Collision Detection in Computer Games

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Outline

1. Self-Introduction
   - Who is Fangkai?

2. Collision Detection
   - Let’s Play a Game!
   - Collision Detection
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1. Self-Introduction
   - Who is Fangkai?

2. Collision Detection
   - Let’s Play a Game!
   - Collision Detection
Fangkai Yang is a crazy Gamer, Mathematician and Programmer.

- PhD candidate in Computer Science. Research on Crowd-simulation and Game AI.
- Game developer: Just Cause 3 (Avalanche Studios), War Rage (NetEase Games).
Collision detection concerns the detection of collisions between objects in the virtual environment. Primarily employed to stop objects moving through each other and the environment.

Collision Detection is everywhere in computer games: between characters and characters, between characters and terrain, etc.

Remember:
- Physical laws do not exist in the virtual world by default.
- Must computationally model and program them.
Dayz Standalone

What my friends think I was playing:
What I was actually playing:
Dayz Standalone

What I was actually playing:

![Image of Dayz Standalone game scene with a character standing on a rooftop]

Fangkai Yang

Collision Detection in Computer Games
What my friends think I was playing:
What I was actually playing:
Basic Geometry Types

Rigid-bodies
- Hard objects (ideal solid bodies)
- Constant distance between vertices in the mesh
- Convex vs. concave

Soft-bodies
- Cloth, for example
- More complicated to simulate
- Soft-bodies like cloth may collide with themselves
Basic Geometry Types
Basic Geometry Types

https://www.youtube.com/watch?v=M5Ygpxfmcg8
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King of Fighter 97

I want a volunteer!
Question:
How to test if a character has been hit?
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Collision Detection

Definition

Collision detection refers to the detection of the intersection of two or more objects.

Figure: Collision detection in Street Fighter
Figure: Overlaps of characters.
How about collision detection in 3D games?
Penetration

When collision is detected, the penetration follows.
Two forms of collision detection:

- Continuous: very expensive. Simulate solid objects in real life.
- Discrete: objects will end up with penetrating each other.
Backtracking

Like Tom Cruise in *Edge of Tomorrow*, it turns time backwards and fix the penetration that occurred in the last frame.
Bounding Volume

**Definition**

Bounding volume for a set of objects is a closed volume that completely contains the union of the objects in the set.

(a) In the game scenario.  
(b) In the physics engine.
Bounding Volume types

- **Bounding Box**: Axis Aligned Bounding Box (AABB), Oriented Bounding Box (OBB), etc. For objects that rest upon other, such as a car resting on the ground, using a bounding box is a better choice.
- **Bounding Sphere**: They are very quick to test for collision with each other.
Sphere Collision Detection

Circles are colliding if $D \leq (R1 + R2)$

d is the distance between the circle centers

R1 and R2 are the radii of both circles respectively
Recall: Faces of an AABB are aligned with the coordinates axes.

To see if A and B overlap, separating axes test can be used along the x,y and z axes. This is faster, as only need to search x,y and z axes.
Some Problems

- Naive collision detection approaches may simply test if two objects are overlapping at every time-step.
- Problem: quickly moving objects can pass right through each other without detection.

(b) First test.
(c) Second test.
Swept Volume

The AABB in the game bounds not the object, but the *Swept Volume* of the object from one frame to the next.

![Diagram of Swept Volume](image)

- $T_0$ and $T_1$ are two time frames.
- $A$ and $A'$ are the objects at $T_0$ and $T_1$.
- $v$ is the velocity of the object.
- The obstacle is represented by a grey shape.
Most efficient implementations use a two-phase approach: a broad phase followed by a narrow phase.

- **Broad phase**: collision tests are based on bounding volumes only. Quickly prune away pairs of objects that do not collide with each other. The output is the potentially colliding set of pairs of objects.

- **Narrow phase**: collision tests are exact—they usually compute exact contact points and normals—thus much more costly, but performed for only the pairs of the potentially colliding set.
Figure: Collision detection between AABBs (Axis Aligned Bounding Box).
The broad phase collision detection helps to filtrate the potentially colliding object sets. The brute-force way is doing collision test for all pairs of objects, and the complexity is $O(n^2)$. 

(a) Sweep and prune. (b) Spatial subdivision.
Narrow Phase

Separating Axis Tests

- Many algorithms are based on the separating hyperplane theorem

Figure: Two disjoint convex sets are separable by a hyperplane.

Separation w.r.t. a plane $P$ => separation of the orthogonal projections onto any line $L$ parallel to plane normal.
Separating Axis Tests

Think of it like this: do a twist to simplify calculations.

Separating axis is a line for which the projection intervals do not overlap.
Separating Axis Tests

Separated if $A_{\text{max}} < B_{\text{min}}$ or $B_{\text{max}} < A_{\text{min}}$

Question: Which axes to be tested?
Separating Axis Tests

Axes to test:
Convex versus Convex Collision Detection

One of the most commonly used algorithms in game engines is the GJK (Gilbert-Johnson-Keerthi) algorithm. This algorithm relies on a support function to iteratively get closer simplices to the solution using Minkowski difference.

(a) Two shapes collide on one vertex.  
(b) No collision.
Given the two polyhedra:
- Computes the distance $d$ between them
- Can also return the closest pair of points on each polygons
Support Mapping Function

- Supporting point. This is an extreme point on the polygon for a given direction $d$.
- The support mapping function returns this point.
The first simplex is built using what is called a *support function*. Support function returns one point inside the Minkowski difference given two sets $K_A$ and $K_B$.

**Figure:** The first two vertices in the first simplex.
An Example

Collision Detection in Computer Games
Select direction $d = (1, 0)$:
$p1 = (9, 9); p2 = (5, 7); p3 = p1 - p2 = (4, 2)$;
Select direction \( d = (-1, 0) \):
\[ p1 = (4, 5); p2 = (12, 7); p3 = p1 - p2 = (-8, -2); \]
Select direction $d = (0, 1)$:
$p1 = (4, 11); p2 = (10, 2); p3 = p1 - p2 = (-6, 9)$;
The Simplex doesn’t contain the origin, but we know that the two shapes are intersecting. The problem here is that our first guess (at choosing directions) didn’t yield a Simplex that enclosed the origin.
Select direction \( d = (0, -1) \):
\[ p_1 = (4, 5); p_2 = (5, 7); p_3 = p_1 - p_2 = (-1, -2); \]
Now we contain the origin and can determine that there is a collision
An Example

```java
Vector d = // choose a search direction
// get the first Minkowski Difference point
Simplex.add(support(A, B, d));
// negate d for the next point
d.negate();
// start looping
while (true) {
    // add a new point to the simplex because we haven't terminated yet
    Simplex.add(support(A, B, d));
    // make sure that the last point we added actually passed the origin
    if (Simplex.getLast().dot(d) <= 0) {
        // if the point added last was not past the origin in the direction of d
        // then the Minkowski Sum cannot possibly contain the origin since
        // the last point added is on the edge of the Minkowski Difference
        return false;
    } else {
        // otherwise we need to determine if the origin is in
        // the current simplex
        if (Simplex.contains(ORIGIN)) {
            // if it does then we know there is a collision
            return true;
        } else {
            // otherwise we cannot be certain so find the edge who is
            // closest to the origin and use its normal (in the direction
            // of the origin) as the new d and continue the loop
            d = getDirection(Simplex);
        }
    }
}
```
Self-Introduction
Collision Detection

Let's Play a Game!
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(a) The first iteration.  (b) New simplex does not contain the origin.

(c) The second iteration.  (d) New simplex contains the origin.
Thank you for Listening and Sleeping!