



ROYAL INSTITUTE
OF TECHNOLOGY

DH2323 DGI16

INTRODUCTION TO COMPUTER GRAPHICS AND INTERACTION

RASTERISED RENDERING

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The Rendering Equation

$$L_o(\mathbf{x}, \omega_o, \lambda, t) = L_e(\mathbf{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o, \lambda, t) L_i(\mathbf{x}, \omega_i, \lambda, t) (\omega_i \cdot \mathbf{n}) d\omega_i$$

Emitted radiance BRDF Account for angle w.r.t. light
 ↓ ↓ ↓
 ↑ ↑ ↑
 Incoming radiance

Describes:

Total amount of light emitted from a point \mathbf{x} along a specific viewing direction

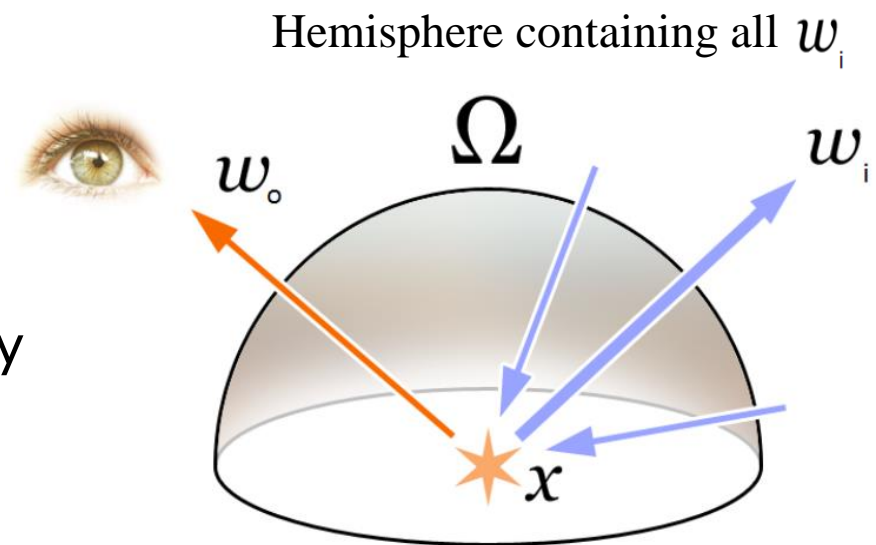
Given:

Incoming light function

BRDF

Basis:

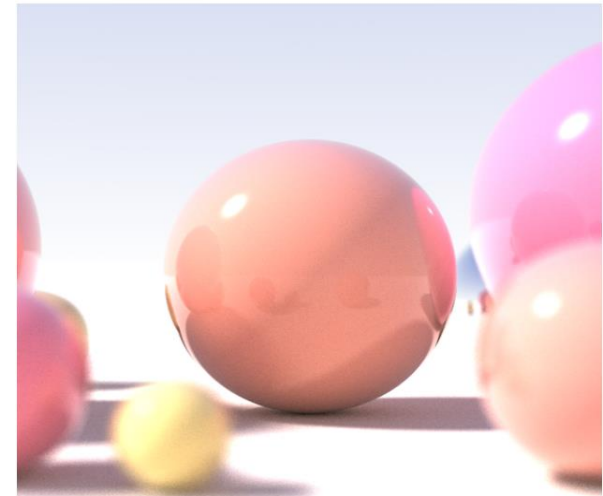
Law of conservation of energy



Global Illumination

Ray tracing:

- Good for specular
- Bad for diffuse



Radiosity:

- Good for diffuse
- Bad for specular



Hybrid techniques

Caustics

- Curved regions of bright reflected or refracted light



Sub-surface scattering

- Light bouncing around inside material before exiting



Ray tracing

Pixel order rendering technique

- Trace at least one ray through each image pixel
- Maintains primitives in geometric scene model
- Queries this for each ray
- Determine which primitive is visible for each pixel

Geometry queries can have high cost

Rasterisation

Scanline: object order based

Fragments

- Data for single pixel
- Frame buffer

Handle occlusion using depth buffer

- Later details (more specifically, *fragments*) overwrite earlier ones if closer to camera

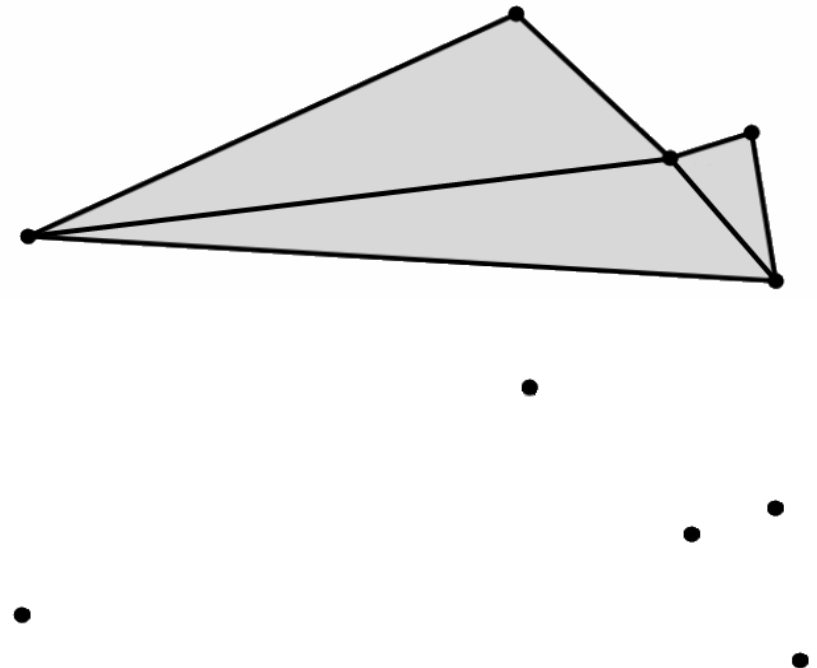
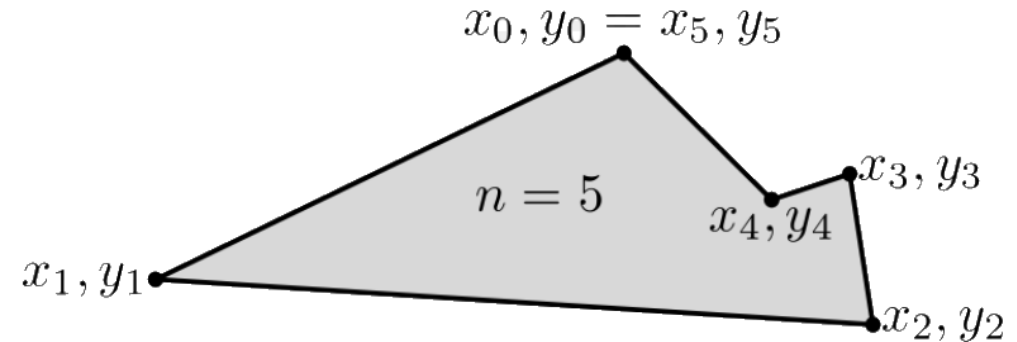
Shade based on vertices and interpolate

- See lighting and shading lecture

Rasterisation

Process of converting geometry into a raster image (series of pixels)

- 3D scene converted into 2D image
- Polygons
- ...composed of *triangles*
- ...composed of *vertices*



Rasterisation

Rasteriser takes stream of vertices

Project them onto the 2D surface of the screen

Fill in the interior of the 2D triangles

Core concepts:

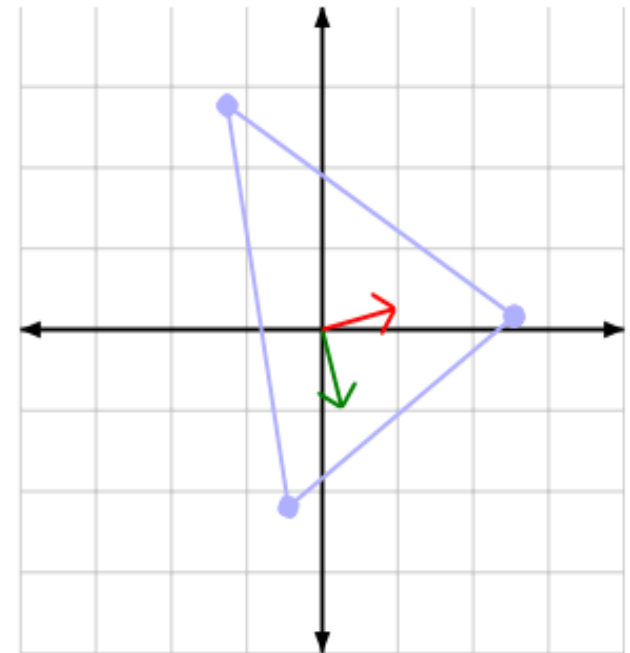
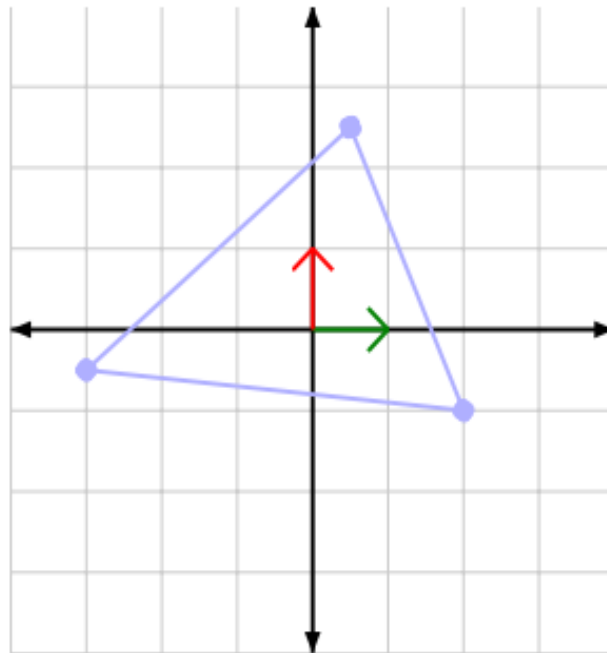
- Geometry and transformations
- Projection
- Clipping
- Scanline Conversion

Geometry Transformations

Matrix multiplication

Translation, scaling, rotation, projection

Familiar?



Transformation Stack

Stack of transforms (i.e. matrices)

- Push and pop

Position stream of input vertices

Incoming vertices transformed according to the transformation stack

Remember: local coordinate marker idea

Projection

Remove depth

- Convert 3D geometry to flat 2D representation
- Do so for each vertex of each polygon

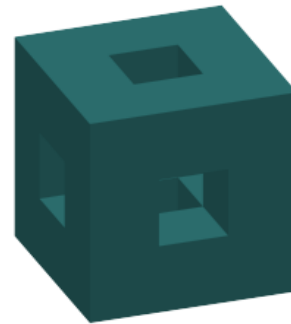
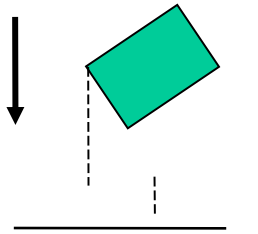
Orthographic projection

- Simply remove z coordinate
- Viewing volume is a cube

Perspective projection

- Single point of projection (focal point)
- Viewing volume is a pyramid

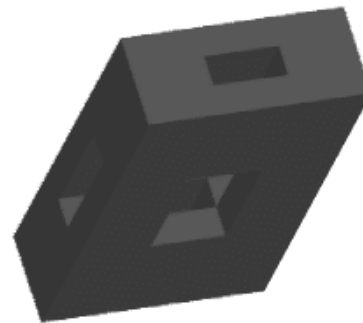
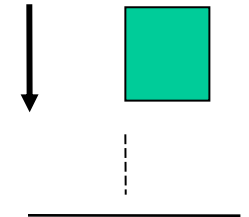
Parallel Projections



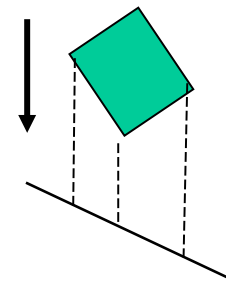
axonometric



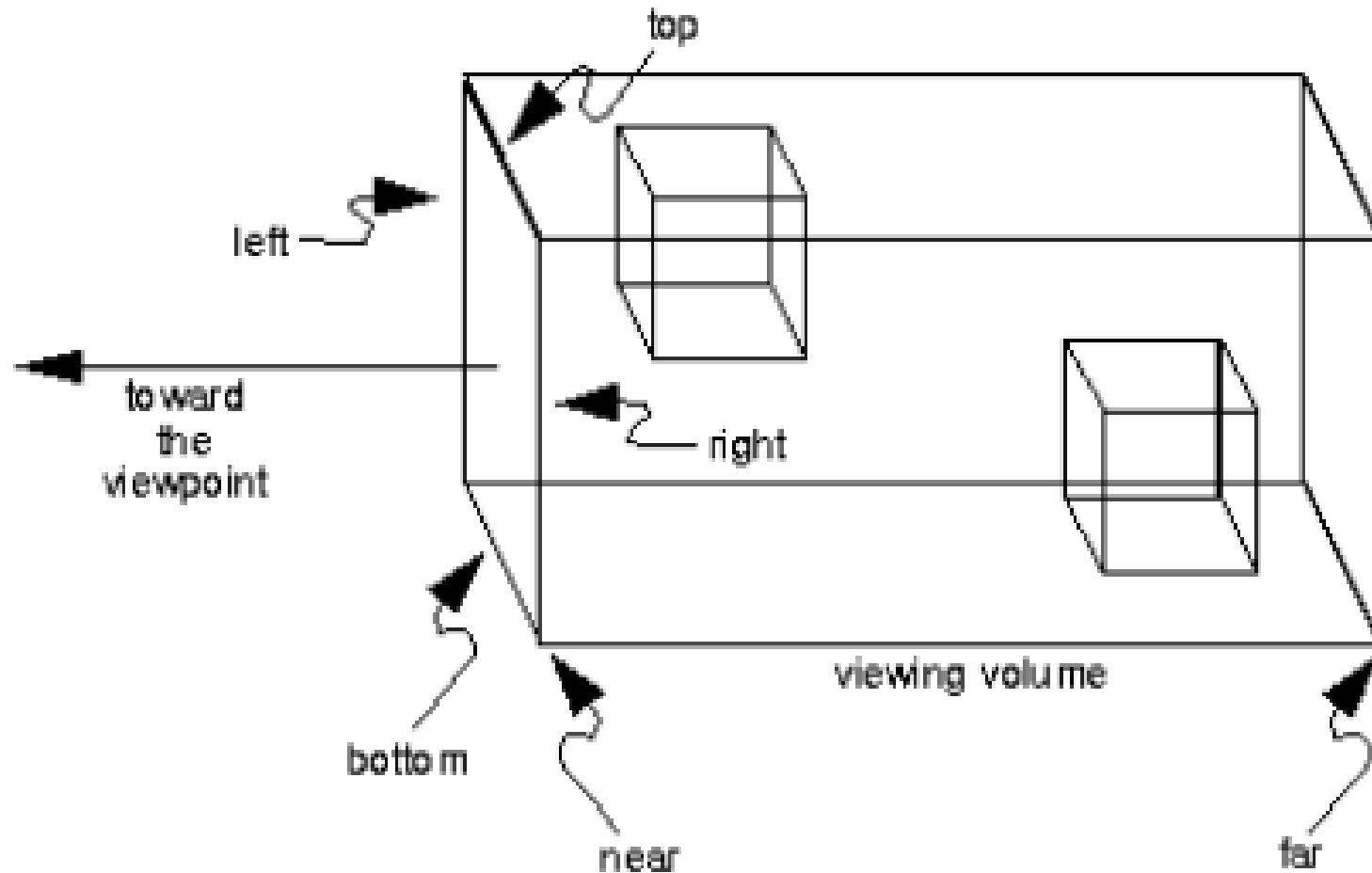
orthographic



oblique

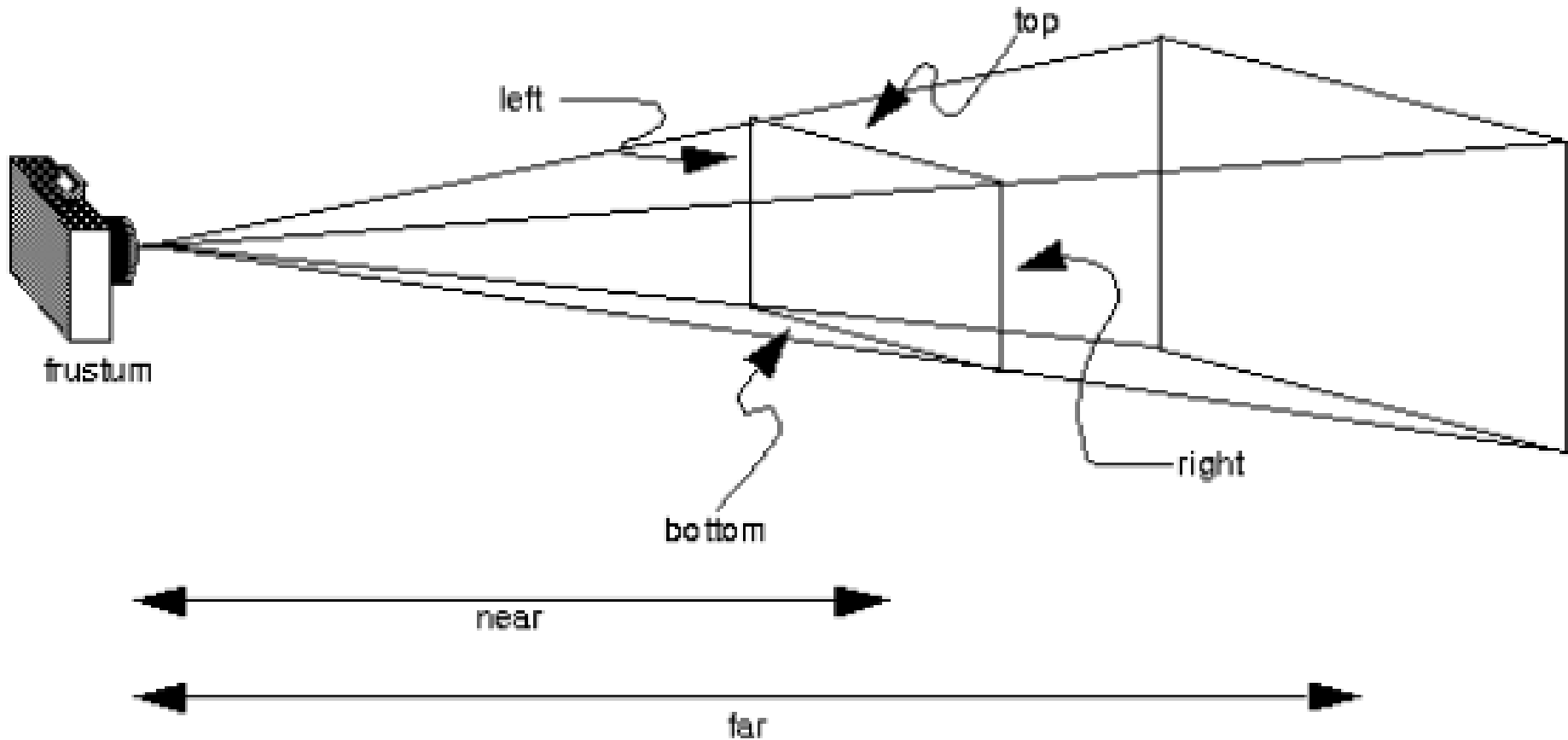


Orthographic Projection



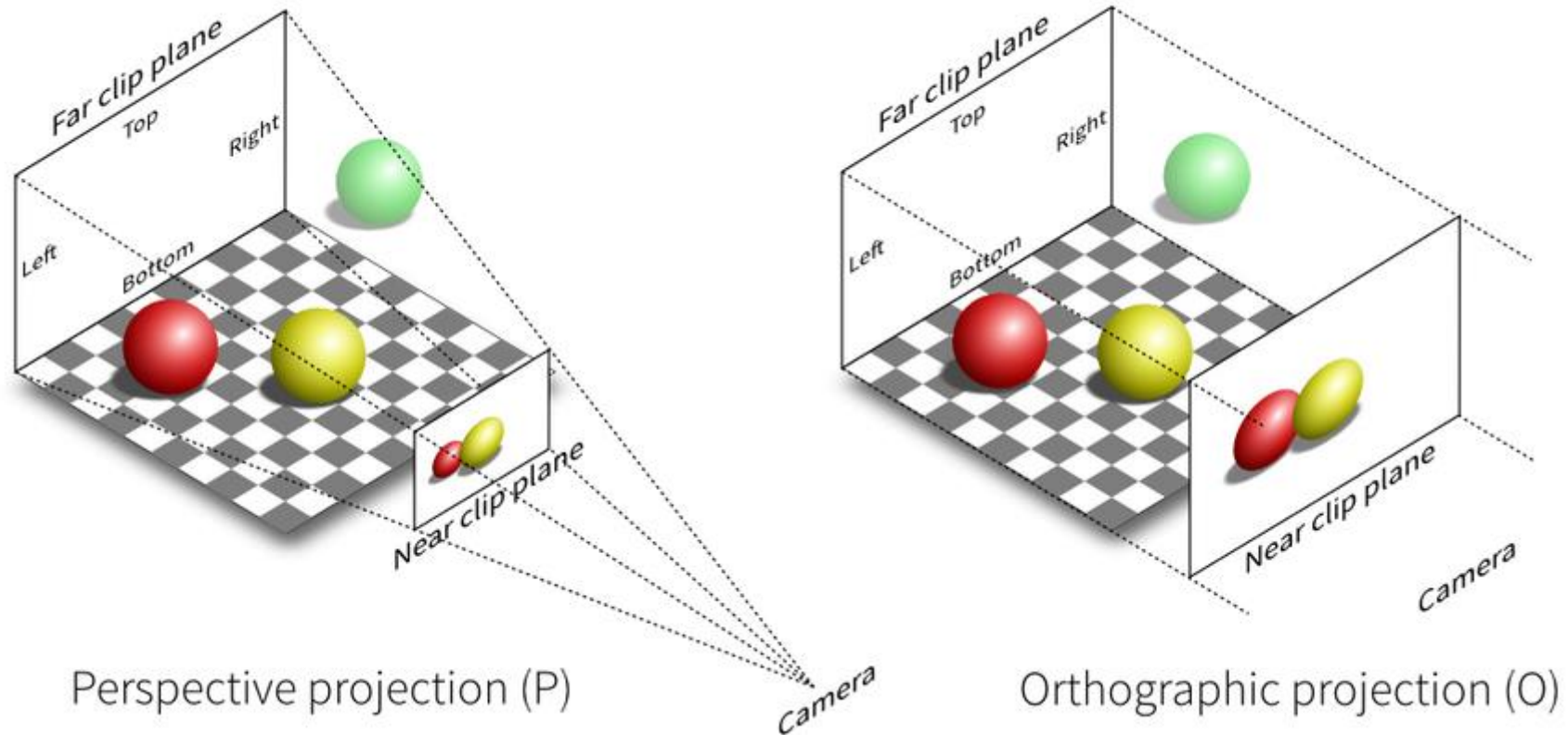
From OpenGL Programming Guide

Perspective Projection



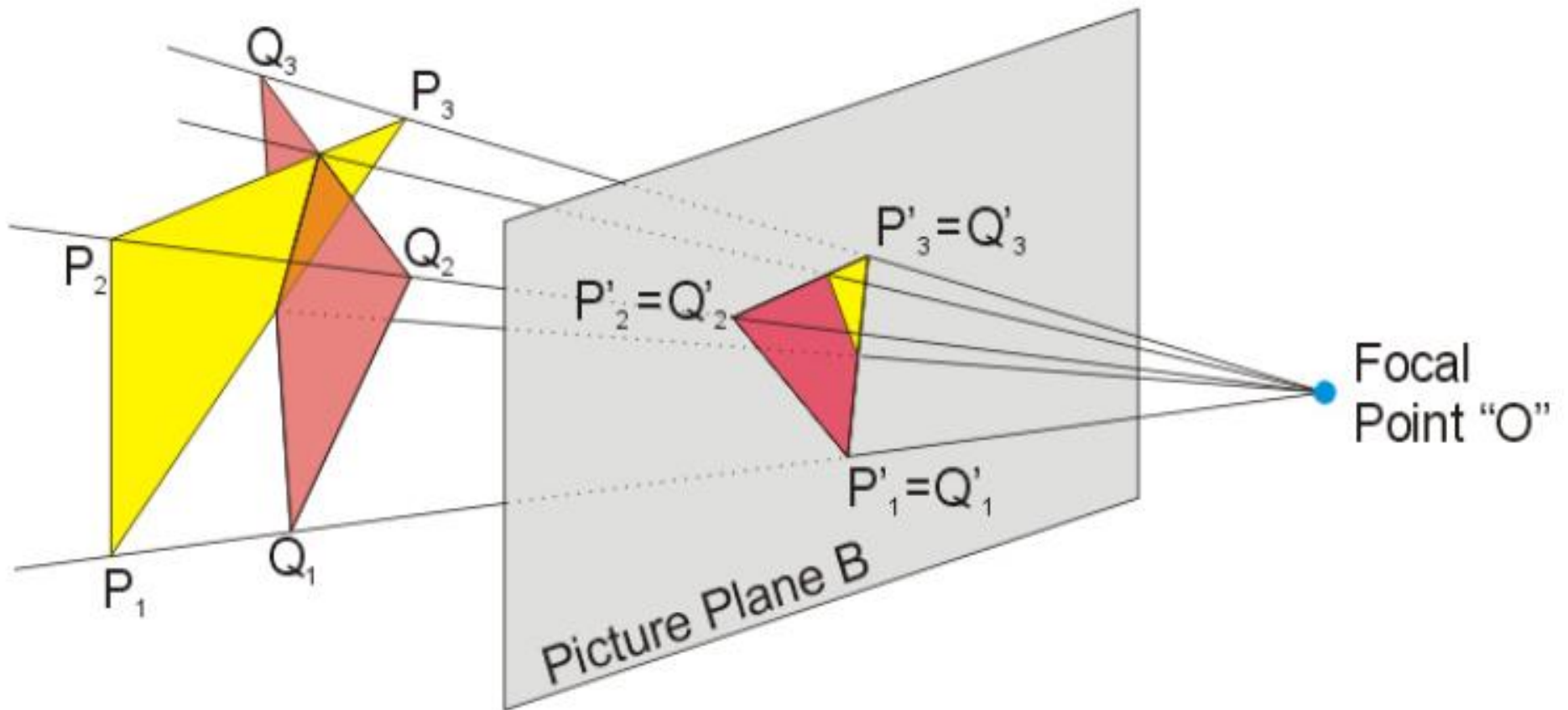
From OpenGL Programming Guide

Example



Nicolas P. Rougier, ERSF Code camp

Projection



Camera Specification

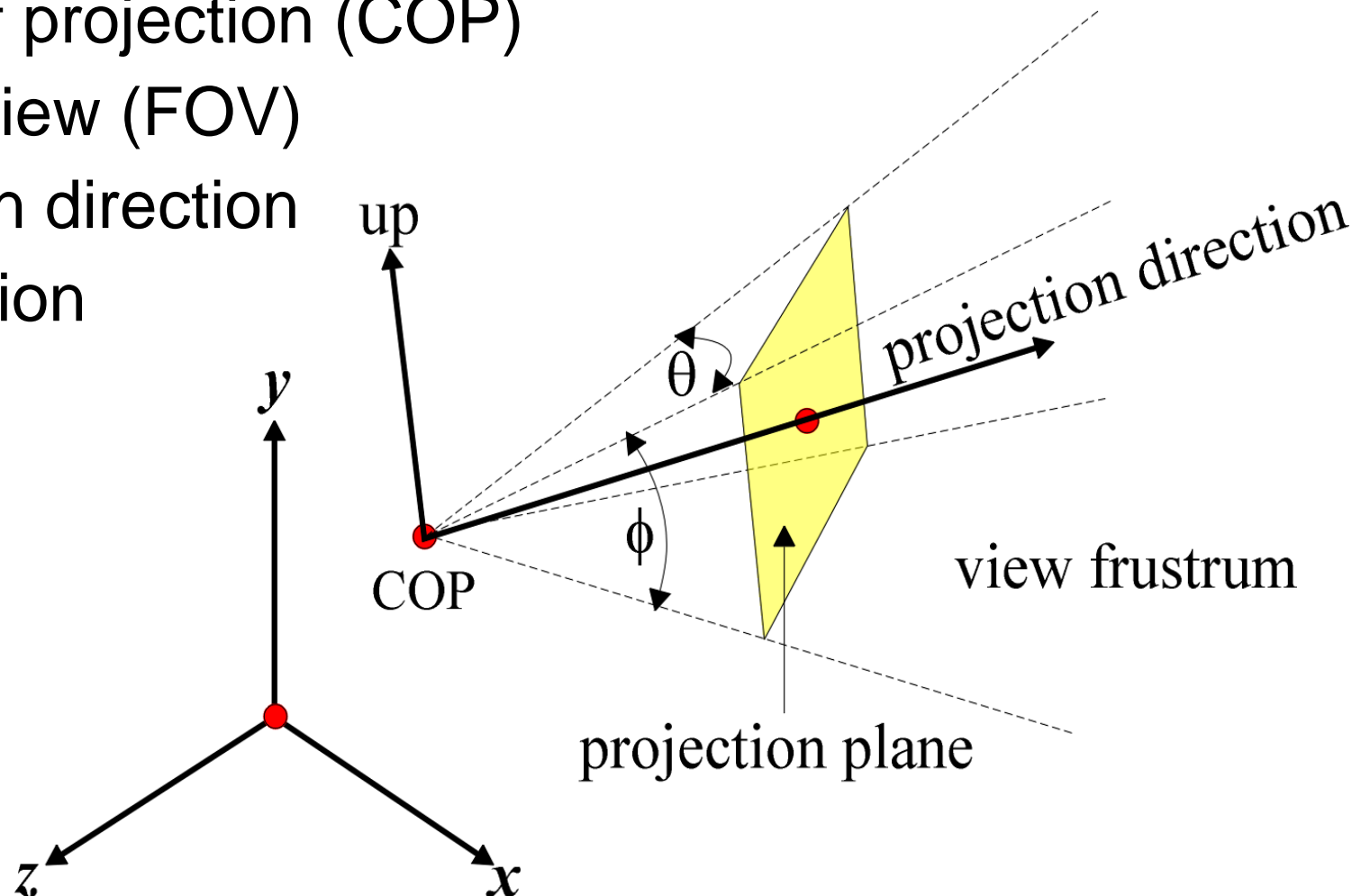
Parameters

Centre of projection (COP)

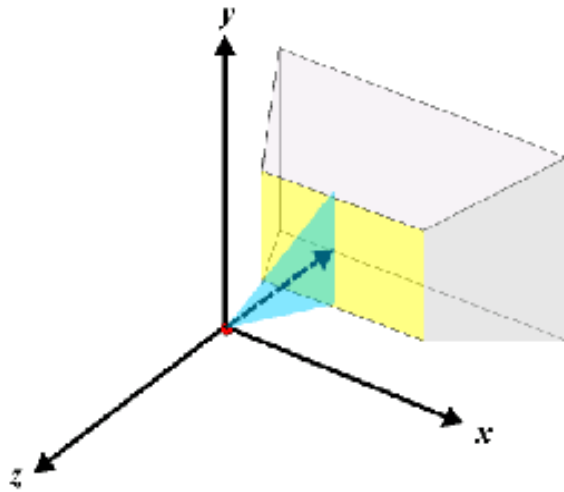
Field of view (FOV)

Projection direction

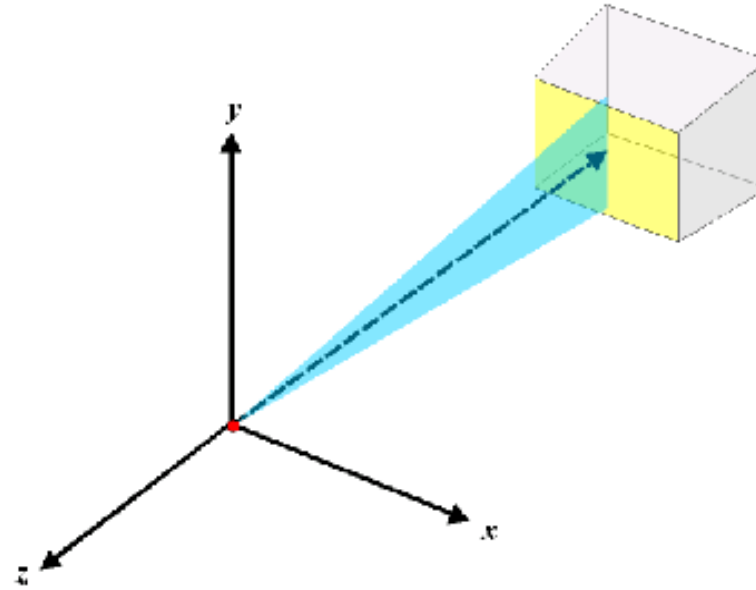
Up direction



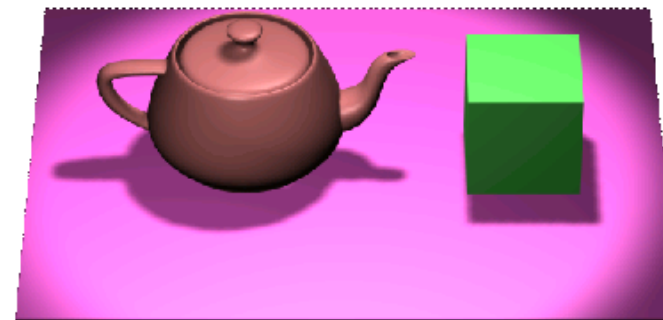
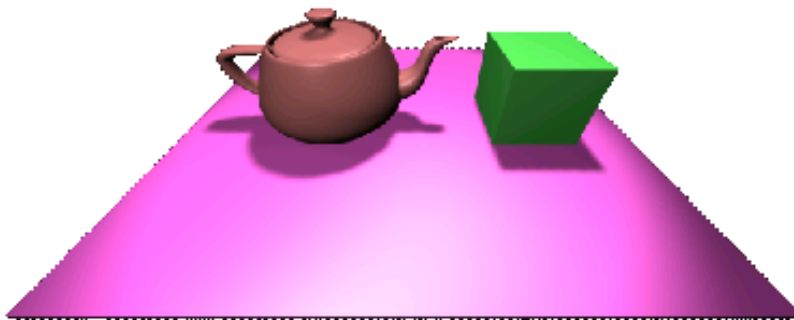
Outcomes



Large FOV



Small FOV

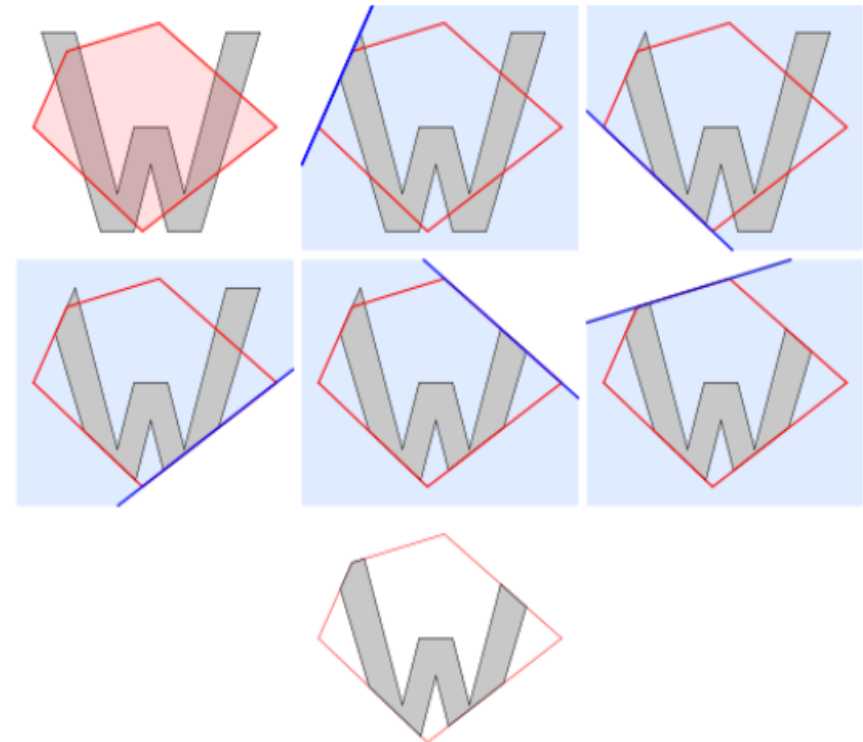


Clipping

Projected locations may be outside the viewing window

Truncate triangles to fit them inside the viewing area

- e.g. Sutherland-Hodgeman algorithm



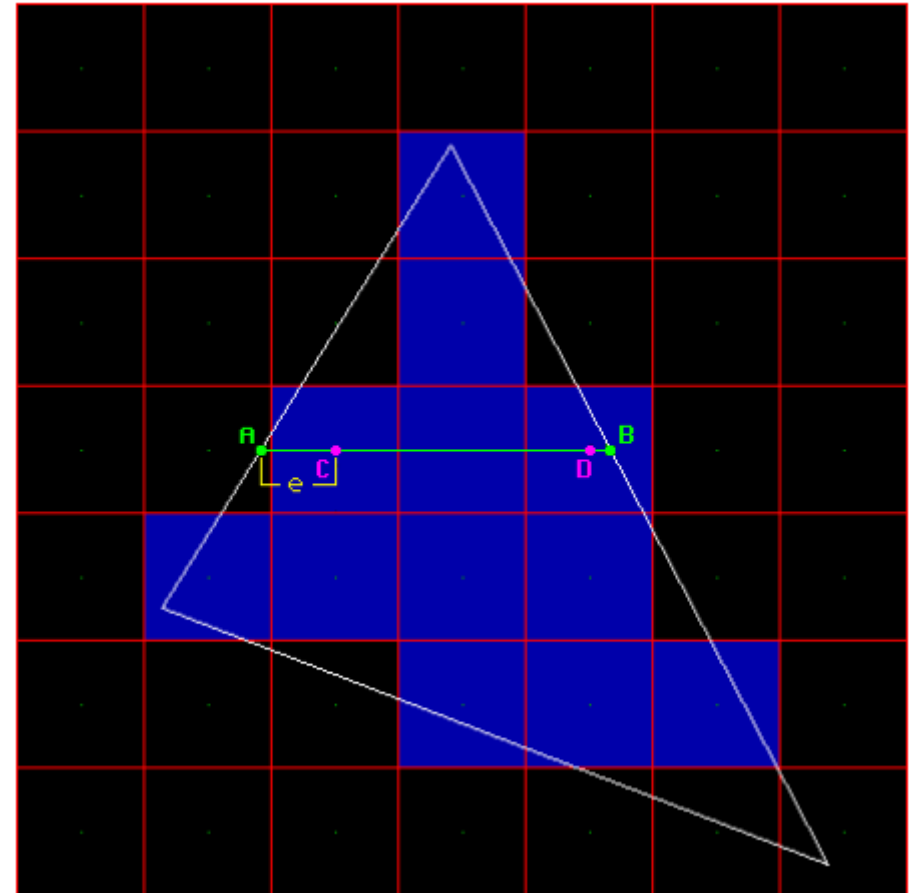
Real-time Rendering, Akenine-Moller, Haines and Hoffman

Scan Conversion

Fill interior of
triangles in image
plane

Use *scanline fill
algorithm* to fill
polygons

Framebuffer



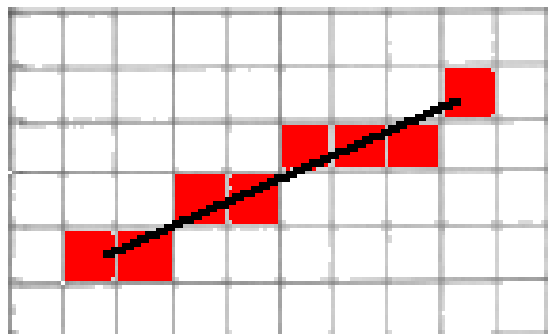
Line Drawing

A line usually defined as infinitely thin
How to display using pixels?

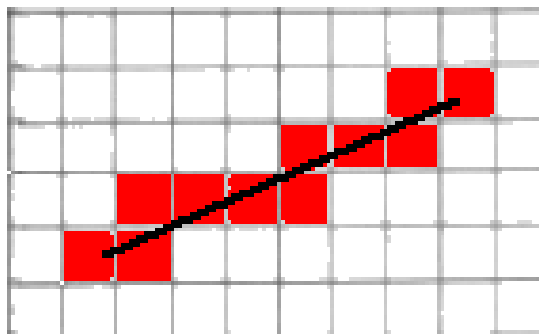
Fixed and finite area

Choose pixels that best represent the line

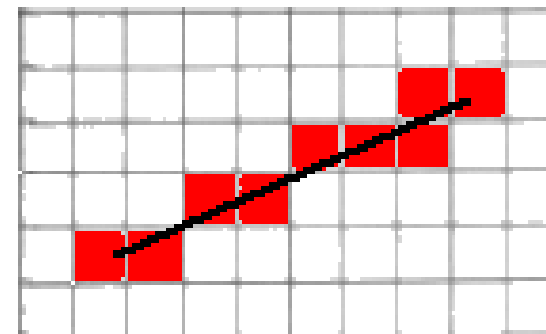
Different algorithms, providing different results:



mid-point



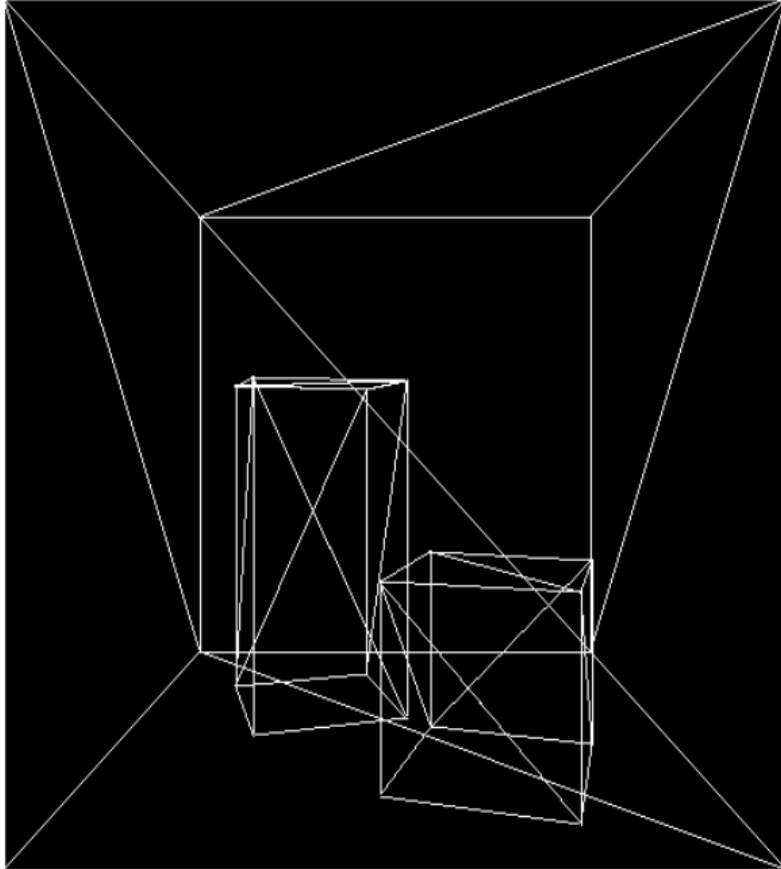
neighbourhood



weighted area

Line Drawing

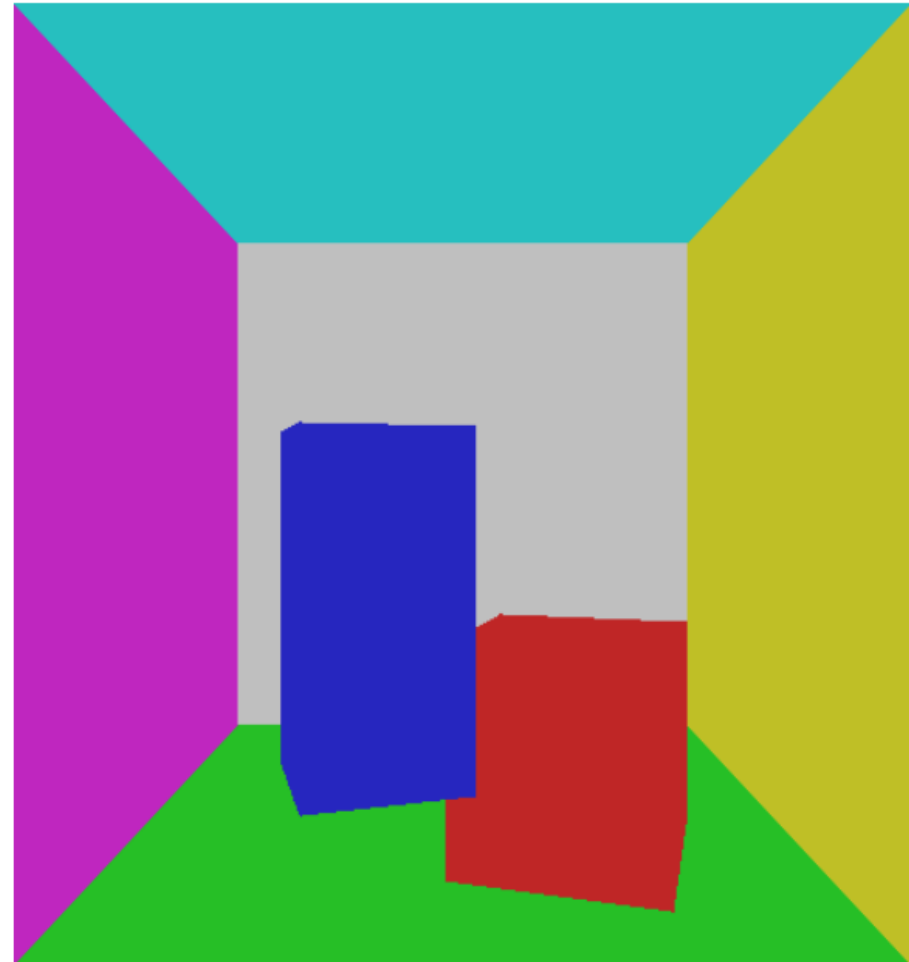
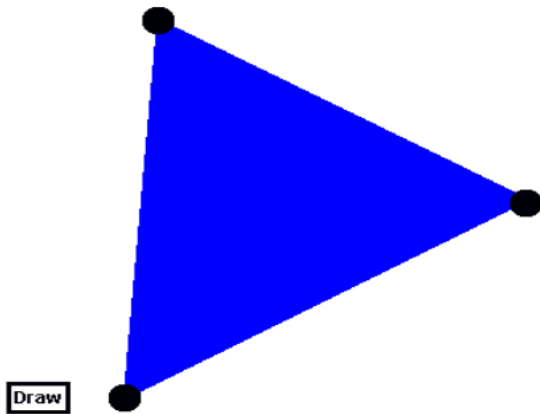
Bresenham's line algorithm



```
dx = x_end - x_start
dy = y_end - y_start
d = 2 * dy - dx
x = x_start
y = y_start
while x < x_end
  if d <= 0 then
    d = d + (2 * dy)
    x = x + 1
  else
    d = d + 2 * (dy - dx)
    x = x + 1
    y = y + 1
  endif
  SetPixel(x,y)
endwhile
```

Polygon Filling

Fill surface
Triangles
Interpolation
Compute edges



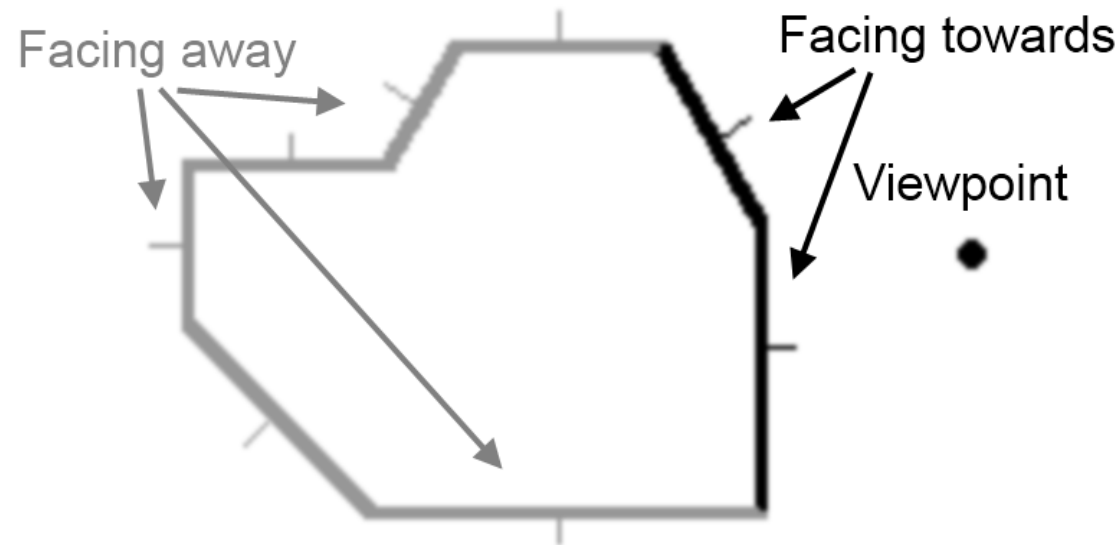
Backface Culling

Objects within the view-frustum may have polygons pointing away from the viewer

Not visible

Back-faces

The process is known as *back-face culling*



Backface Culling

To eliminate back-faces:

```
For each polygon in the scene {  
    Take its normal vector  
    Take the view direction vector  
    Use the dot product to find the angle between  
    normal and view direction  
    If the angle is LESS than 90 degrees, then the  
    polygon is culled  
}
```

Visible Surface Determination

Painter's algorithm

Sort polygons relative to the viewpoint

Render those polygons that are nearer the viewpoint *after* those polygons that are further away from the viewpoint

Problems?

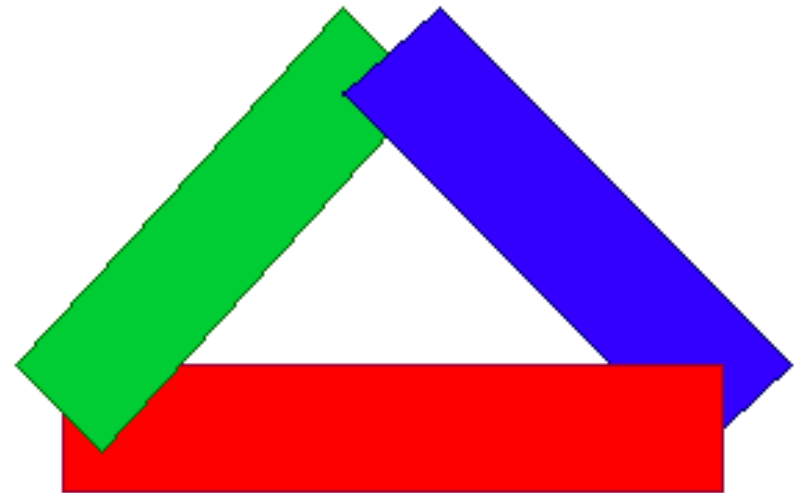
Visible Surface Determination

Painter's algorithm

Sort polygons relative to the viewpoint

Render those polygons that are nearer the viewpoint *after* those polygons that are further away from the viewpoint

Problems?



Depth Buffer

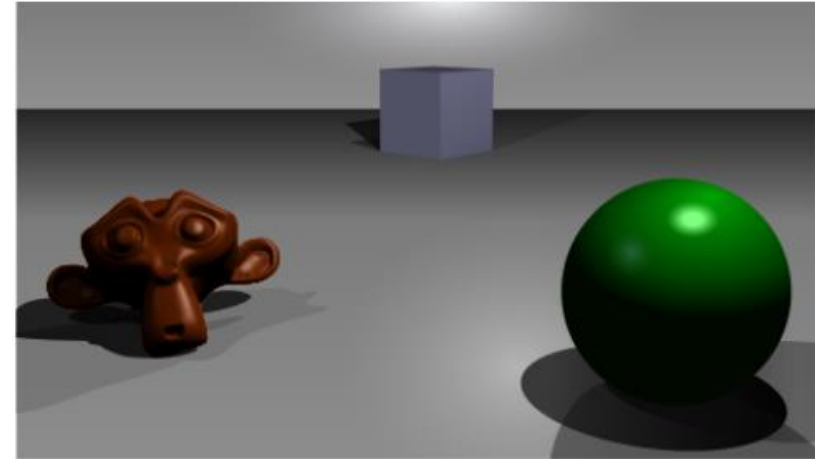
Image-space visibility algorithm

Buffer is 2D array,
one element per pixel

Compute depth of
each generated pixel

Overwrite depth buffer
value if new value is
nearer to camera than
previous

Non-linear, Z-fighting



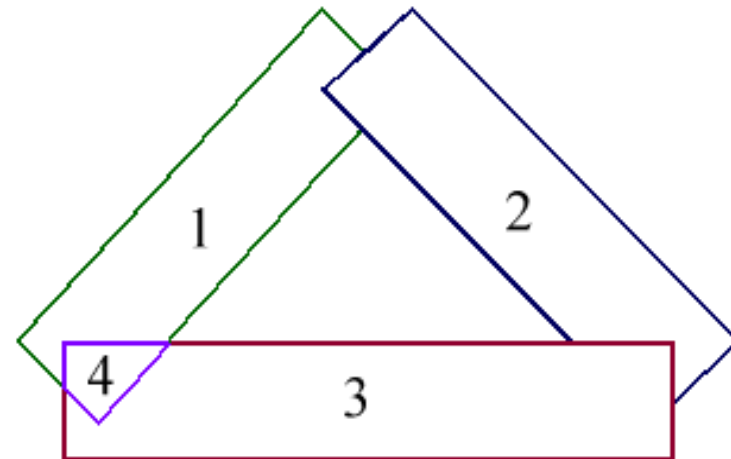
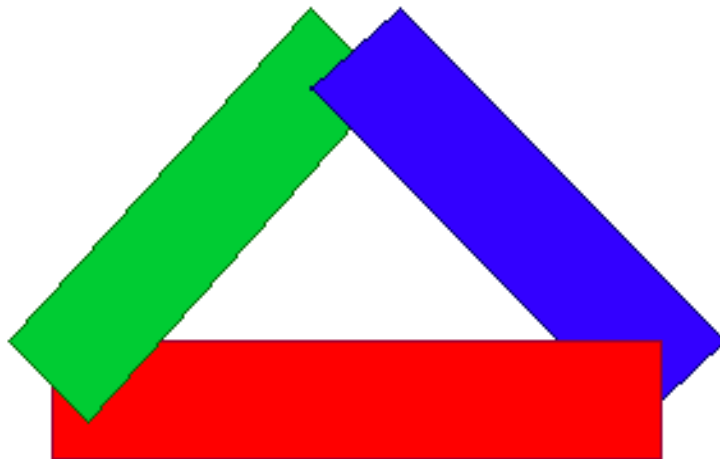
A simple three-dimensional scene

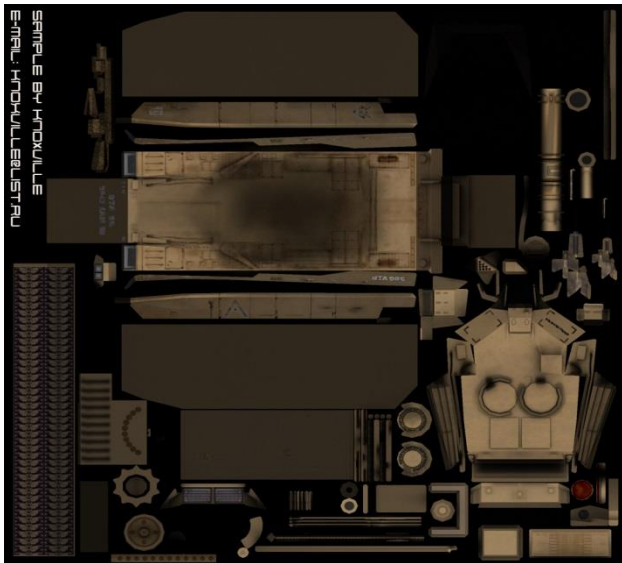


Z-buffer representation

Note: BSP Trees

Used by Quake, Quake 2, etc
World-space visibility algorithm
Visibility calculations on a *per polygon* basis
Split polygons
Compare with Z-buffer algorithm





Texturing

Bitmap (2D image) applied to a triangle

Each triangle associated with an image

Each vertex associated with a texture coordinate (u, v)

For each rendered pixel:

- Lookup corresponding texture element (*texel*)
- Interpolation

Labs

Animation track, lab 3 posted this Friday

Labs

Animation track, lab 3 posted this Friday

You should be finishing Lab 2 soon

Any major problems?

Suggested steps:

`Fork(continue working on problem)`

`If (help session happening soon)`

`Goto help session and ask(question)`

`Else`

`Post(specific details, KTH Social)`

`Wait until (reply or help session)`

Try not to crash in meanwhile...

(Physical) Labs Session

- Friday 29th April, 12.30-2p.m, Visualisation (VIC) Studio

See previous KTH Social posts for directions

- Purposes:
 - Ask questions/get help if in process of completing a lab task
 - Obtain **feedback** if you have work-in-progress
 - Code / report
 - Documentation

Submission dates

Submission date for all labs:

On or before **May 20th**

Through *Bilda* (will open by end of this week – look out for the notification email)

Submission date for all projects**:

On or before **May 31st**

Through *Bilda* (will open by end of this week)

****Also upload your project specifications to Bilda**