

$$2.4) E[x(n)] = -P + (1-P) = 1-2P$$

each realization independently happens  $\rightarrow E[x(n)x(m)] = E[x(n)]E[x(m)] = (1-2P)^2$

$$\Rightarrow E[y(n)] = (1-2P)^2 = m_y$$

$$r_y(k) = E[y(n)y(n+k)] = E[x(n)x(n-1)x(n+k)x(n+k-1)]$$

$$k=0 \Rightarrow r_y(0) = \underbrace{E[x(n)^2]}_{1} E[x(n-1)^2] = 1 \times 1 = 1$$

$$k=1 \Rightarrow r_y(1) = E[x(n)^2] E[x(n-1)] E[x(n+1)] = (1-2P)^2 = r_y(-1)$$

$$|k| \geq 2 \Rightarrow r_y(k) = E[x(n)] E[x(n-1)] E[x(n+k)] E[x(n+k-1)] = (1-2P)^4$$

$$2.8) E[z(n)z(n+k)] = E[x^2 \cos(2\pi\nu n) \cos(2\pi\nu(n+k)) + xy \sin(2\pi\nu n) \cos(2\pi\nu(n+k)) + xy \sin(2\pi\nu(n+k)) \cos(2\pi\nu n) + y^2 \sin(2\pi\nu n) \sin(2\pi\nu(n+k))]$$

$$= \underbrace{\frac{1}{2} \cos(2\pi\nu(2n+k)) (b_x^2 - b_y^2)}_{\text{function of } n} + \underbrace{\frac{1}{2} \cos(2\pi\nu k) (b_x^2 + b_y^2)}_0 + 0$$

$\Rightarrow$  for  $Z(n)$  to be WSS  $\Rightarrow b_x^2 = b_y^2$

$$E[z(n)] = 0$$

$$\text{if } b_x^2 = b_y^2 \Rightarrow R_z(k) = b_x^2 \cos(2\pi\nu k)$$

$$2.10) Z(+)>0 \Rightarrow g(x(+), y(+)) = 1 \Rightarrow x(+) \geq y(+)$$

$$Pr(x(+) \geq y(+)) = Pr(\underbrace{x(+) - y(+)}_{U(+)} \geq 0)$$

$U(+)$   $\rightarrow$  Gaussian because linear combination of independent Gaussian r.v.

$$m_U = m_x - m_y = -2$$

$$\sigma_U^2 = E[(x(+)-y(+))^2] - 4 = b_x^2 + b_y^2 - 2m_x m_y - 4 + m_x^2 + m_y^2 = 4 + 18 - 6 - 4 + 1 + 9 = 20$$

$$P(U(+) \geq 0) = Q\left(\frac{0 - (-2)}{\sqrt{20}}\right) = Q\left(\frac{2}{\sqrt{20}}\right)$$

\*note:  $Q(x) = \int_x^\infty \frac{1}{\sqrt{2\pi}} e^{-t^2/2} dt$