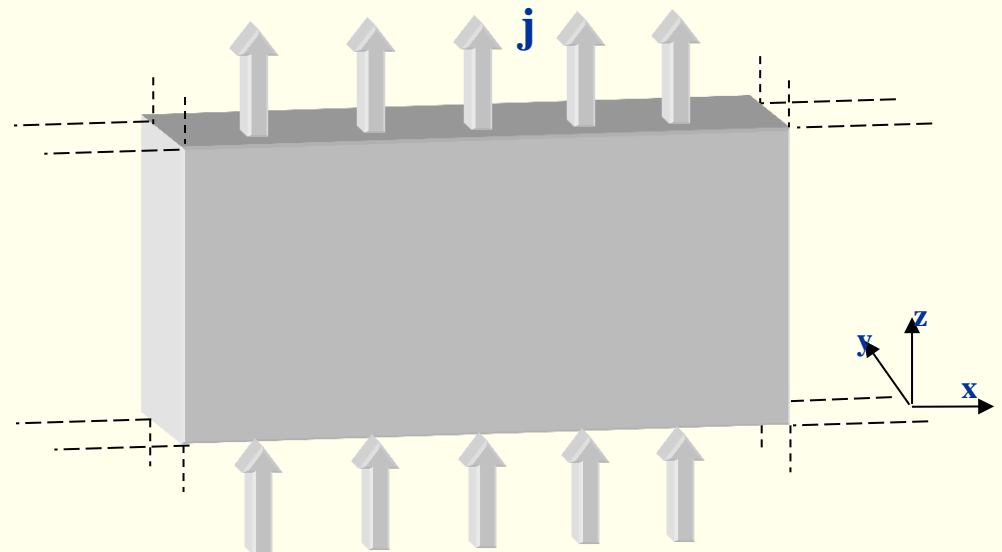
# How can you measure currents in space?



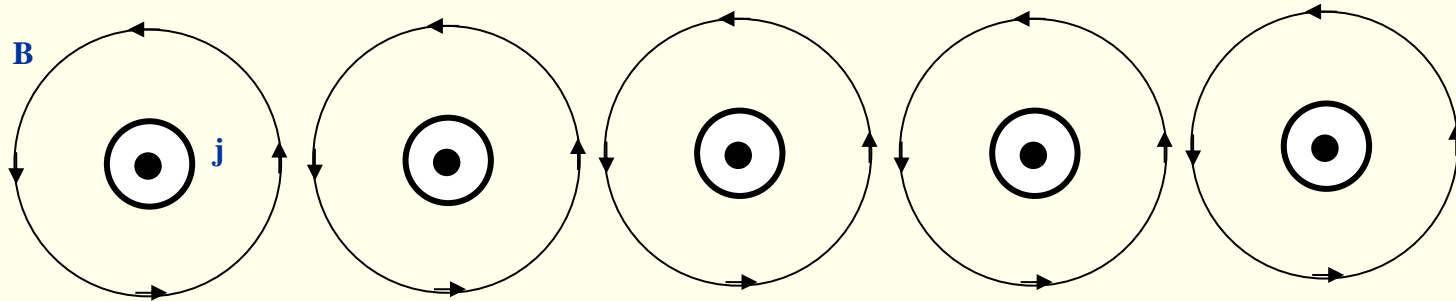
# Current sheet approximation



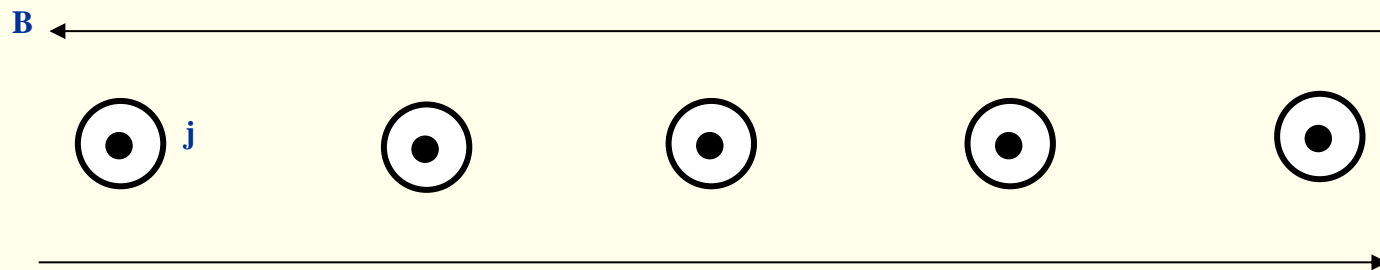
Approximate currents by thin current sheets with infinite size in the  $x$ - and  $z$ -directions.



# Current sheet approximation



What will the magnetic field around such a current configuration be? Start by approximating with line currents to get a qualitative picture.



The closer you place the line currents, the more the magnetic fields between the line currents will cancel