



DH2323 DGI17

INTRODUCTION TO  
COMPUTER GRAPHICS AND  
INTERACTION

**IMAGE-BASED RENDERING  
AND ANIMATION**

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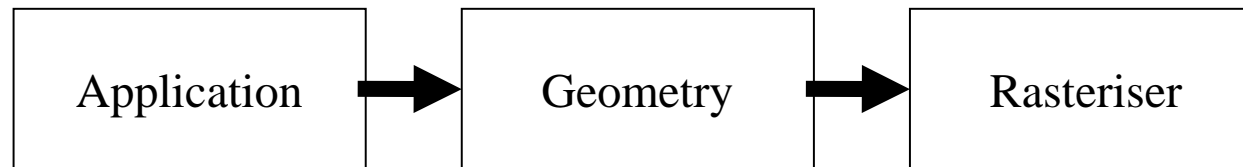
# Graphics Pipeline Architecture

Can divide pipeline into three conceptual stages:

*Application* (input, animations, think SDL)

*Geometry* (transforms, projections, lighting)

*Rasteriser* (draw image as pixels)



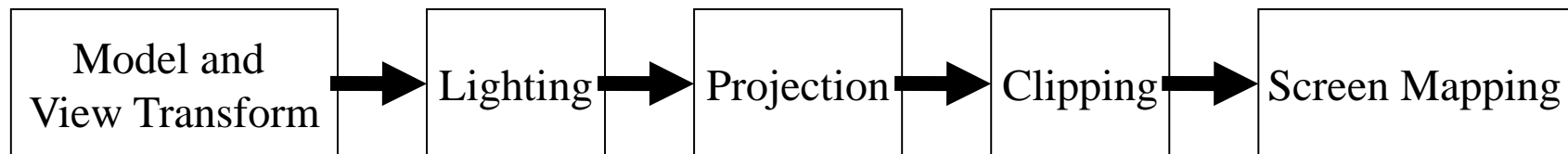
These define the core structure of the pipeline

# Geometry Stage

Responsible for polygon and vertex operations

Consists of five sub-stages:

- Model and View Transform
- Lighting and Shading
- Projection
- Clipping
- Screen Mapping



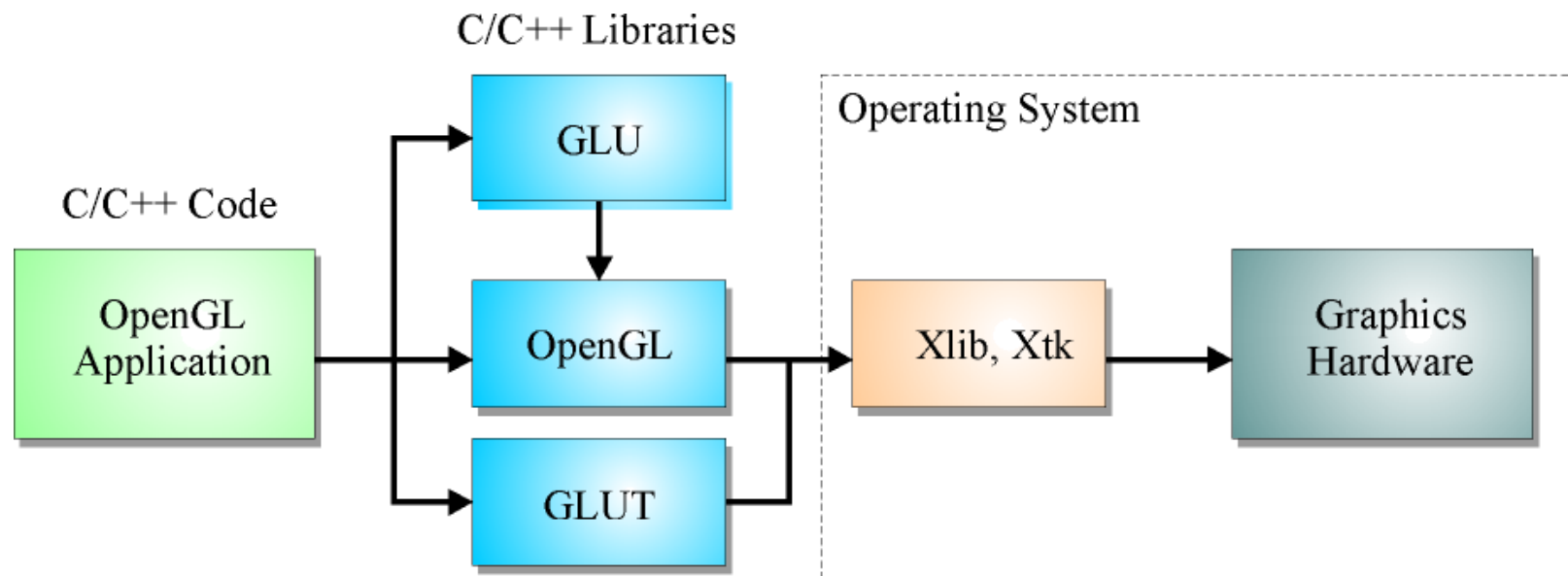
# What is OpenGL ?

Software interface to graphics hardware

Commands for interactive three-dimensional graphics

Hardware independent interface

Drawing operations performed by underlying system and hardware



# I.

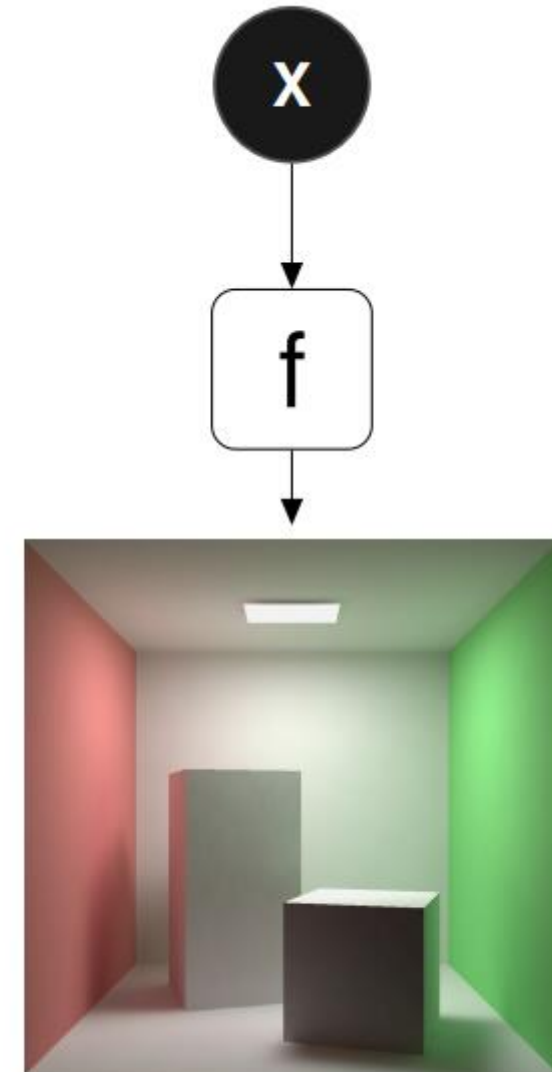
## Image-based Rendering

# Image-based Rendering

**X** constitutes:

- Geometry
- Texture
- Lighting
- Material

Parameterisation of the 'world'

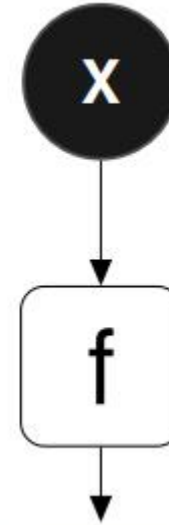


# Image-based Rendering

How does  $f(\cdot)$  manipulate  $X$ ?

- Light
- Surface interaction
- Light transport

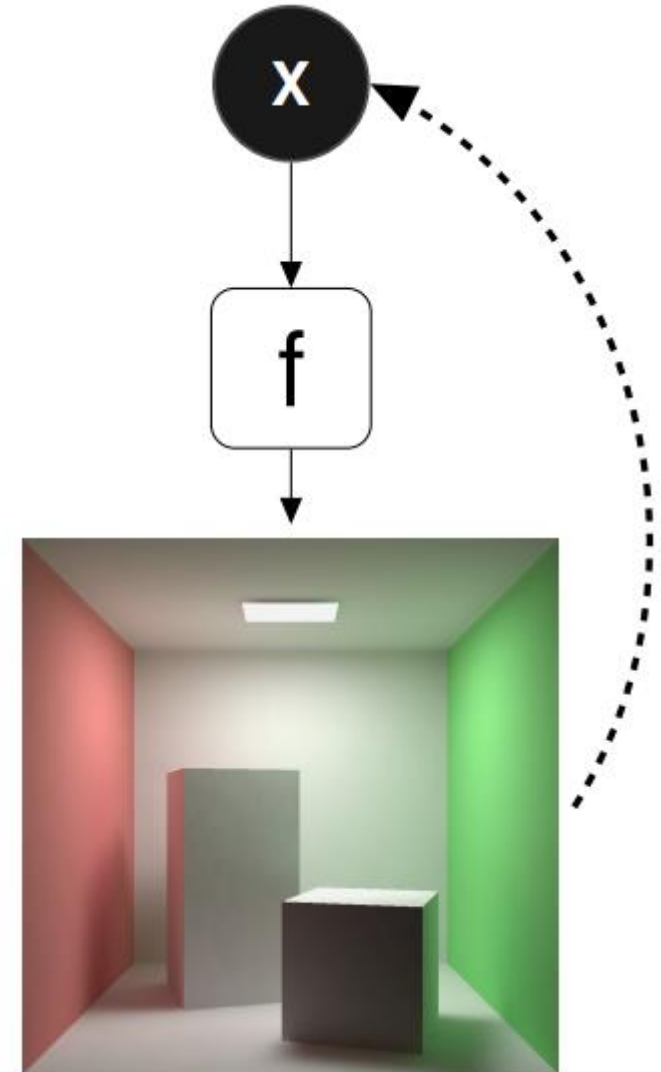
Formulate model  $f(\cdot)$  through assumptions



# Image-based Rendering

## Computer Vision

- Image easy to acquire
- Solve inverse problem
- What parameters have generated the image?





# Image-based Rendering

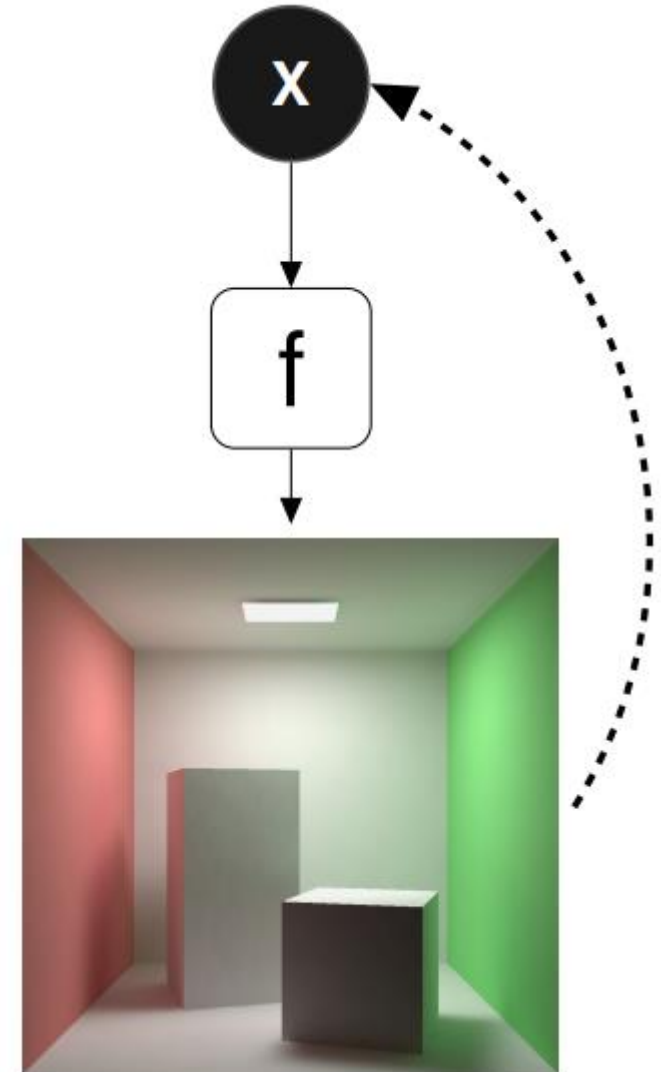
Challenge:

Given an image recover the parameters

- Texture
- Light
- Geometry

Models still valid

- $x_i = f^{-1}(y_i)$



# Image-based Rendering



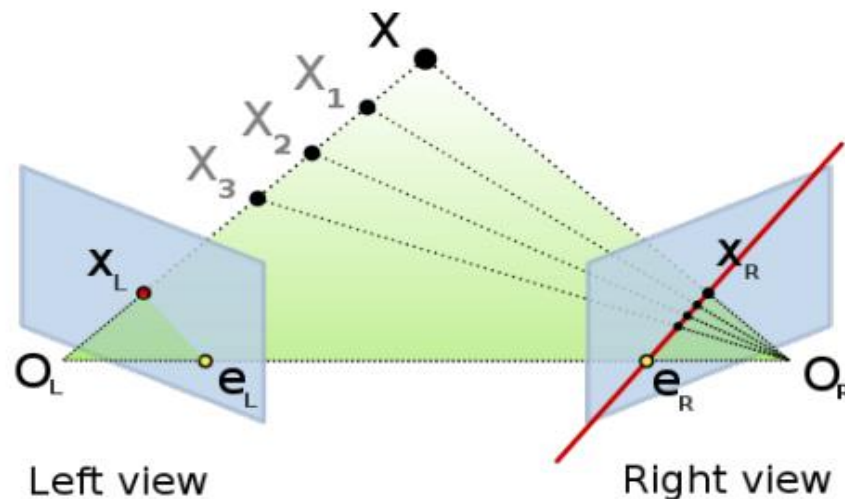
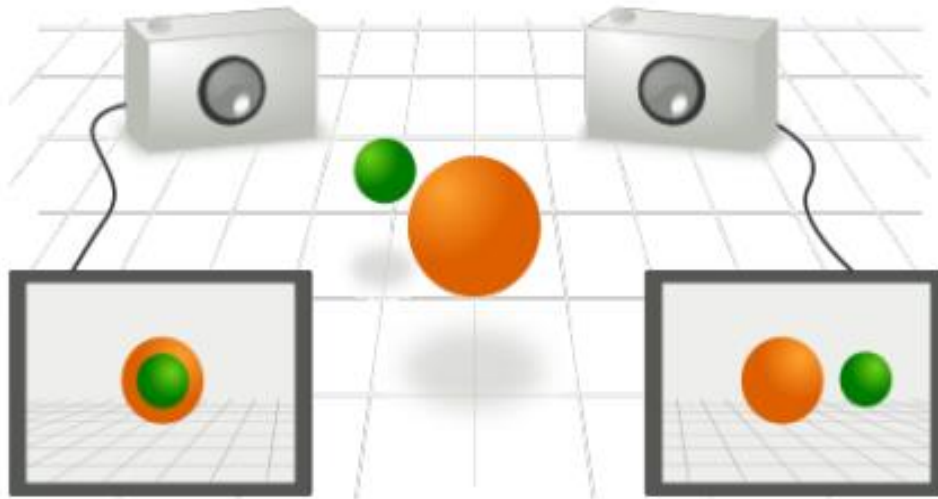
Rendering: generate images from viewpoints

Image-based rendering: replace geometry and material attributes with real images

Most realistic image? A photograph

- Lacks flexibility
- Cannot change lighting or viewpoint
- Combine images to produce a new one

# Epipolar Geometry



The geometry of stereo vision

Two cameras viewing 3D scene from different positions

Study geometric relations between 3D points and their 2D projections

More images = more constraints



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# II.

## Animation



# Traditional Animation

Showing consecutive related static images one after another produces the perception of a moving image

Master artists draw certain important **key-frames** in the animation

Apprentices draw the multitude of frames in-between these key-frames

Called **tweens**



# Computer Animation

Objects have an initial configuration and a final configuration (often specified by the artist)

- Position, orientation, etc

Computer calculates the intermediate configurations:  
*interpolation*

Orientation Interpolation:

Given two key-frame orientations, calculate an intermediate orientation between them

# Question

How do we interpolate orientations?

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Remember how they are represented

- 1) Rotations around axes
- 2) Rotation matrices



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Possible solutions: Euler angles and rotation matrix interpolation

# #1: Euler Angles

An Euler angle is a rotation around a single axis

Any orientation can be specified by composing three rotations

Each rotation is around one of the **principle axes**

i.e. (x, y, z) – first rotate around x, then y, then z

Think of roll, pitch and yaw of a flight simulator

When rotating about a single axis, is possible to interpolate a single value

However, for more than one axis, interpolating individual angles will not work well

Unpredictable intermediate rotations

Gimbal lock

## #2: Rotation Matrices

Interpolating between two rotation matrices does not result in a rotation matrix

- Does not preserve rigidity of angles and lengths
- This result of an interpolation of 0.5 between the identity matrix and 90 degrees around the x-axis does not produce a valid rotation matrix:

$$\text{Interpolate} \left( \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix} \right) \equiv \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0.5 & 0.5 \\ 0 & -0.5 & 0.5 \end{bmatrix}$$

# Solution

Use *quaternion interpolation*

Quaternions don't suffer from Gimbal lock

Can be represented as 4 numbers instead of 9 of a 3x3 matrix

Trivial conversion between angle/axis representation

Interpolation between two quaternions is easy (once you know how)

Quaternion looks like this:

$q[w, (x, y, z)]$  also written  $q[w, v]$  where  $v = (x, y, z)$

$q = w + xi + yj + zk$

# Representation

For a right-hand rotation of  $\theta$  **radians** about unit vector  $v$ , quaternion is:

$$q = (\cos(\theta/2); \mathbf{v} \sin(\theta/2))$$

- Note how the 3 imaginary coordinates are noted as a vector
- Only **unit quaternions** represent rotations
  - Such a quaternion describes a point on the 4D unit hypersphere
- Important note:  $q$  and  $-q$  represent the **exact same** orientation
- Different methods for doing quaternion interpolation: LERP, SLERP (Spherical linear interpolation)



# In Practice

Not always the best choice

Quaternions are (as you will have noticed) hard to visualise and think about

If another method will do and is simpler, it will be a more appropriate choice

But...

Extremely useful in many situations where other representations are awkward

Easy to use in your own programs once you have a quaternion class

See Animation track labs and GLM library

# Reminders

- You should be working on Lab 3
- Labs due on Friday 26<sup>th</sup> May
  - Canvas DH2323 submission will open this week
- Project work (due May 31st)
- Lab session:
  - Today from 13:00-15:00,
  - Visualization Studio

# Next lecture

- User studies and perception
- Will take place in B2
- Monday 15<sup>th</sup> May
- 10:00 – 12:00