

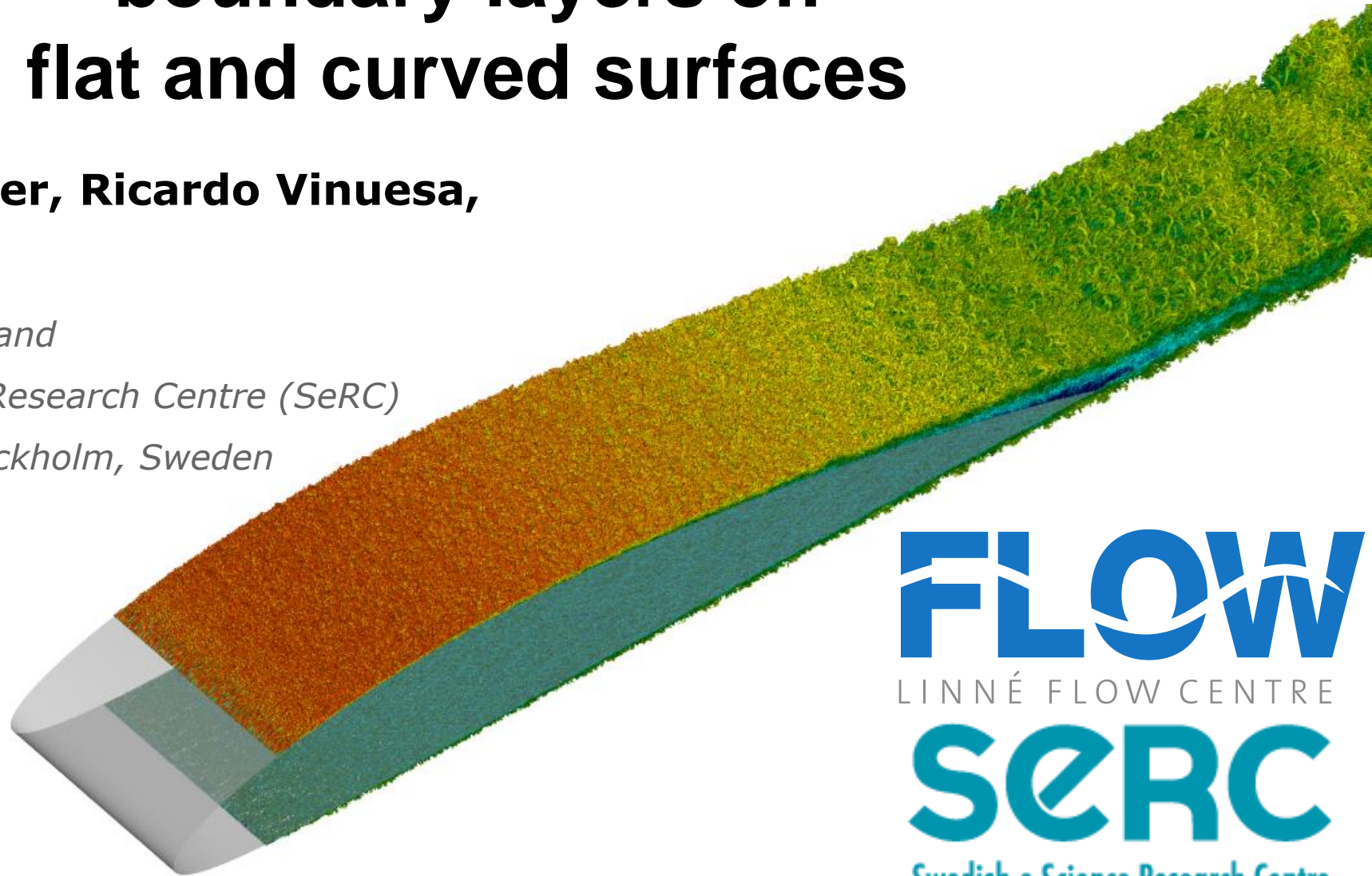
# High-fidelity simulations of turbulent boundary layers on flat and curved surfaces

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*Linné FLOW Centre and*

*Swedish e-Science Research Centre (SeRC)*

*KTH Mechanics, Stockholm, Sweden*





# Outline

- Introduction – HPC
- Turbulent boundary layers – Simulation
- Wing simulations
- Flow control
- Codes and tools

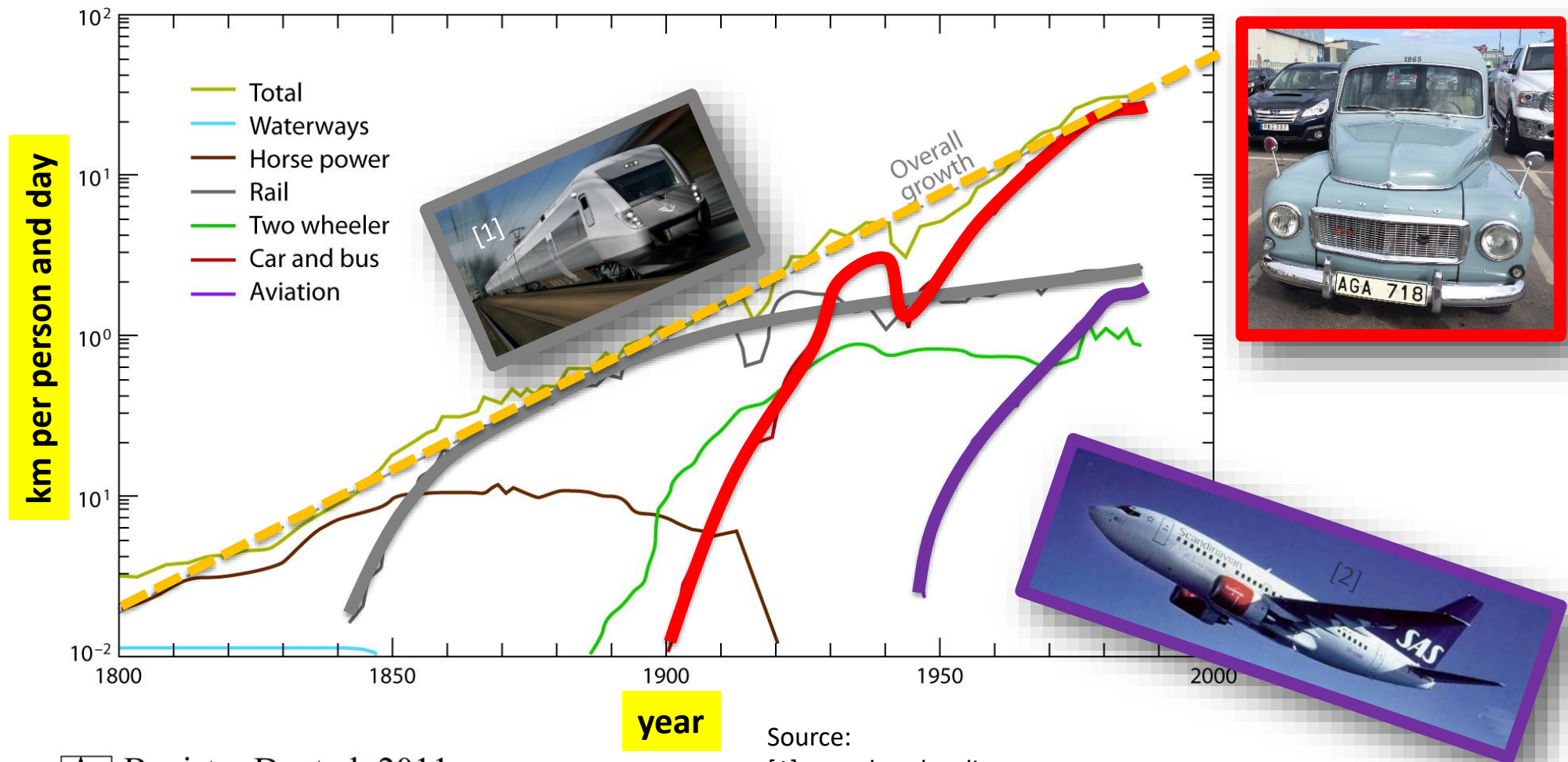



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# Why CFD?

Skin friction/drag reduction is the key for economically and ecologically more efficient transport



 Banister D, et al. 2011.  
Annu Rev. Environ. Resour. 36:247–70

Source:  
[1] [www.bombardier.com](http://www.bombardier.com)  
[2] [www.flysas.de](http://www.flysas.de)



# Navier-Stokes equations...

Data from Mira (ANL, 2013), million core hours

• Engineering/CFD	525	19%
• Subsurface flow & reactive transport	80	3%
• Combustion	100	4%
• Climate	280	10%
• Astrophysics	133	5%

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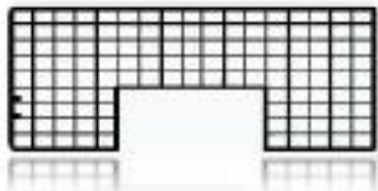
**1118 40%**

(fraction of Navier-Stokes based simulations on current supercomputers)

# Why Spectral Elements?

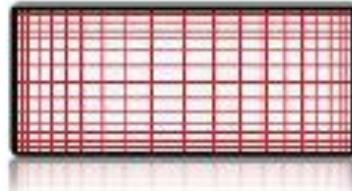
- **High-order numerical methods** are beneficial for accurate simulations of turbulent flows due to the significant scale disparity of the flow structures, both in time and space.
- Spectral elements allow to solve **flows in complex geometries**.

Finite element (FE)

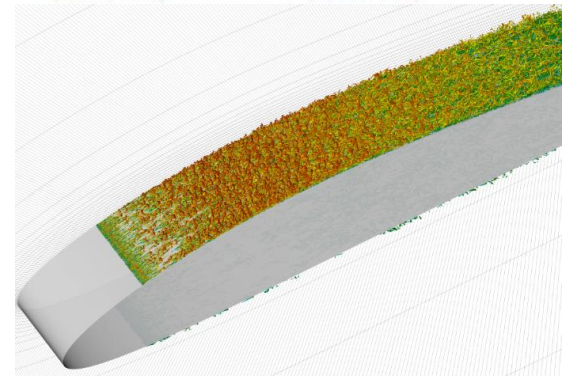
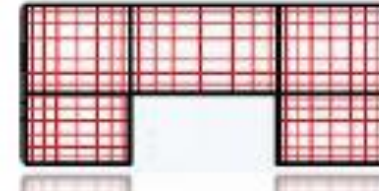


+

Spectral



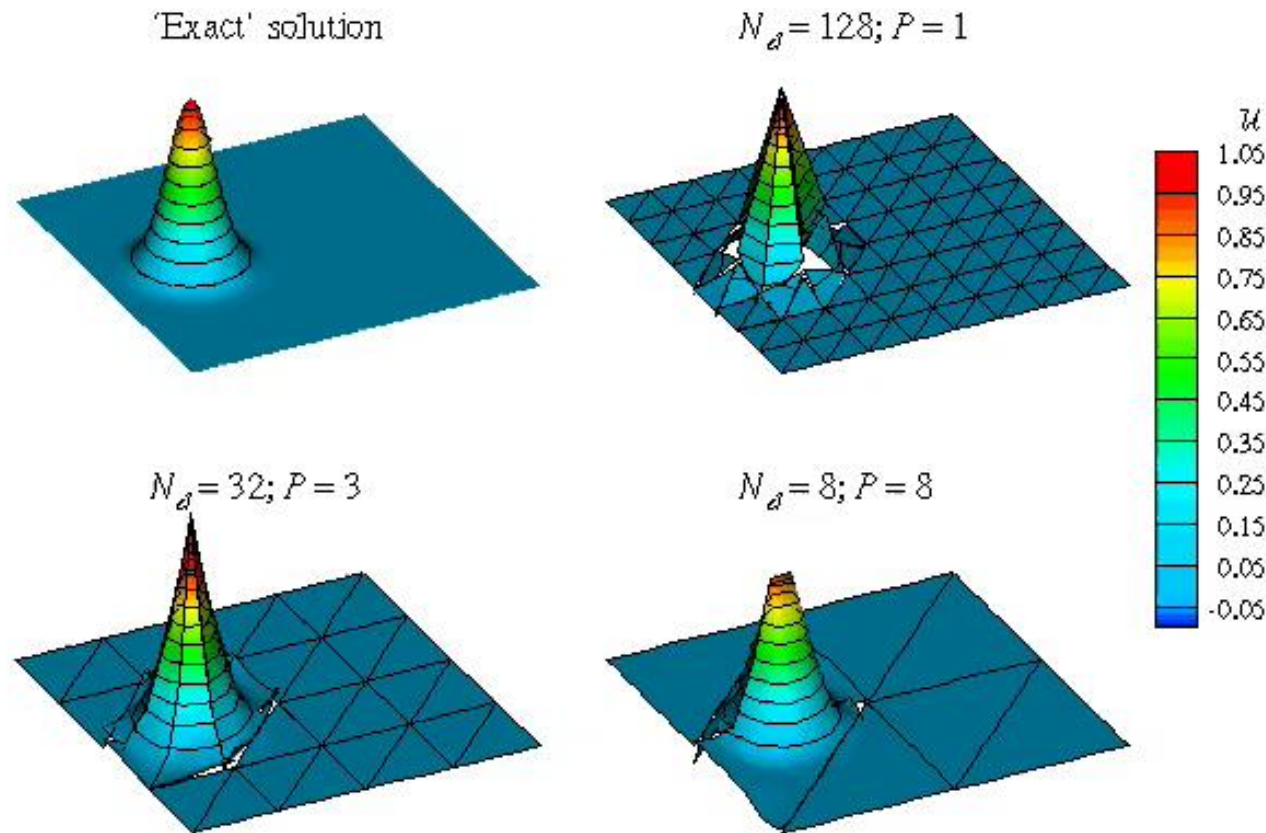
Spectral element (SE)



# Why Spectral Elements?

- Higher order  $p$  (vs. smaller grid spacing  $h$ ) means more work per core/communication: **"convecting cone"**

Time = 0

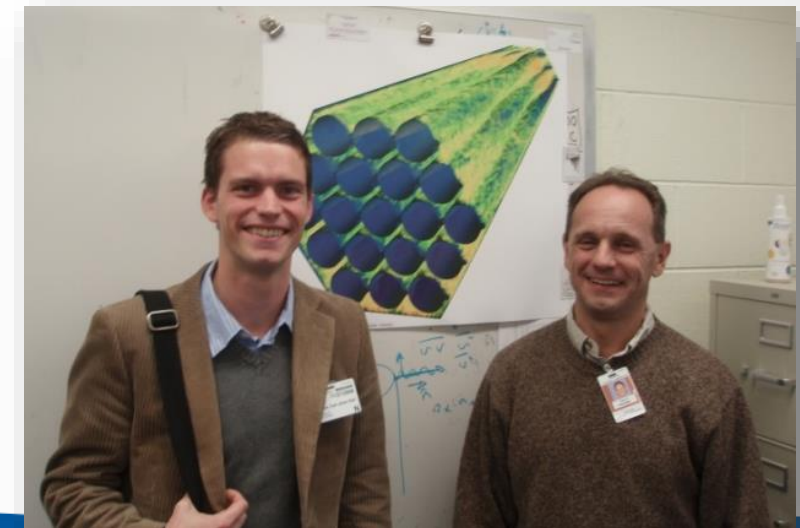


# Nek5000 – Spectral Elements (CG)

- SEM code by **Paul F. Fischer**, Argonne National Lab, USA  
Open source: `nek5000.mcs.anl.gov`
- 80 000 lines of **Fortran 77** (some C for I/O), MPI (no hybrid)
- **Gordon Bell Prize 1999** for algorithmic quality and performance
- **KISS** ("Keep it simple, stupid") – world's most powerful computers have very weak operating systems
- **EU Projects on algorithms** (CRESTA, ExaFLOW, Excellerat ...):  
adaptive meshing, GPUs, ...



- Good scaling up to **1,000,000** ranks  
on **Mira** (10PFlops BG/Q)





# ExaFLOW Team



Imperial College  
London



UNIVERSITY OF  
Southampton

Universität Stuttgart



asc(s)  
Automotive Simulation Center Stuttgart

epcc



- Address current **algorithmic** bottlenecks to enable the use of **accurate CFD codes** for problems of practical **engineering interest**.
- With: Imperial College, Southampton, Uni Stuttgart, Uni Edinburgh, EPFL, McLaren Racing, ASCS







# Outline

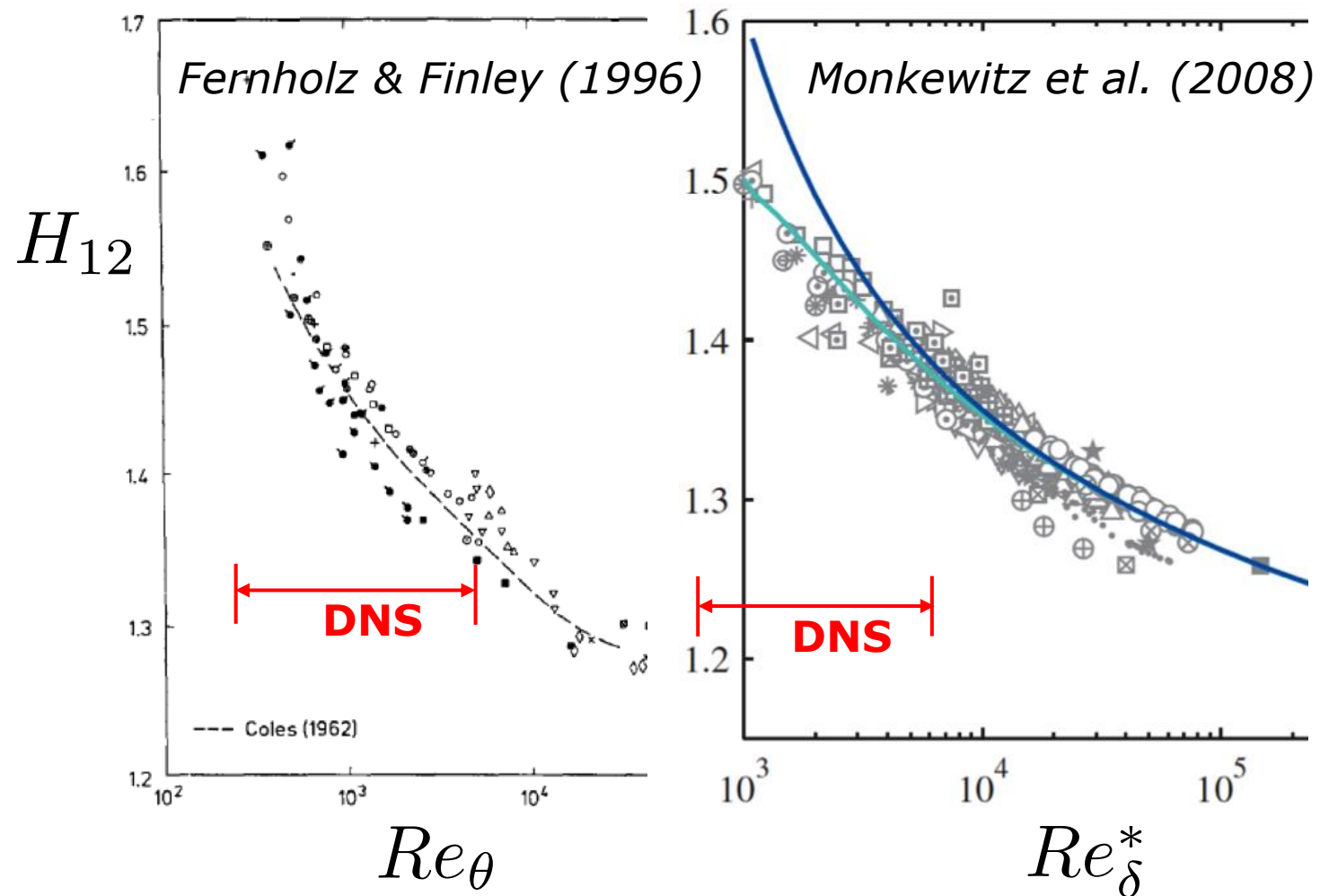
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# What we are used/expect to see ...



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Compilation/  
Assessment of  
experimental data  
from ZPG TBL flows



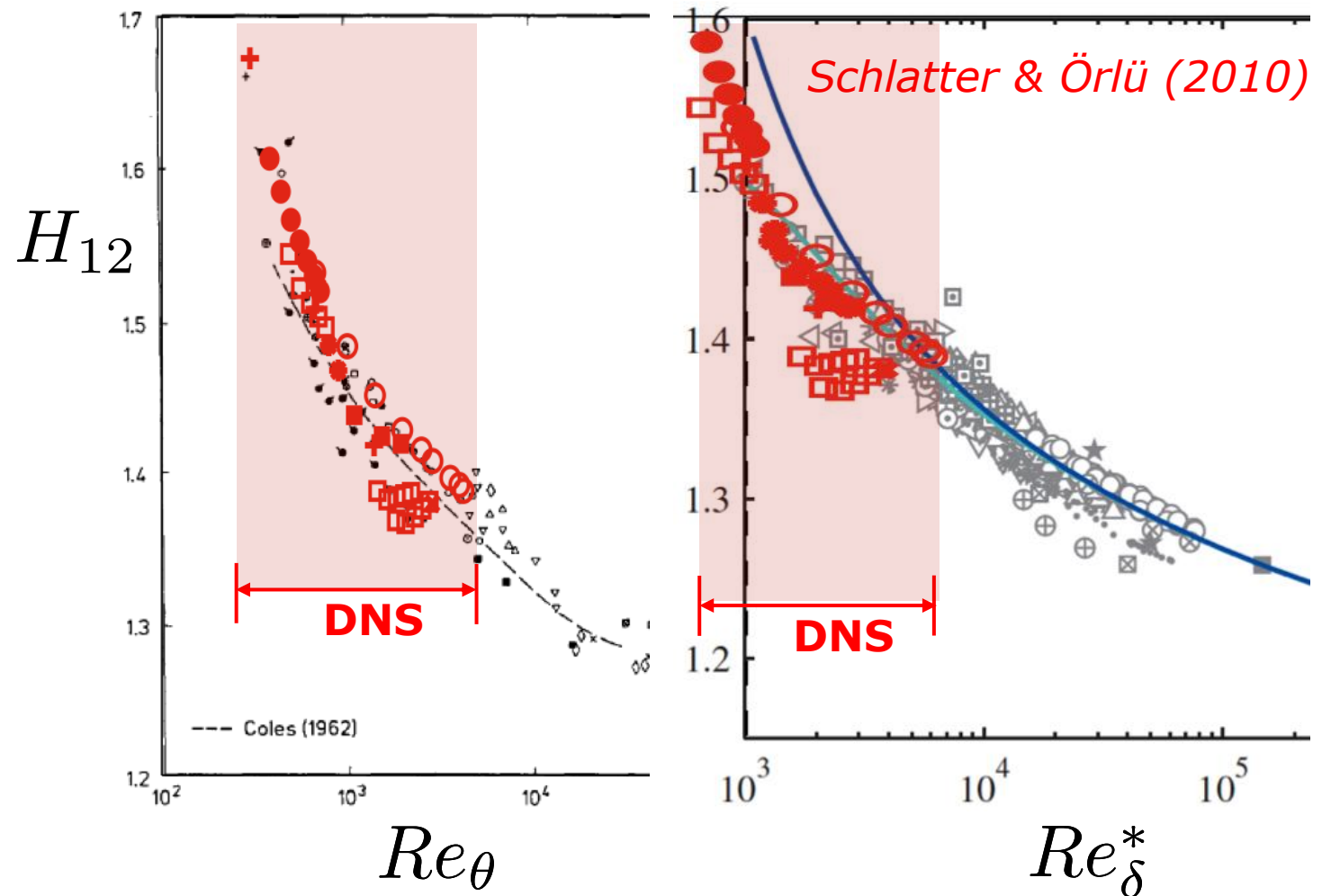
**Physical experiments** are commonly scrutinised before they are employed to calibrate, test, or validate other experiments, scaling laws or theories

# ... and what “we” are not so used to see

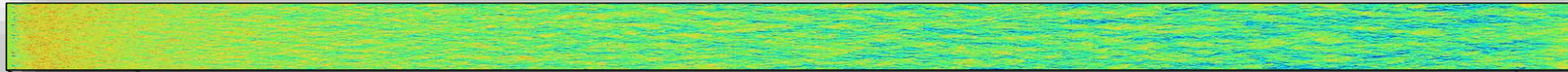


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Red symbols are  
data from 7  
independent DNS  
from ZPG TBL flows

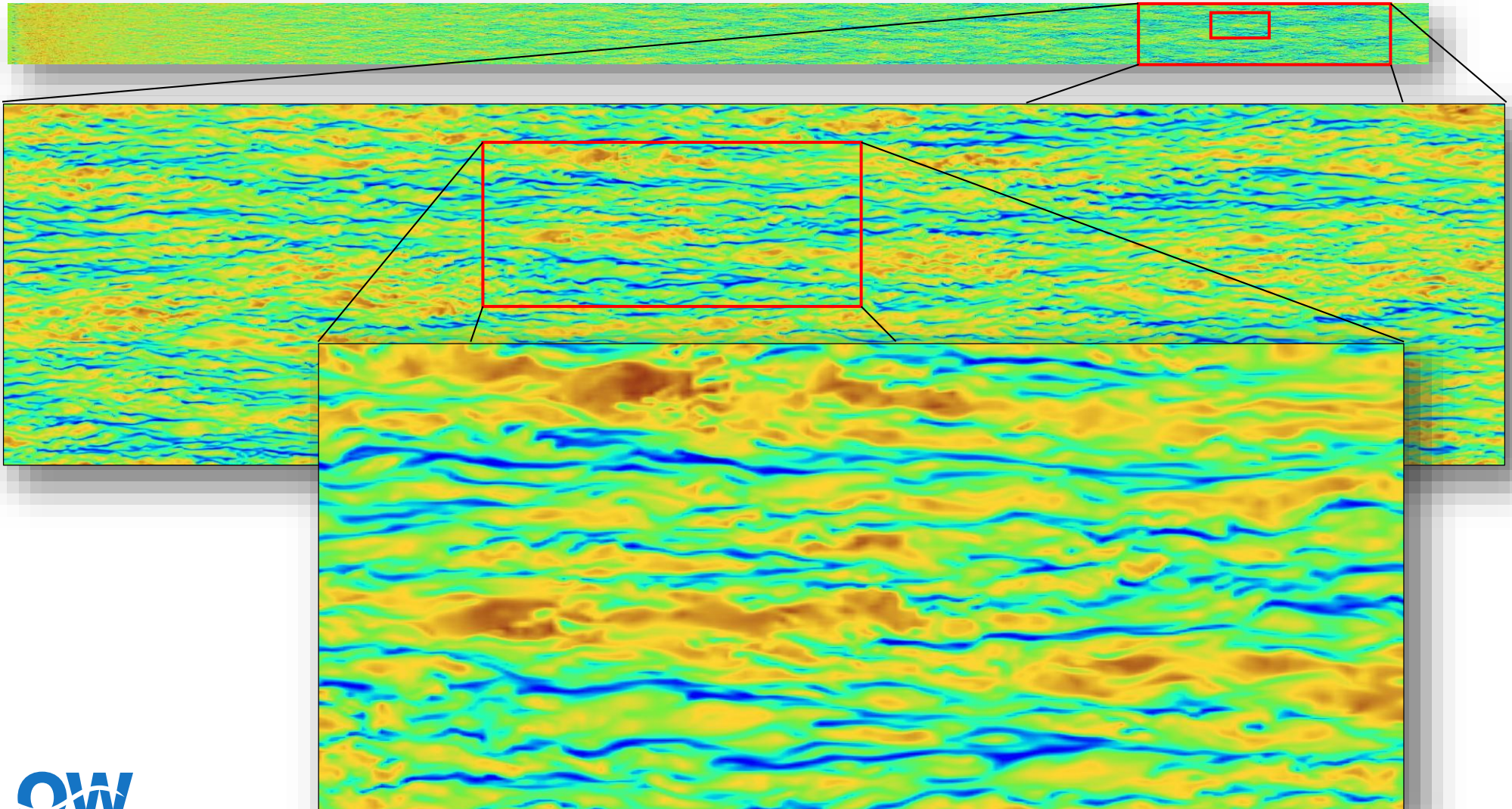


**Simulation data** are hardly scrutinised, when it comes to basic (integral) quantities



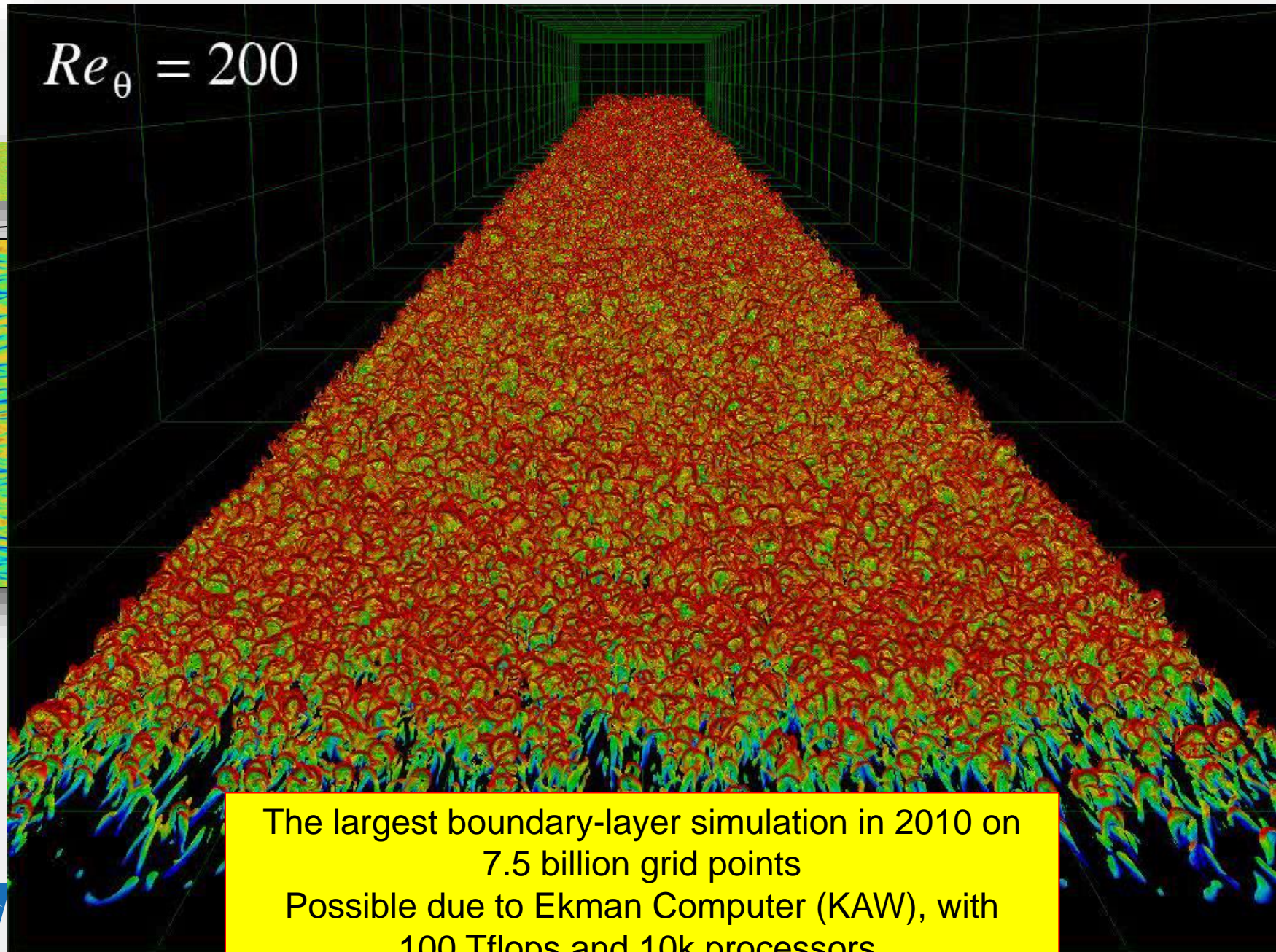


simulation result





# Turbulent flow close to solid walls...



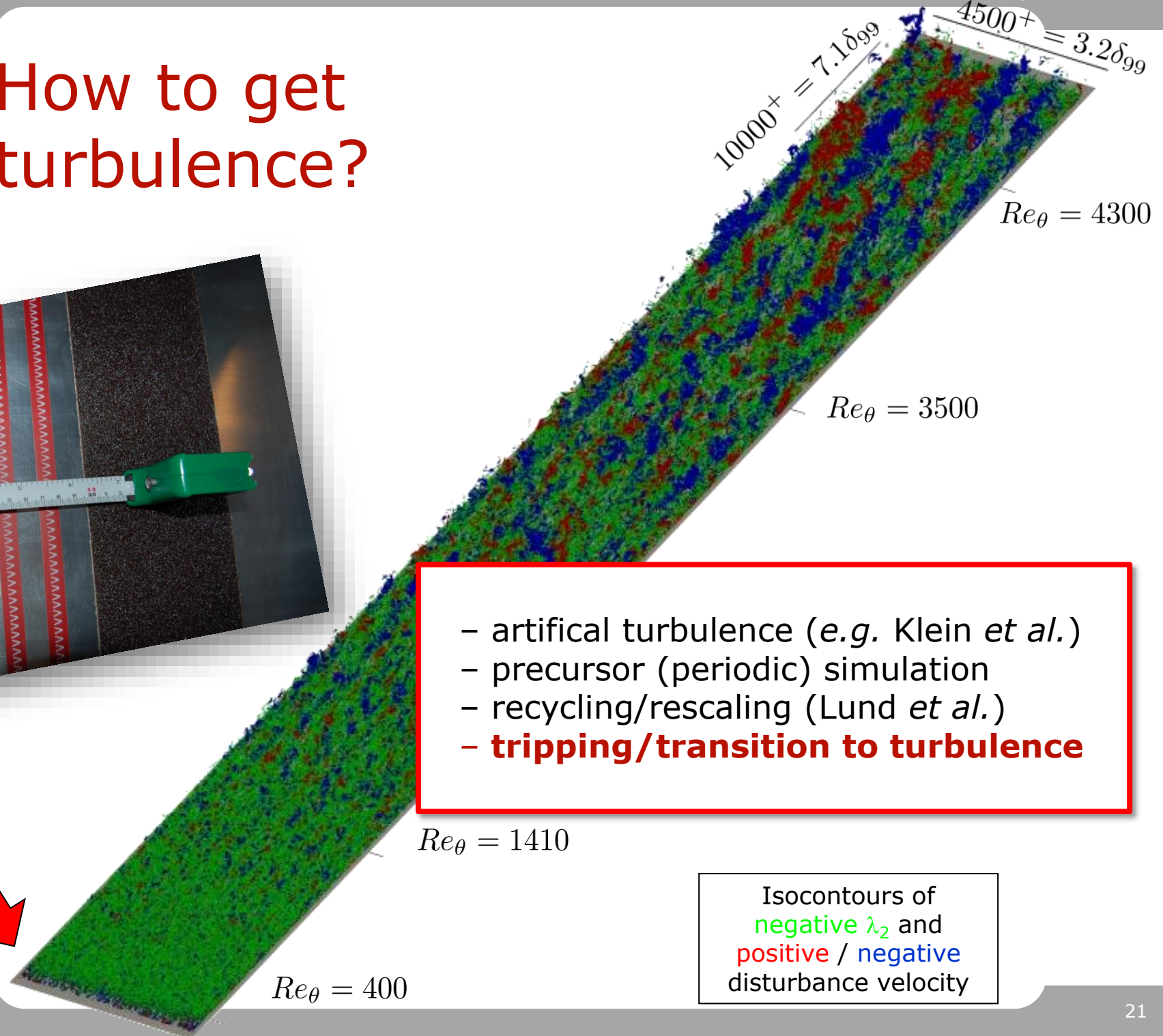
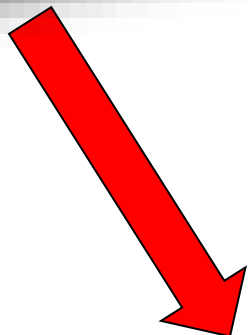
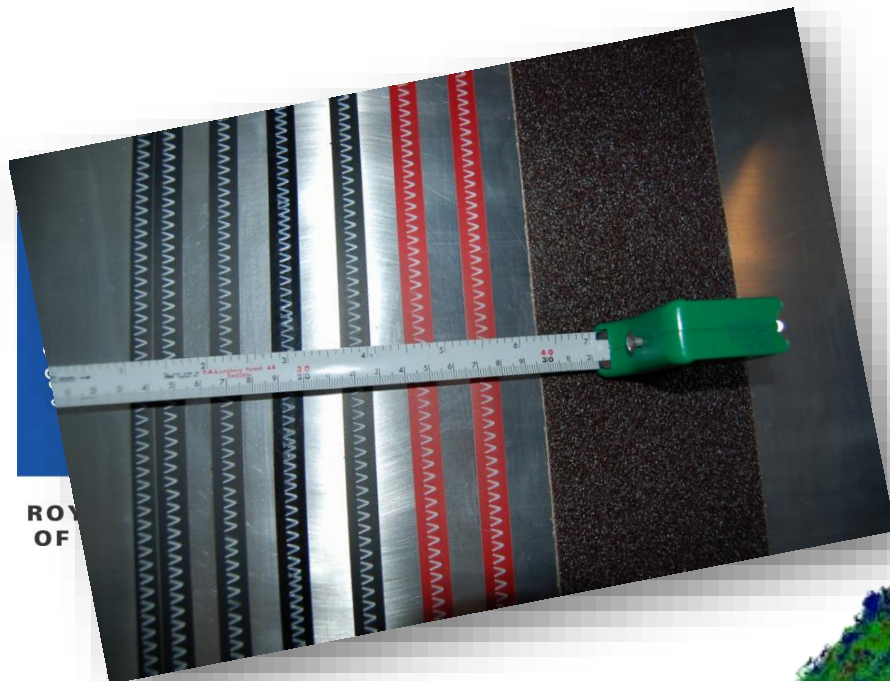
# How to get turbulence?



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# How to get turbulence?



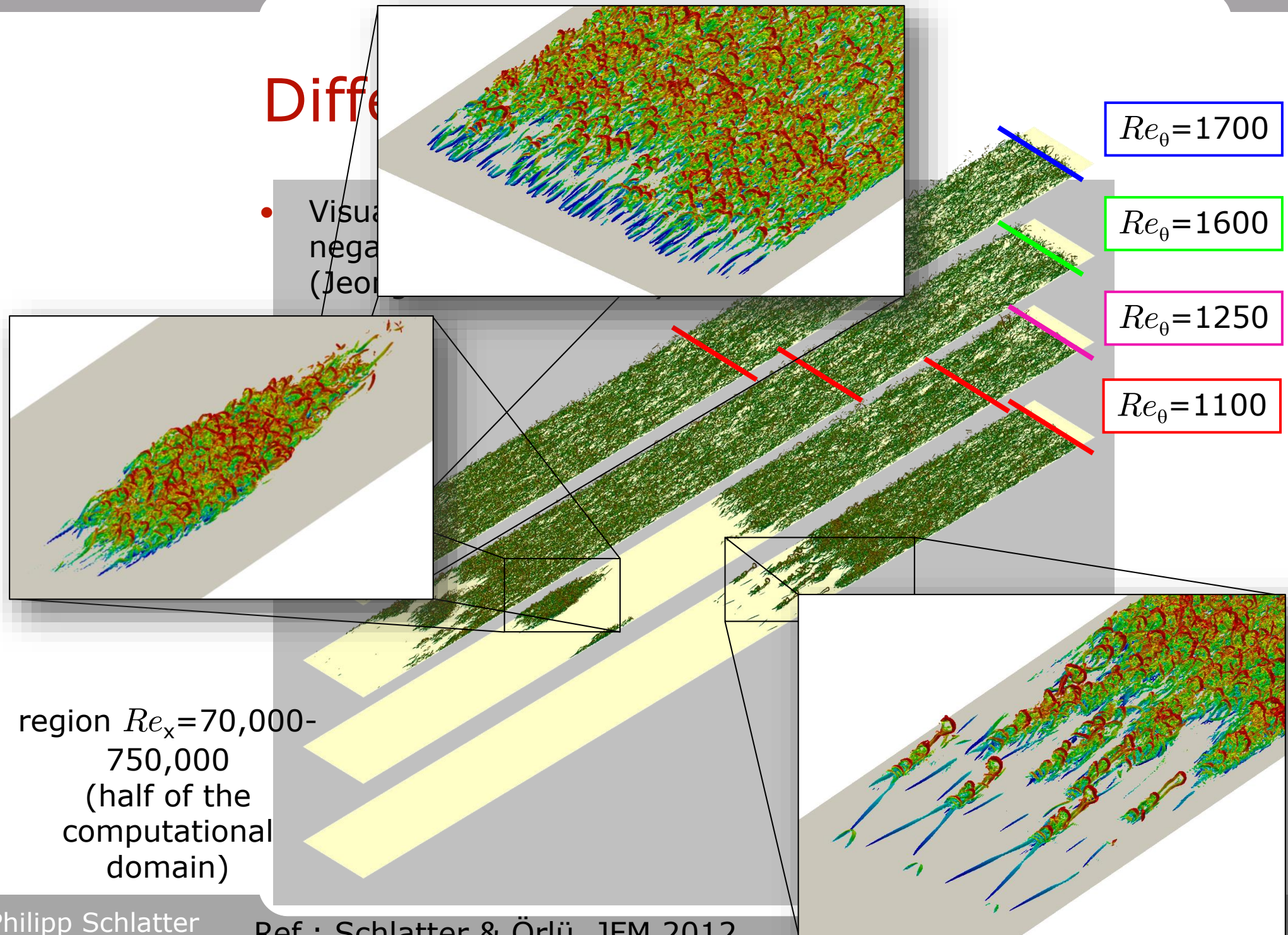
- artificial turbulence (e.g. Klein *et al.*)
- precursor (periodic) simulation
- recycling/rescaling (Lund *et al.*)
- **tripping/transition to turbulence**

Isocontours of  
negative  $\lambda_2$  and  
positive / negative  
disturbance velocity



# Diff

- Visual  
nega  
(Jeon)





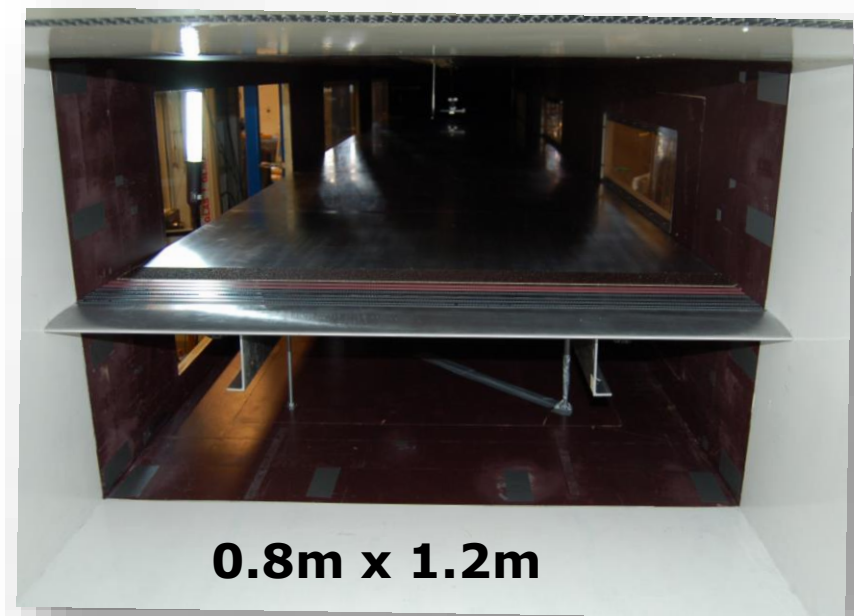
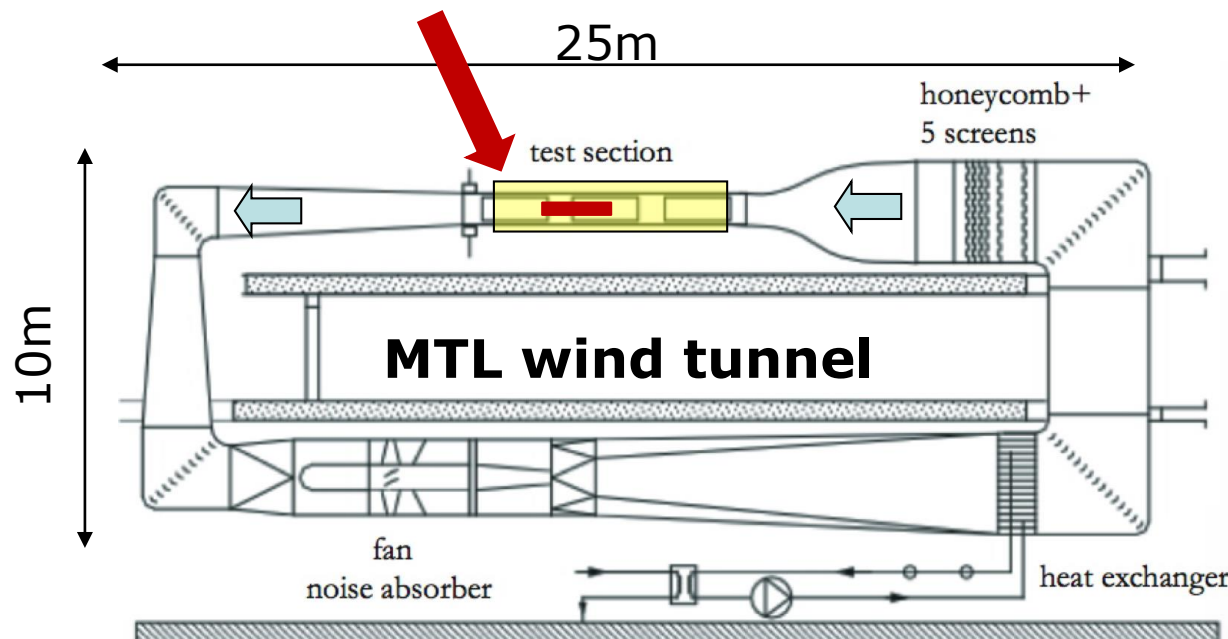
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Let's compare DNS and  
experiments...



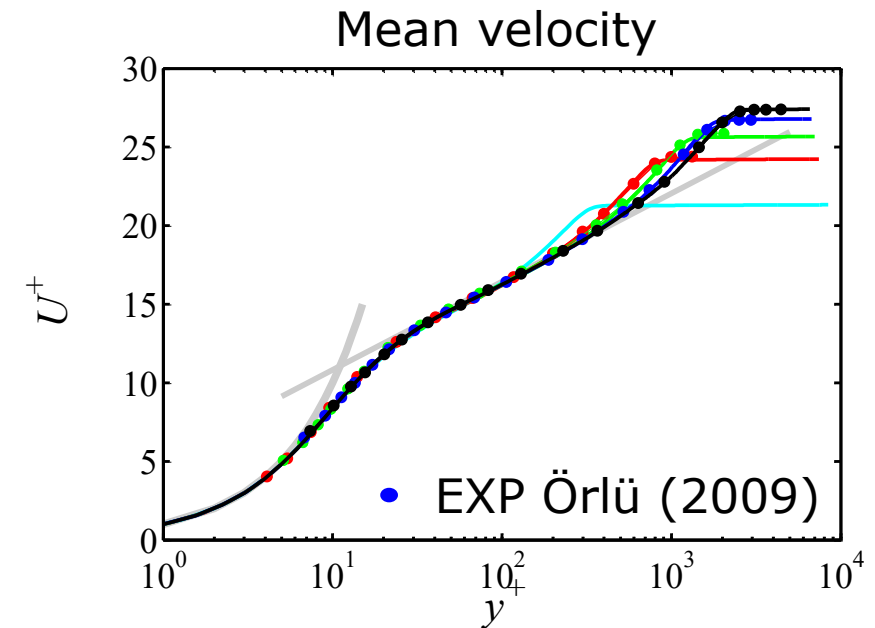
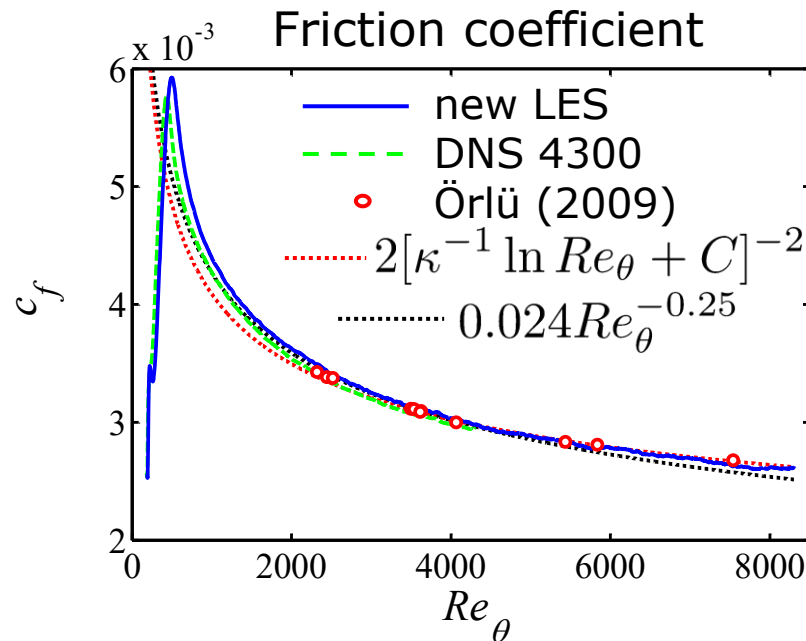
# New experiments at KTH

- ZPG TBL flow in the range  $2300 < Re_\theta < 7500$  (Örlü, 2009)
  - single hot-wire measurements at 1.65m from leading edge of a 7m long plate fulfilling “**equilibrium**” criteria (*à la Chauhan et al. 2009*)
  - independent skin friction measurements by means of **oil-film interferometry**
  - **DNS** corresponds to a 2m stretch... —



# TBL LES up to $Re_\theta = 8300$

- **Ongoing** LES (using ADM-RT)



Domain:  $13500 \times 400 \times 540\delta_0^*$   
 $Re_\theta = 500-8300$  ;  $Re_\tau = 2500$

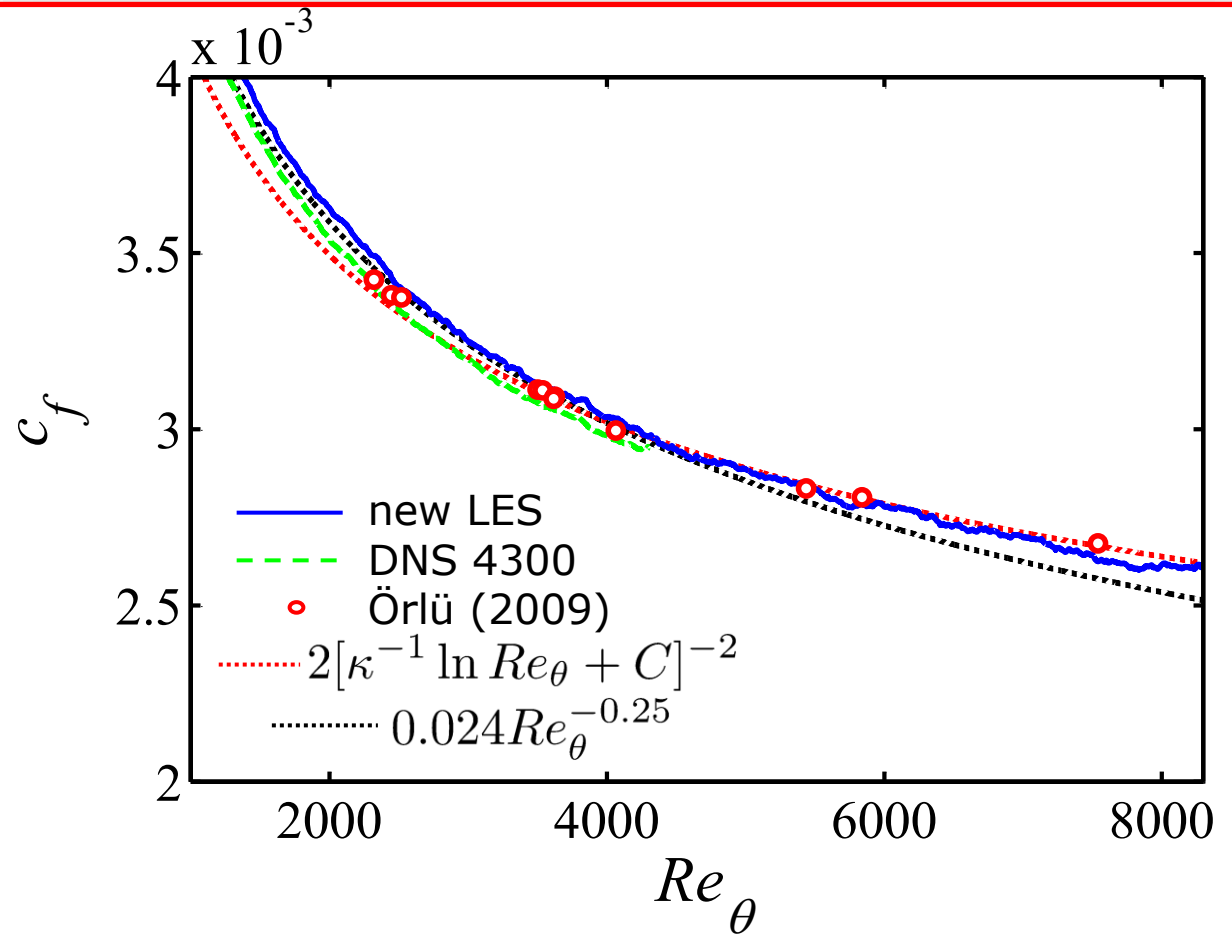
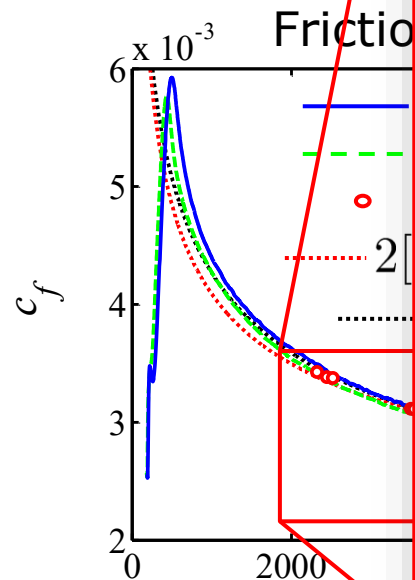
Resolution:  $9216 \times 513 \times 768$   
 (8.5 billion grid points)  
 $\Delta x^+ = 18$ ,  $\Delta y^+ = 0.06-16$ ,  $\Delta z^+ = 8$

—  $Re_\theta = 1000$   
 —  $Re_\theta = 2500$   
 —  $Re_\theta = 4000$   
 —  $Re_\theta = 5800$   
 —  $Re_\theta = 7500$



# TBL LES

- Ongoing LES



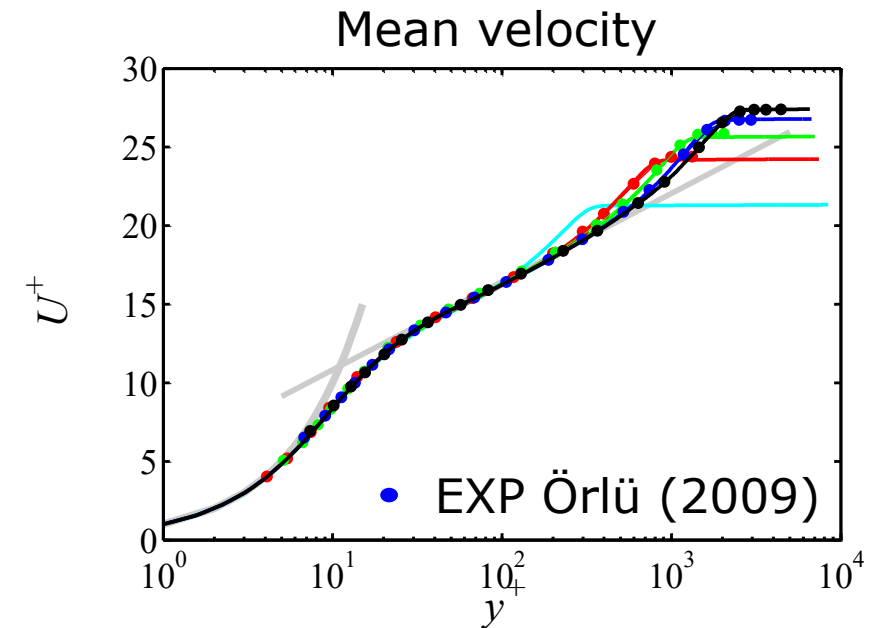
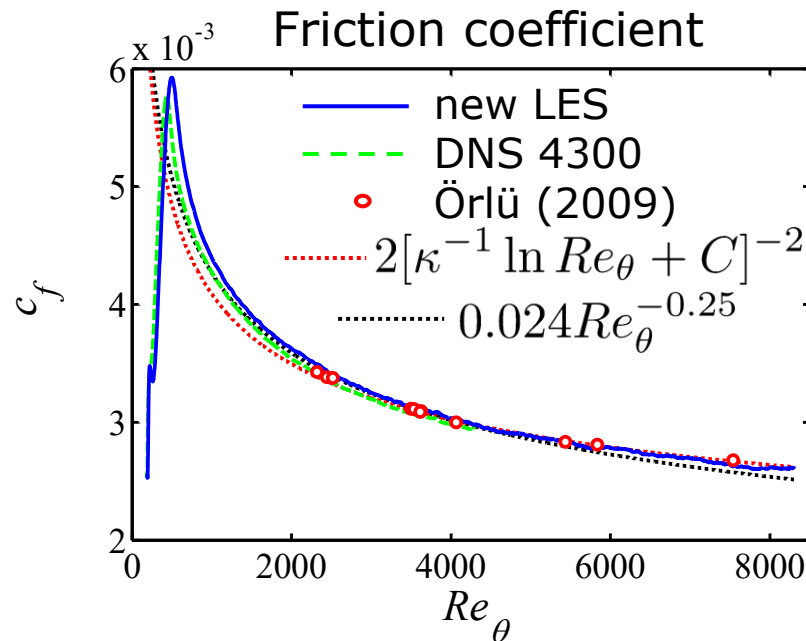
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 —  $Re_\theta = 7500$

# TBL LES up to $Re_\theta = 8300$

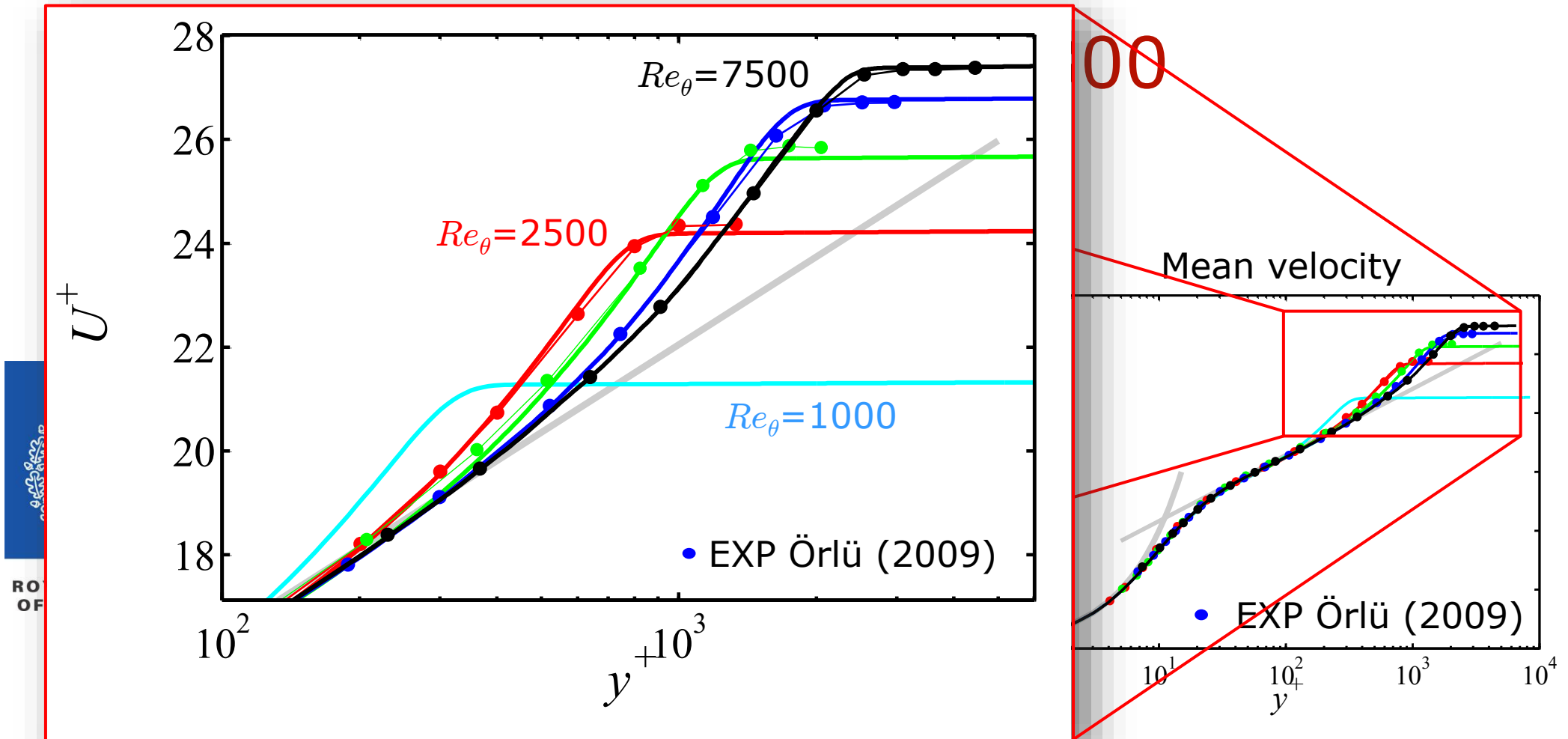
- **Ongoing** LES (using ADM-RT)



Domain:  $13500 \times 400 \times 540\delta_0^*$   
 $Re_\theta = 500-8300$  ;  $Re_\tau = 2500$

Resolution:  $9216 \times 513 \times 768$   
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 $\Delta x^+ = 18$ ,  $\Delta y^+ = 0.06-16$ ,  $\Delta z^+ = 8$

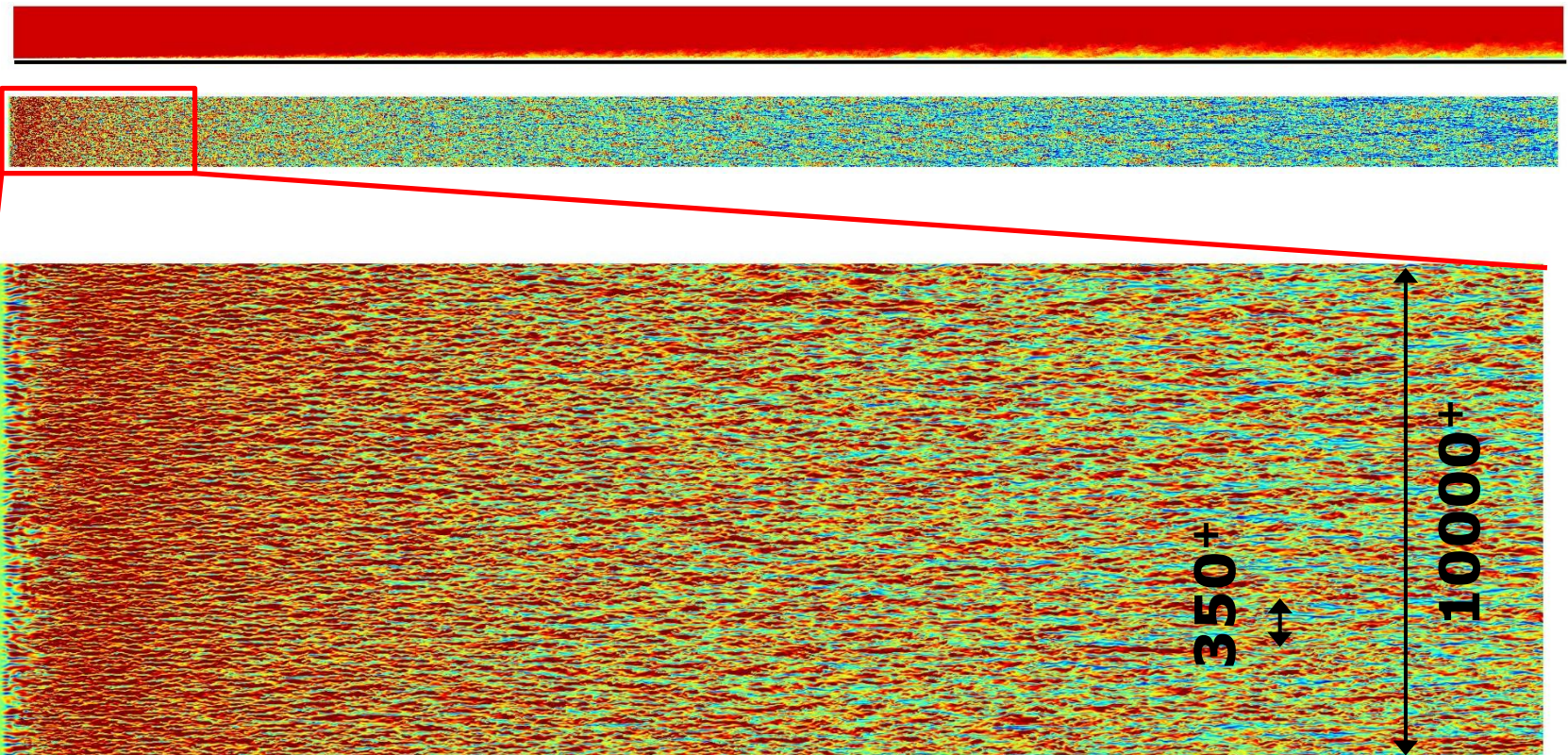
—  $Re_\theta = 1000$   
 —  $Re_\theta = 2500$   
 —  $Re_\theta = 4000$   
 —  $Re_\theta = 5800$   
 —  $Re_\theta = 7500$





# Visualisation

- Streamwise velocity  $u$  in wall-parallel plane  $y^+ \approx 15$

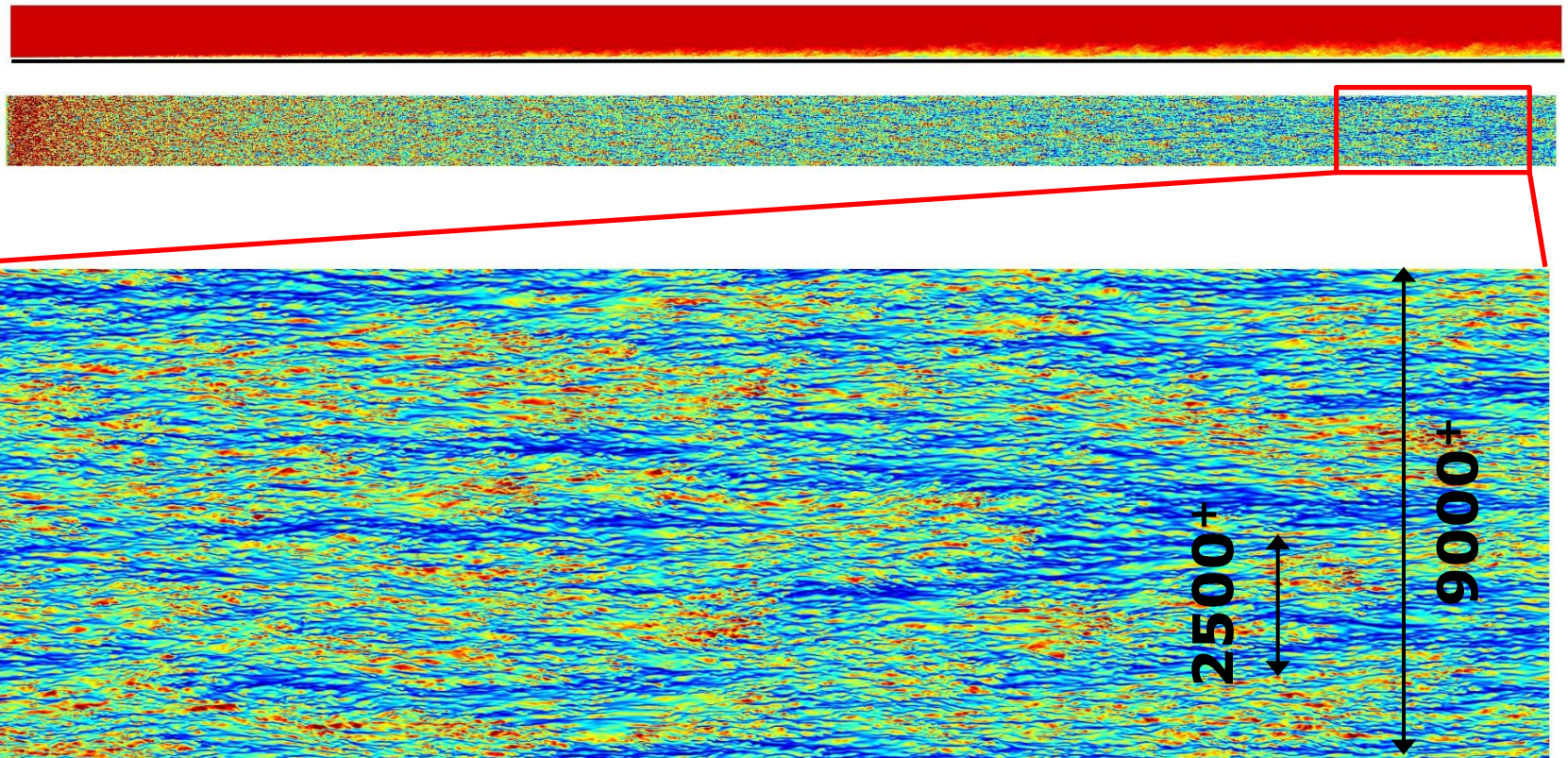


$$Re_\theta = 180-1400 \quad Re_\tau = 350$$



# Visualisation

- Streamwise velocity  $u$  in wall-parallel plane  $y^+ \approx 15$



$$Re_\theta = 8300 \quad Re_\tau = 2500$$



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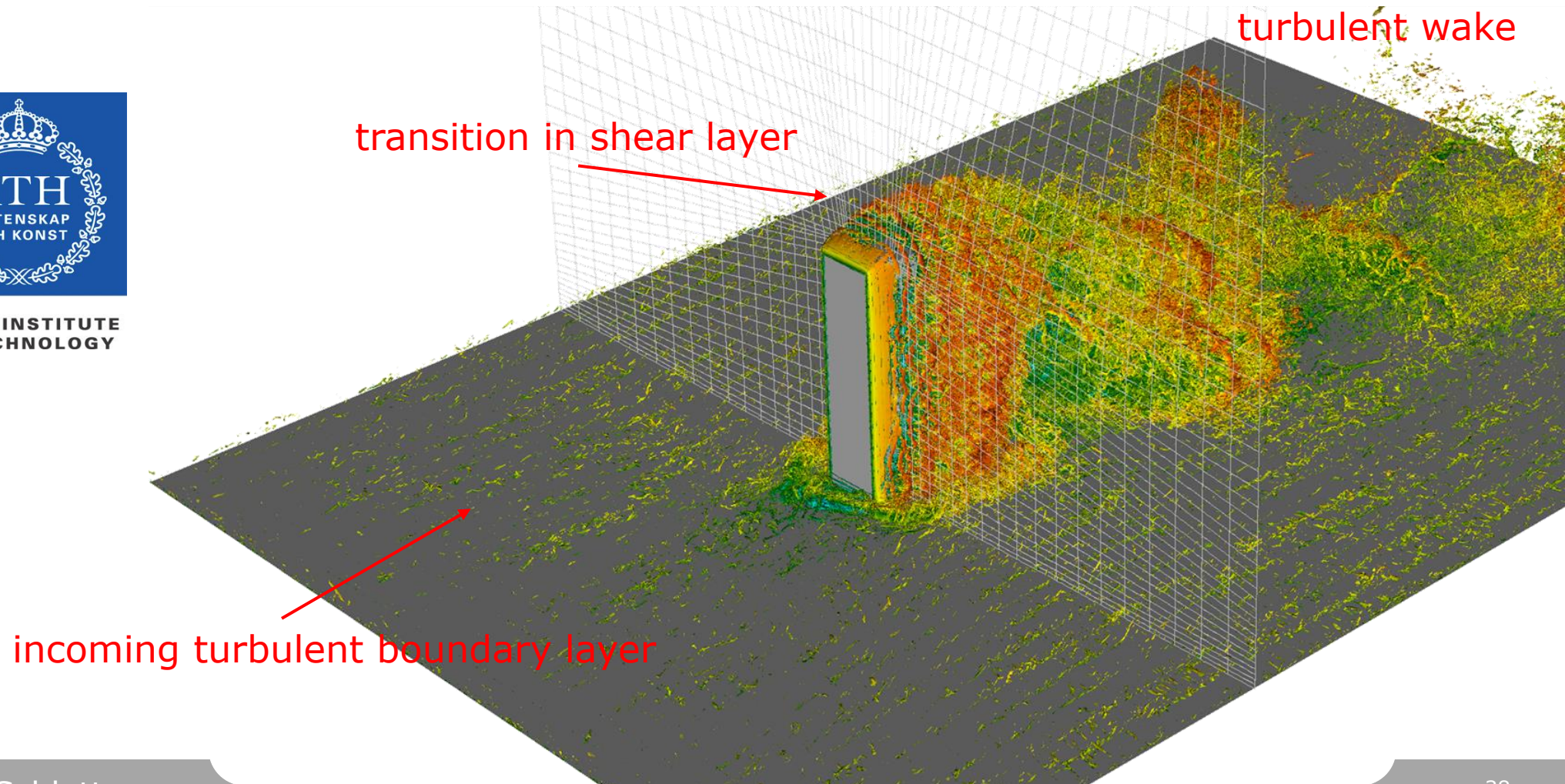


# TBL with "obstacles"

- "Skyscraper" reference case: Canadian CFD Challenge (2014)



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# Outline

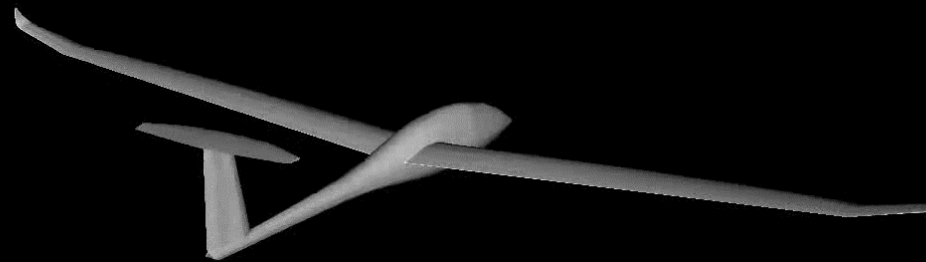
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# DNS of flow around a NACA4412 wing section; $Re_c=400\ 000$ and $AoA=5^\circ$

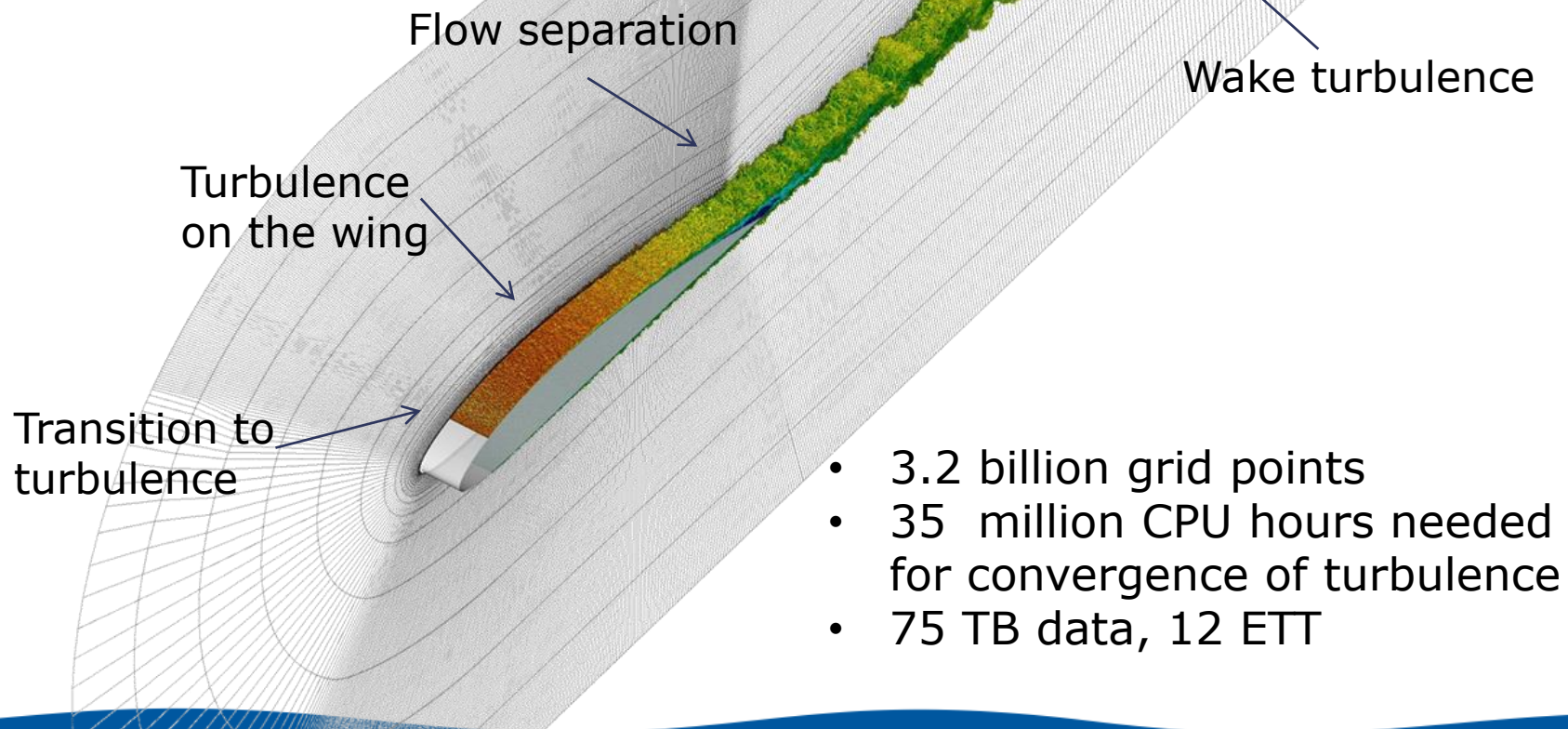
2017...

High-order methods are finding their way into aircraft design procedures, providing accuracy and reducing design risks, particularly for turbulent flow with regions of flow separation.



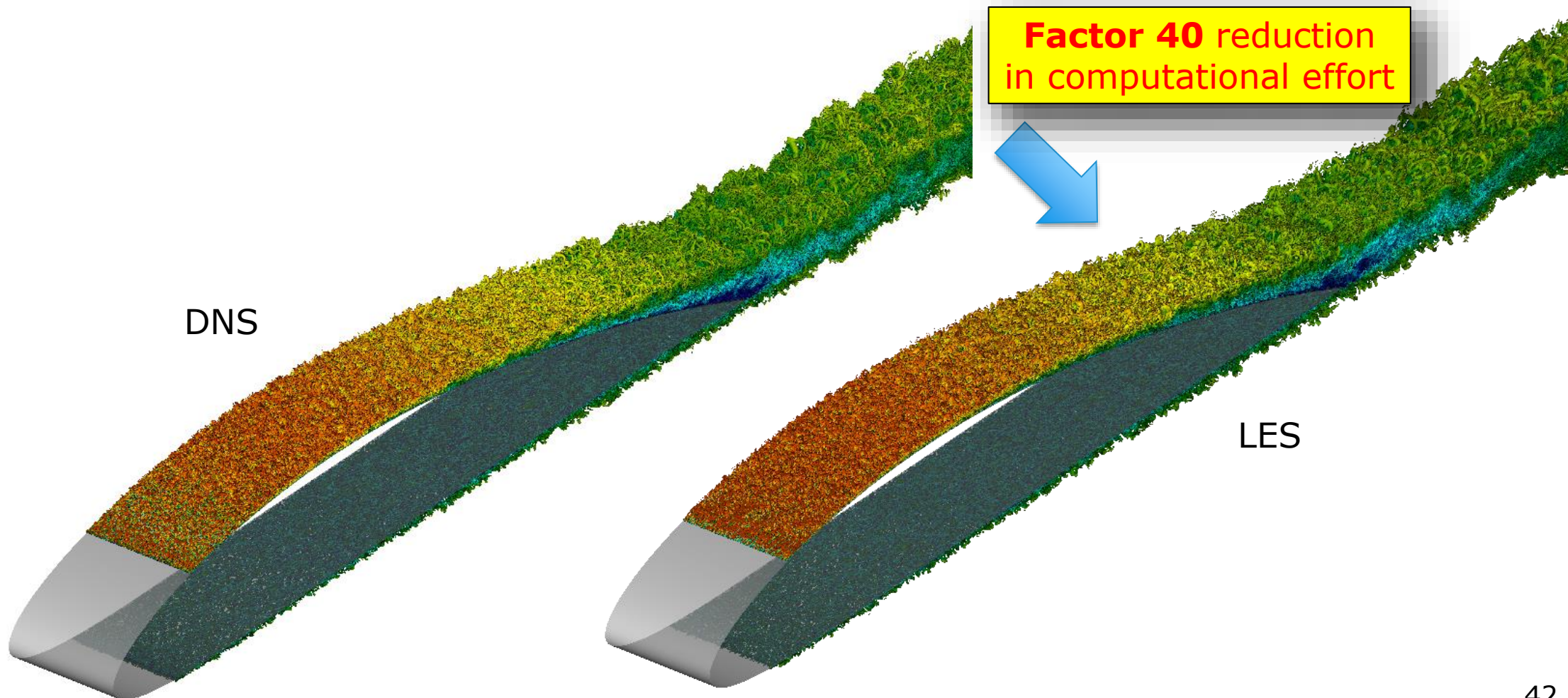
# Direct numerical simulation of flow over a full NACA4412 wing at $Re_c = 400\,000$

- DNS with Nek5000
- $Re_\tau=400$ ,  $Re_\theta=2800$
- AoA=5 deg.
- $z_L=10\%$  chord



# LES towards $Re = 1M$ and beyond...

- Similar approach as Eitel-Amor *et al.* (2014) based on **relaxation filtering** (Schlatter *et al.* 2005)





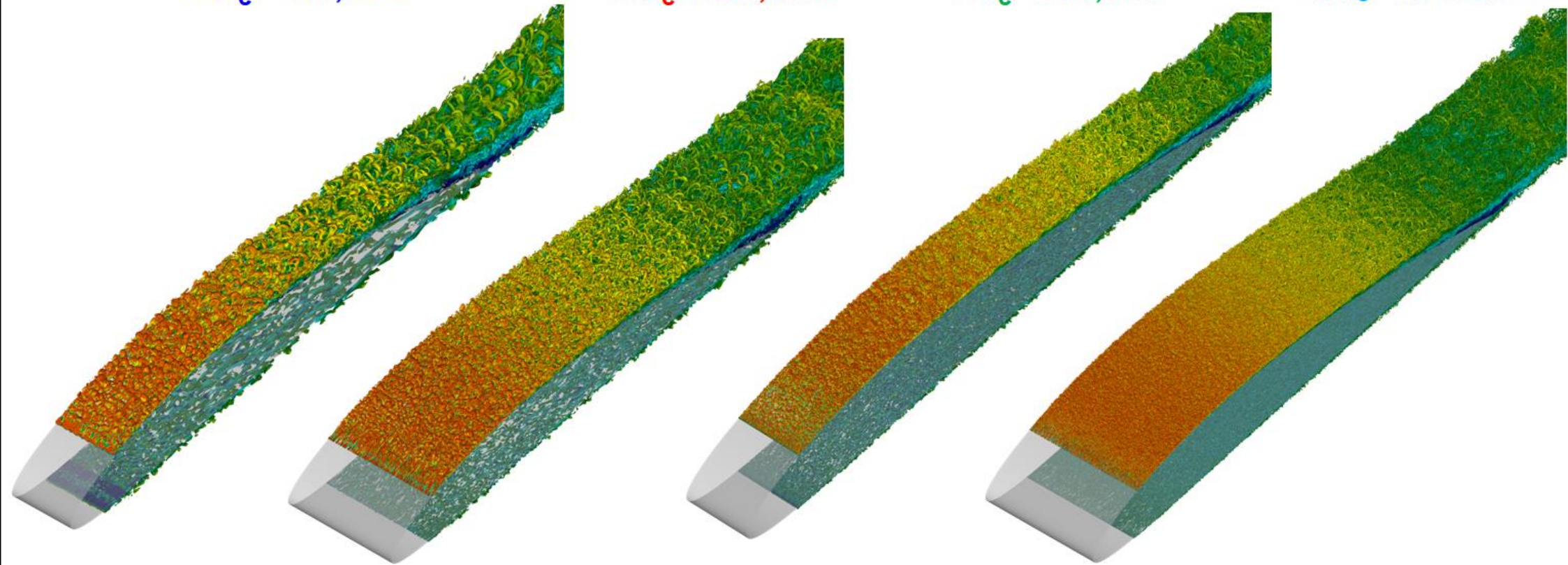
# Four different wings...

$Re_c=100,000$

$Re_c=200,000$

$Re_c=400,000$

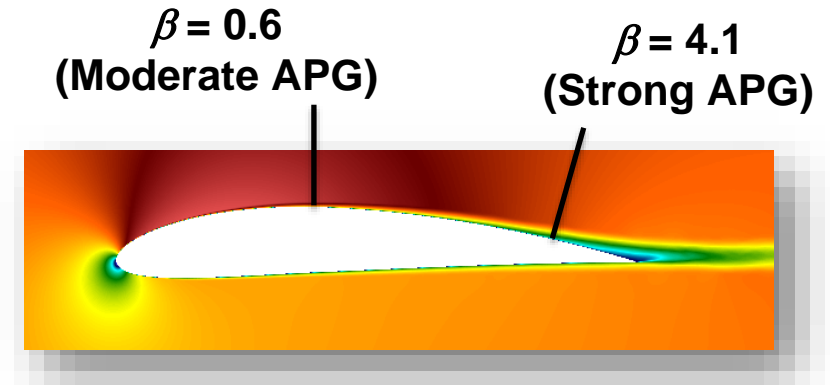
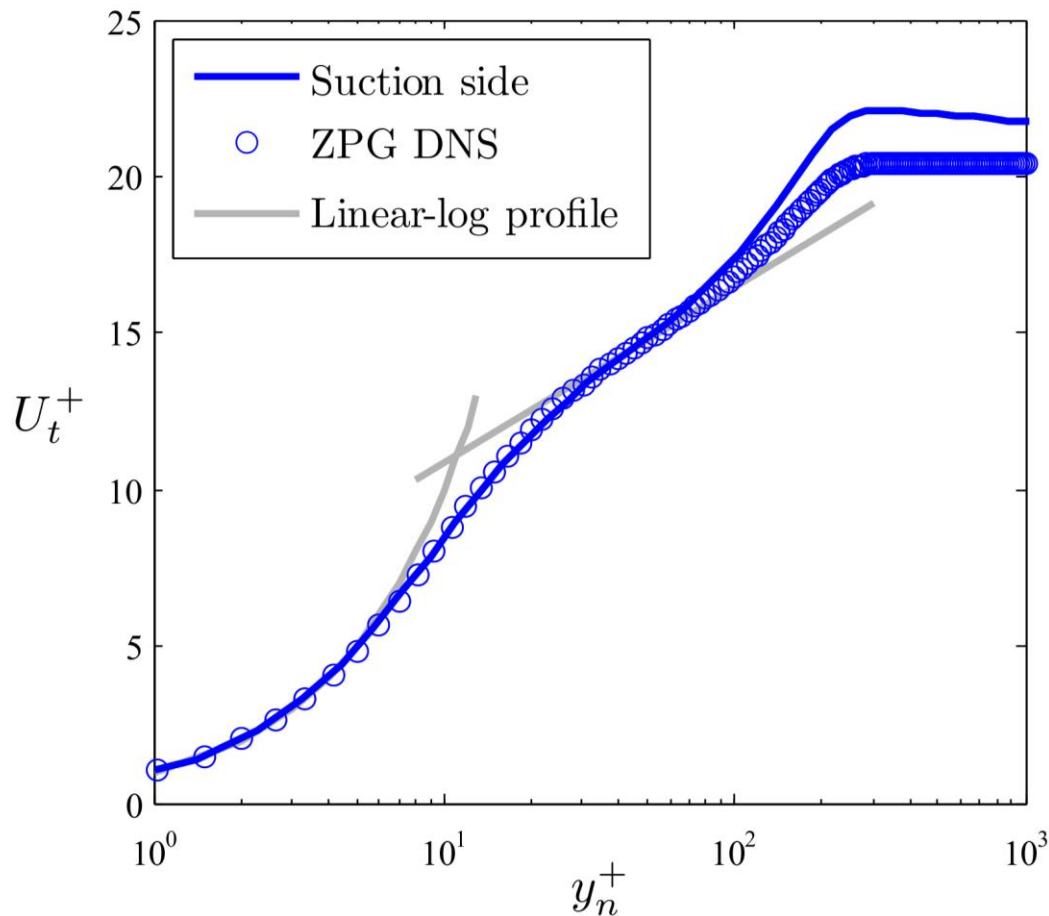
$Re_c=1,000,000$





# Mean velocity profiles

- Inner-scaled **mean flow** at  $x/c=0.4$ .

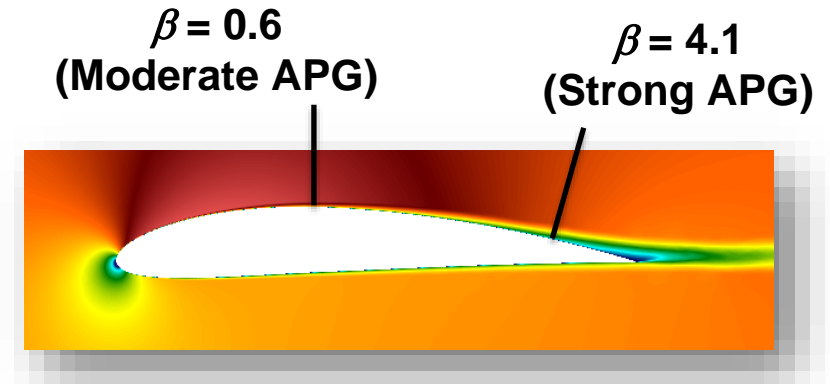
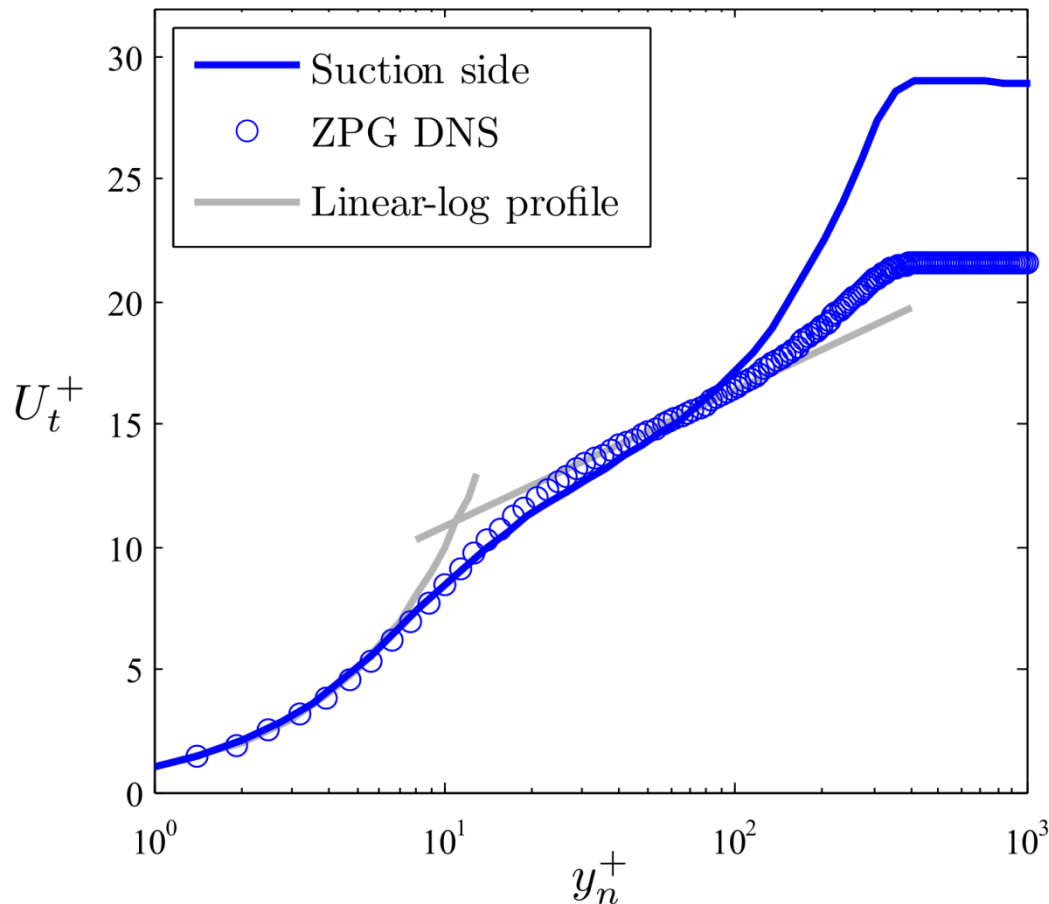


- Effect on the outer part, more prominent wake

Parameter	At $x/c=0.4$	ZPG (S&Ö)
$Re_\tau$	242	252
$Re_\theta$	712	678
H	<b>1.59</b>	<b>1.47</b>
$C_f$	$4.1 \times 10^{-3}$	$4.8 \times 10^{-3}$
$\kappa$	0.38	0.42
B	4.20	5.09
$\Pi$	0.56	0.31

# Mean velocity profiles

- Inner-scaled **mean flow** at  $x/c=0.8$ .

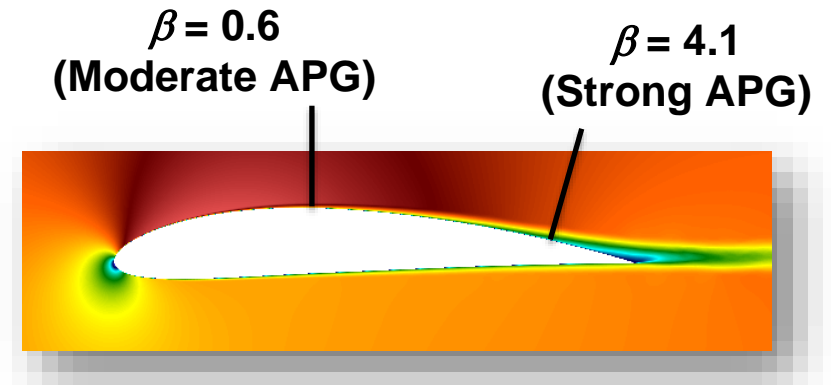
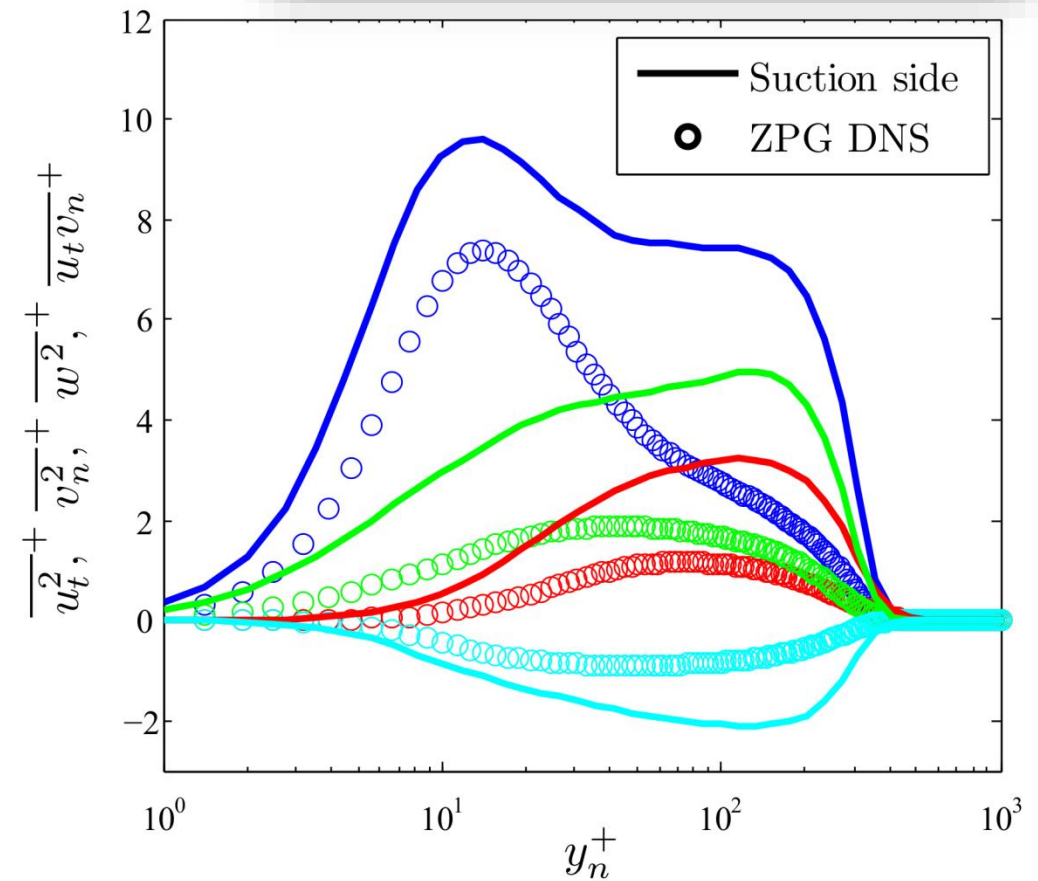
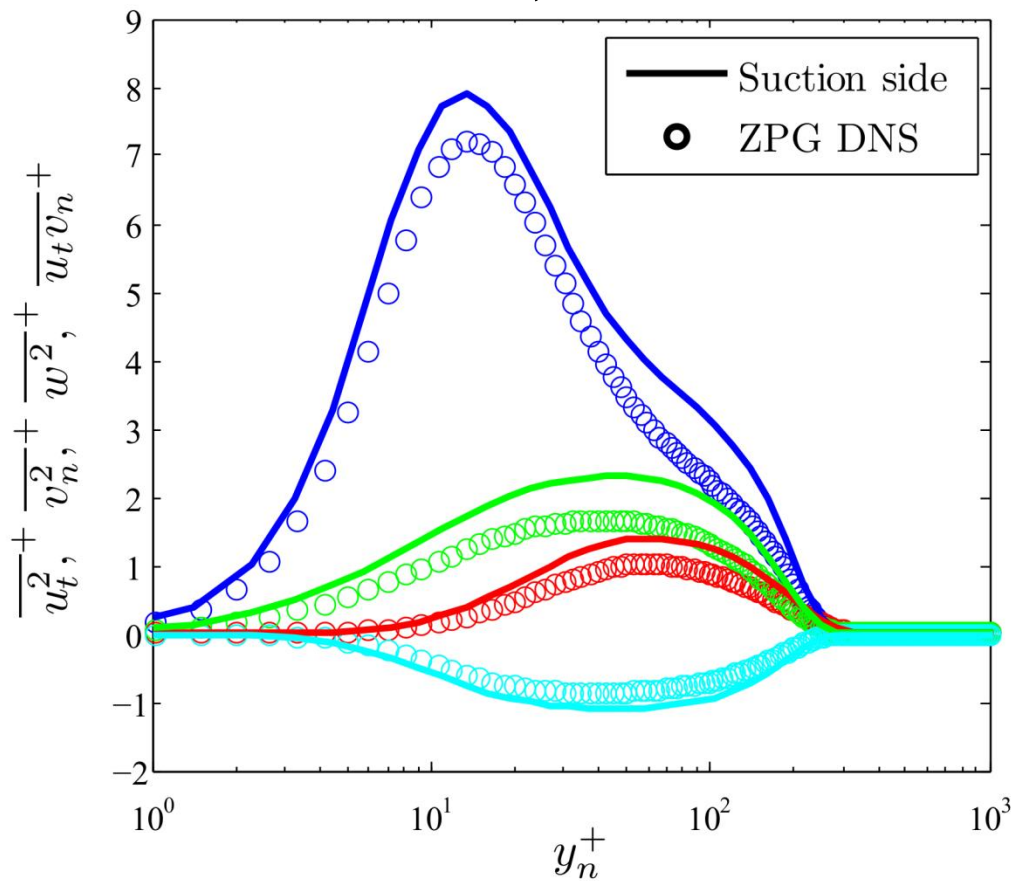


- Effect on the outer part (more prominent wake), but also in the incipient log region and even the buffer layer.

Parameter	At $x/c=0.8$	ZPG (S&Ö)
$Re_\tau$	373	359
$Re_\theta$	1,722	1,007
H	<b>1.74</b>	<b>1.45</b>
$C_f$	<b><math>2.4 \times 10^{-3}</math></b>	<b><math>4.3 \times 10^{-3}</math></b>
$\kappa$	0.33	0.41
B	2.08	4.87
$\Pi$	1.35	0.37

# Reynolds stress tensor components

- Reynolds stress tensor at  $x/c=0.4$  and  $0.8$ .
- Comparison with **ZPG** from Schlatter and Örlü, 2010.



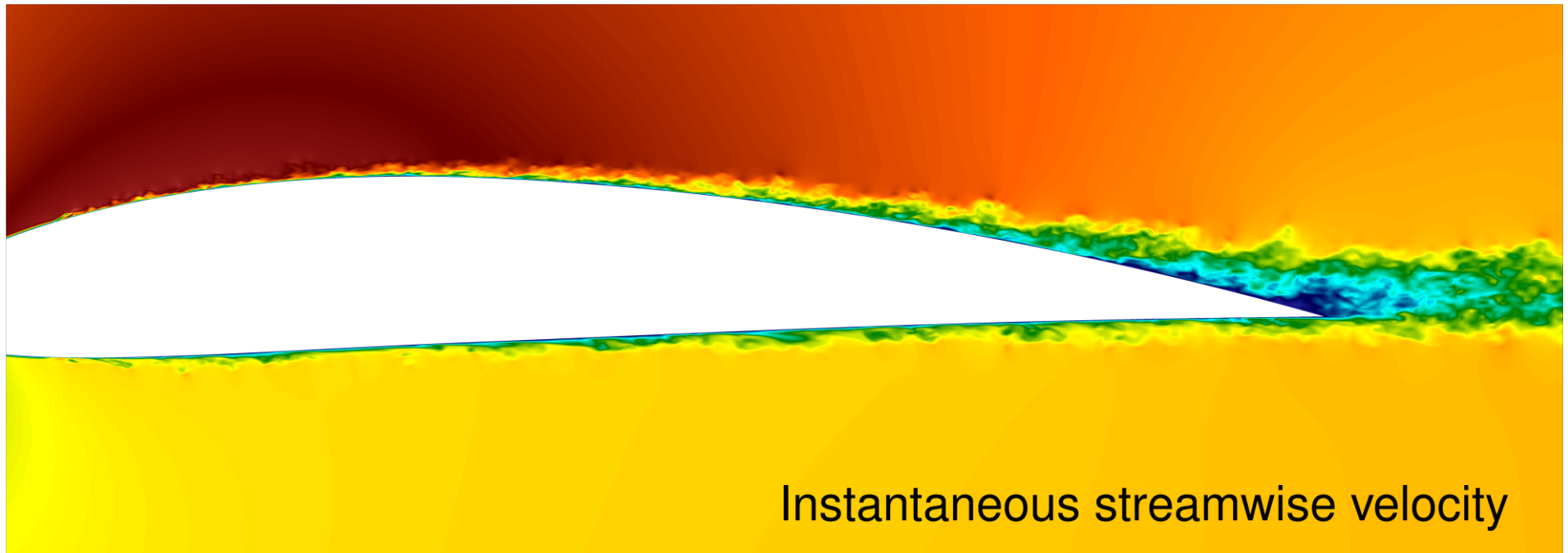


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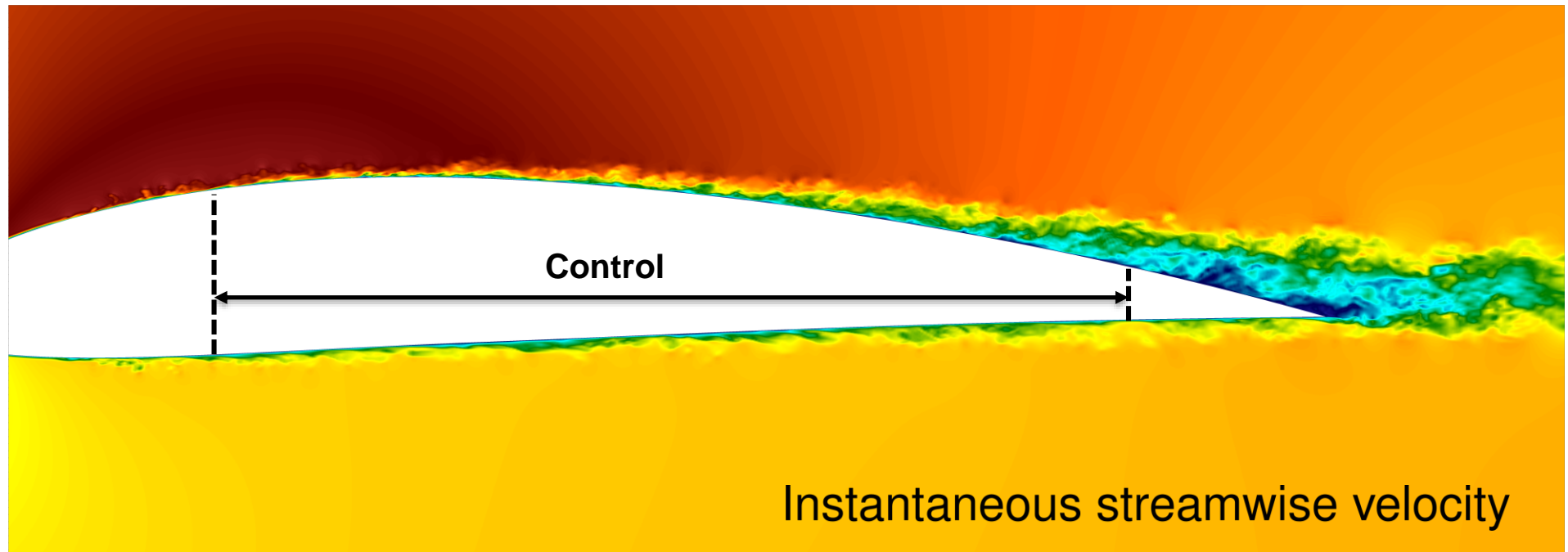


## Considered cases



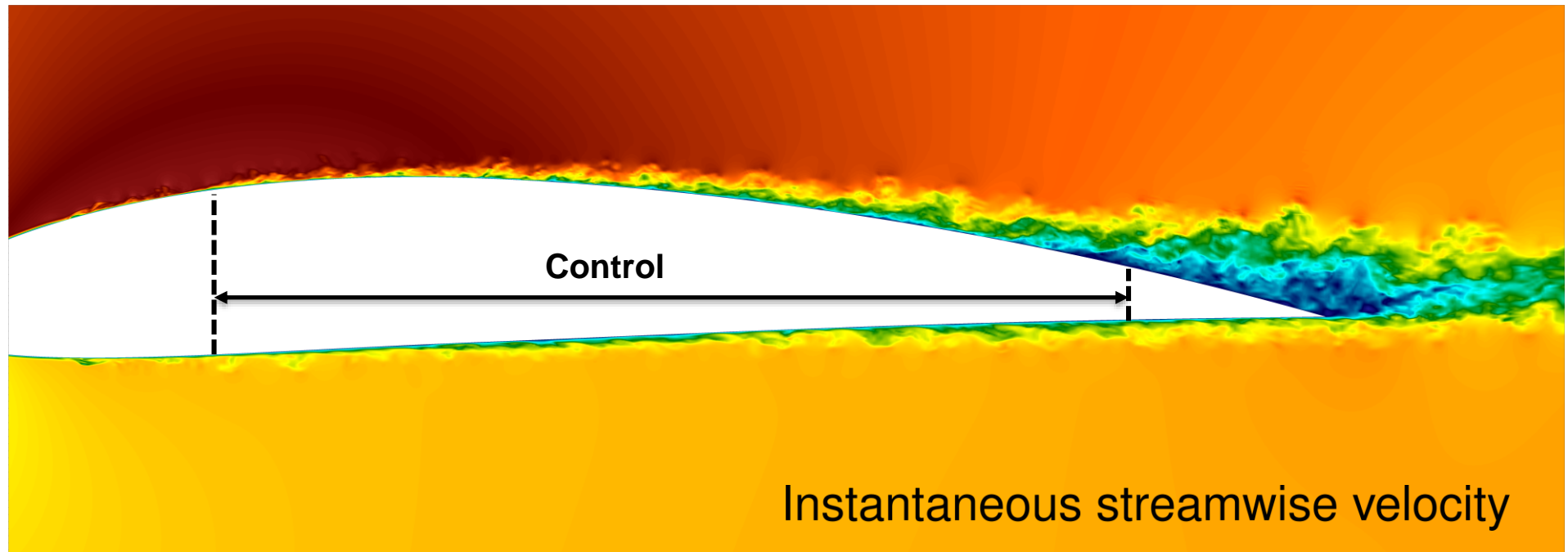
- **Reference case: NACA4412,  $Re_c = 200,000$**
- Controlled case 1: Uniform blowing,  $0.1\%U_\infty$ , at  $0.25 < x_c < 0.86$
- Controlled case 1: Uniform blowing,  $0.2\%U_\infty$ , at  $0.25 < x_c < 0.86$
- Controlled case 1: Uniform suction,  $0.1\%U_\infty$ , at  $0.25 < x_c < 0.86$

## Considered cases



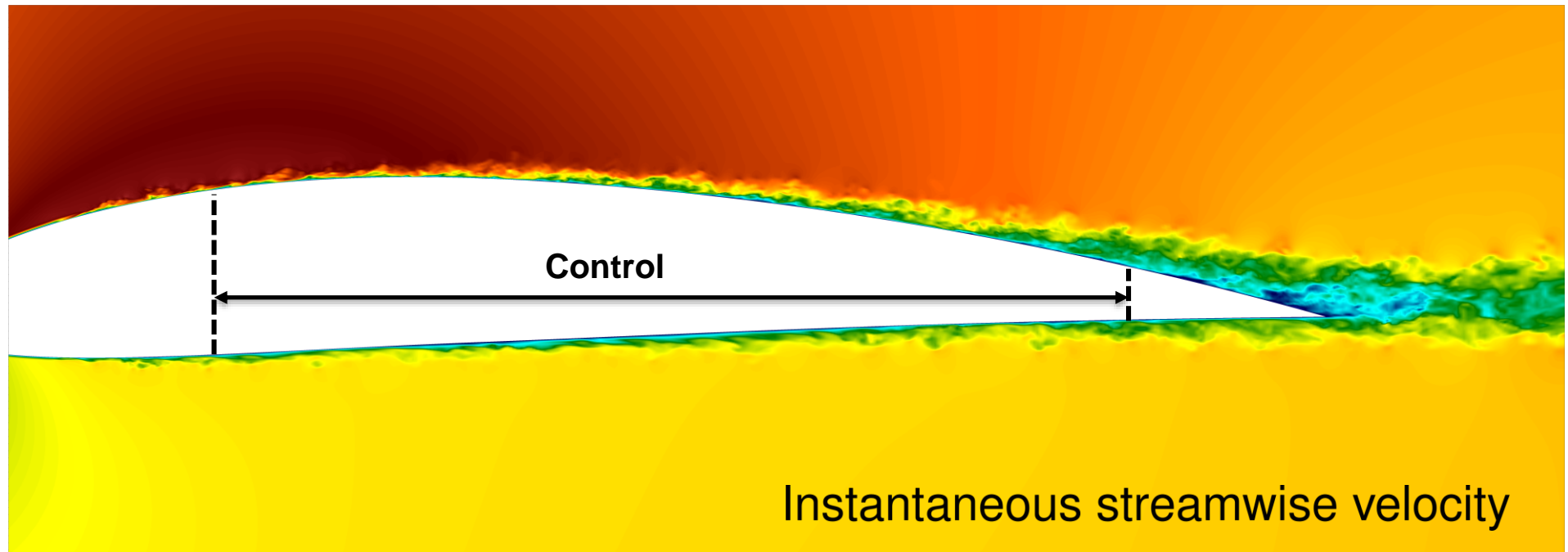
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## Considered cases



- Reference case: NACA4412,  $Re_c = 200,000$
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## Considered cases

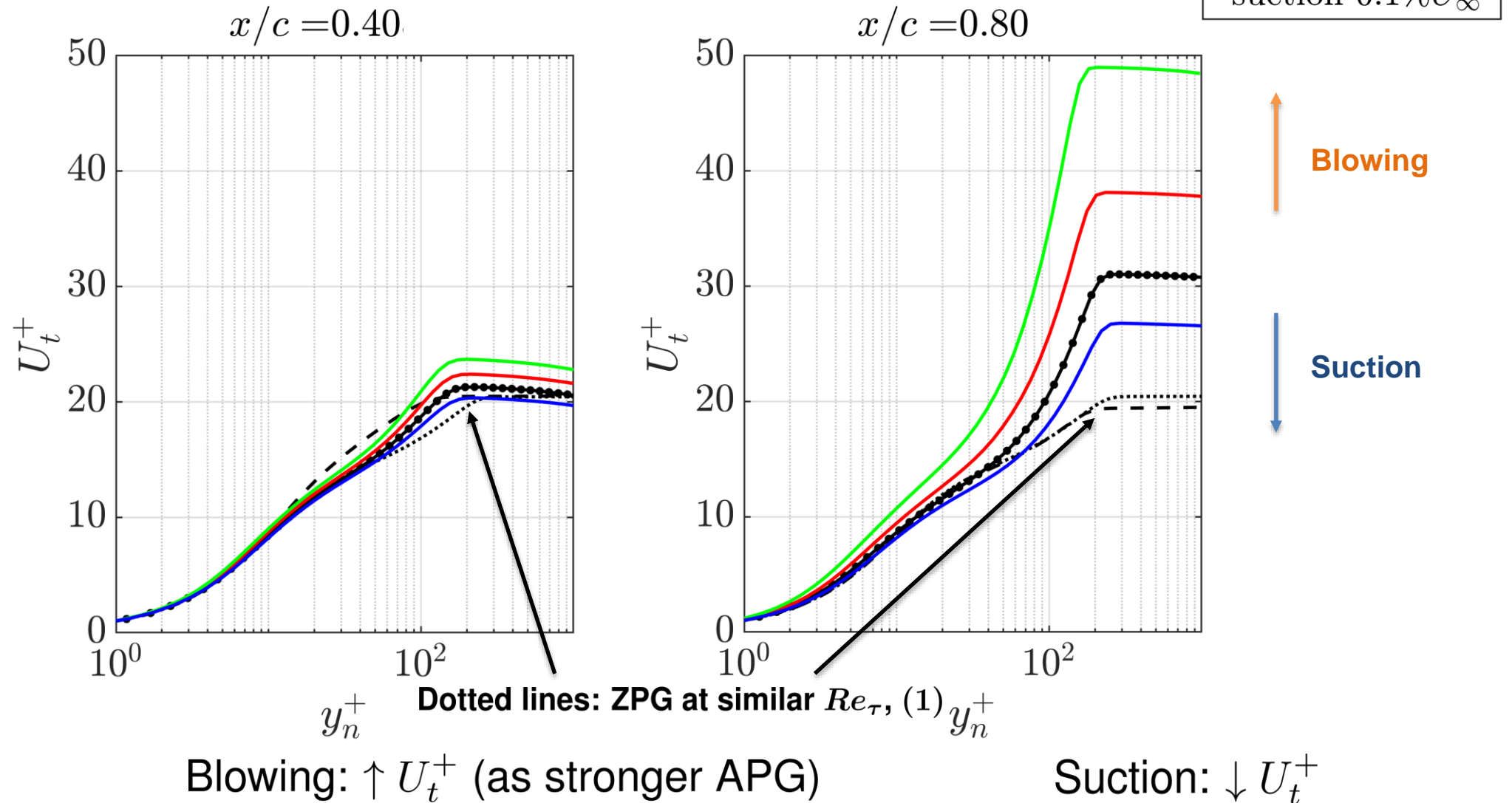


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- **Controlled case 1: Uniform suction,  $0.1\%U_\infty$ , at  $0.25 < x_c < 0.86$**



# Comparison with pressure-gradient effects:

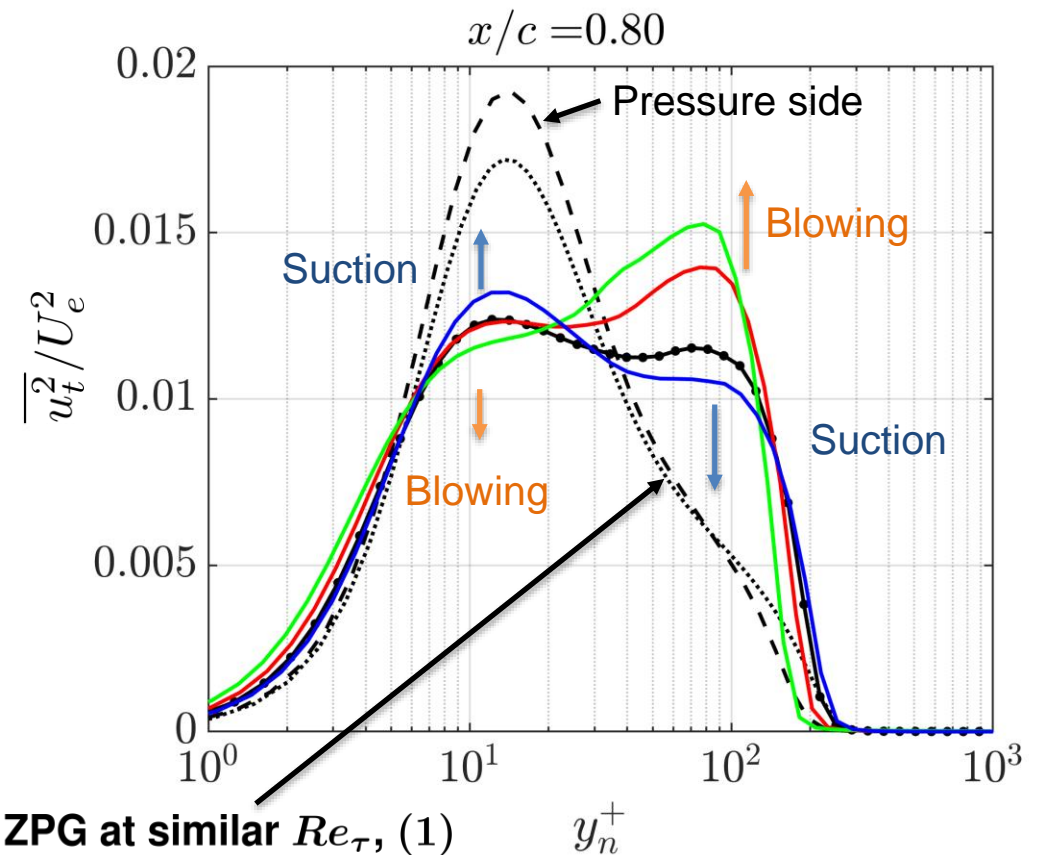
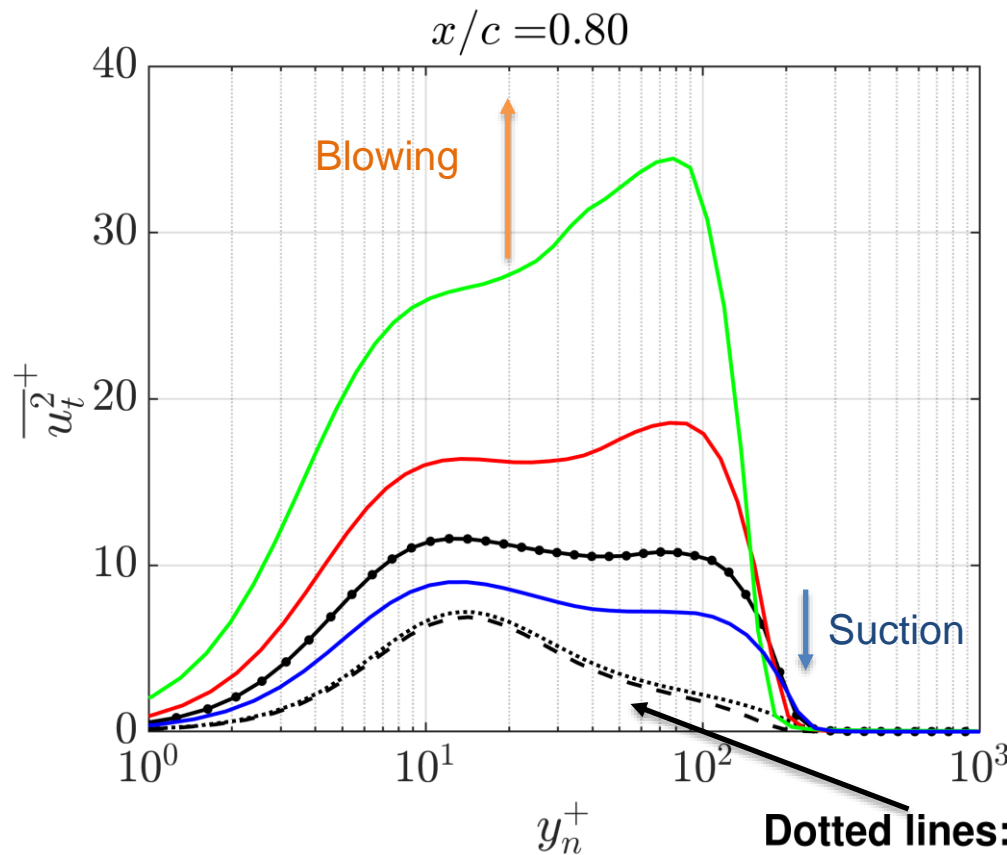
Inner-scaled mean tangential velocity



(1): Schlatter & Örlü, J. Fluid Mech. (2018), 710:5-34

# Comparison with pressure-gradient effects: Fluctuations of the tangential velocity component (inner and outer scaling)

- ref. pressure side
- ref. suction side
- blowing  $0.1\%U_\infty$
- blowing  $0.2\%U_\infty$
- suction  $0.1\%U_\infty$



Blowing:  $\uparrow \overline{u_t^2}^+$  (as APG)    Suction:  $\downarrow \overline{u_t^2}^+$

(1): Schlatter & Örlü, J. Fluid Mech. (2018), 710:5-34

# Effects of the control on the aerodynamic efficiency:

	$c_f$		$c_p$		$C_d$	$C_l$	$L/D$
ref.	<b>0.0125</b>	+	<b>0.0071</b>	=	<b>0.0196</b>	<b>0.87</b>	<b>44</b>
blowing ( $0.1\%U_\infty$ )	<b>0.0119</b> ↓	+	<b>0.0082</b> ↑	=	<b>0.0201</b> ↑	<b>0.84</b> ↓	<b>42</b> ↓
blowing ( $0.2\%U_\infty$ )	<b>0.0115</b> ↓	+	<b>0.0091</b> ↑	=	<b>0.0206</b> ↑	<b>0.82</b> ↓	<b>40</b> ↓
suction ( $0.1\%U_\infty$ )	<b>0.0131</b> ↑	+	<b>0.0063</b> ↓	=	<b>0.194</b> ↓	<b>0.89</b> ↑	<b>46</b> ↑

- **Uniform blowing on the suction side decreases L/D!**
- **Uniform suction on the suction side improves L/D!**

**(At this Reynolds number!)**



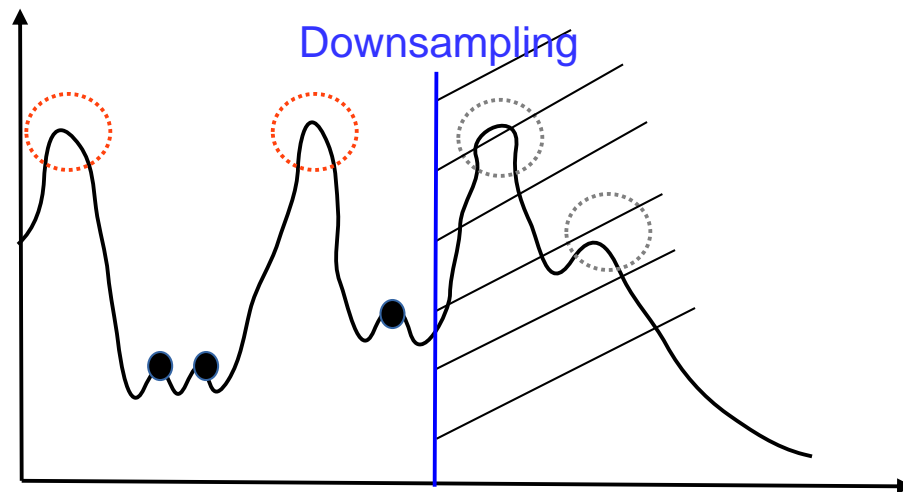
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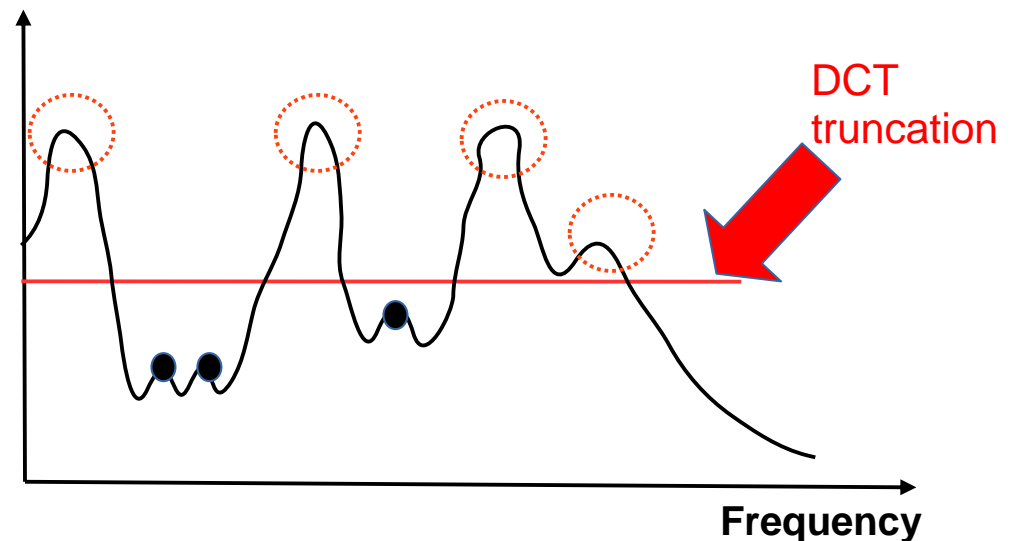
- **Novelty**: Truncation algorithm based on the amplitude of the modes and not on the frequencies (downsampling).

Amplitude



Interesting case where the downsampling loses part of the relevant data  and keep weak data .

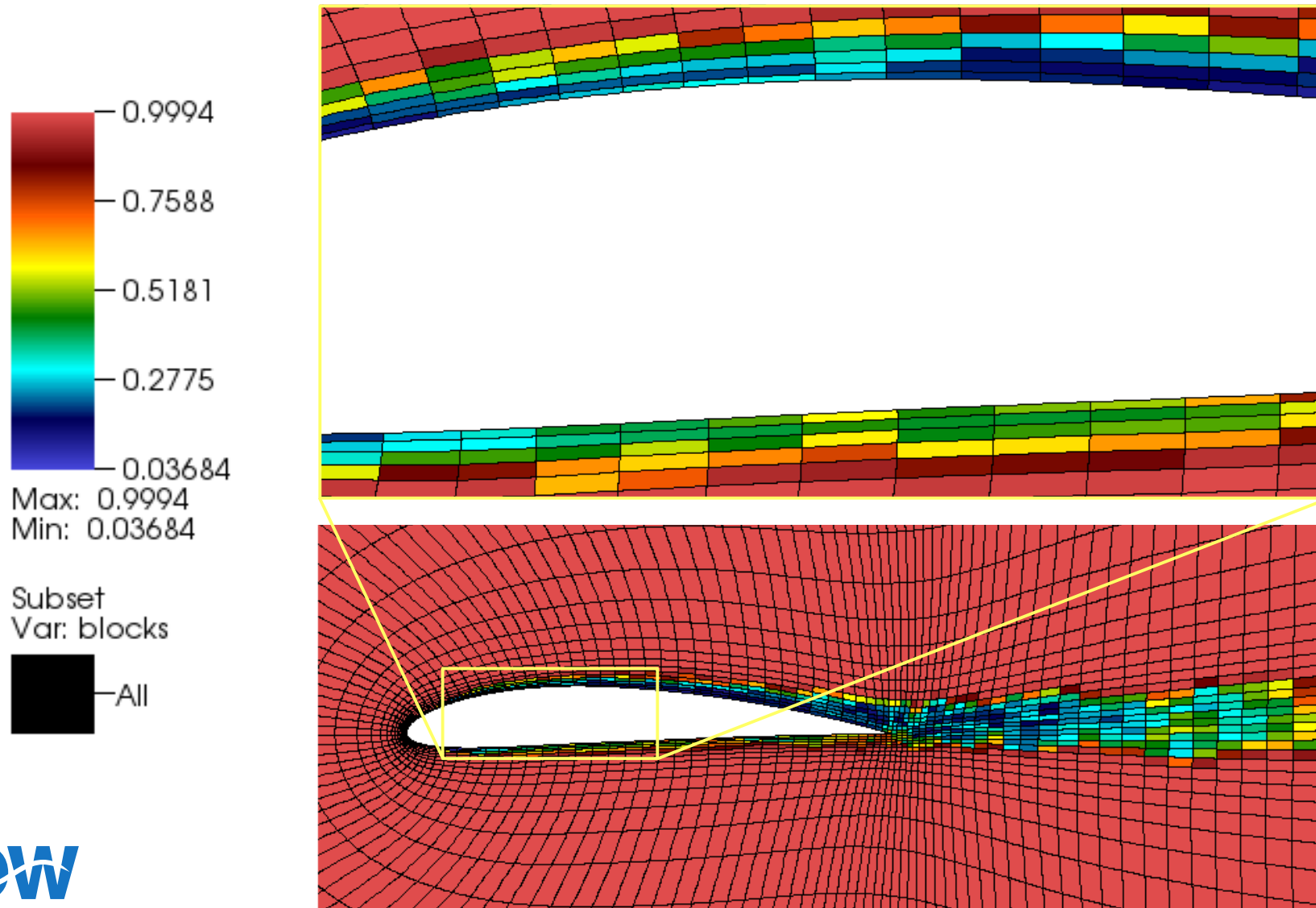
Amplitude



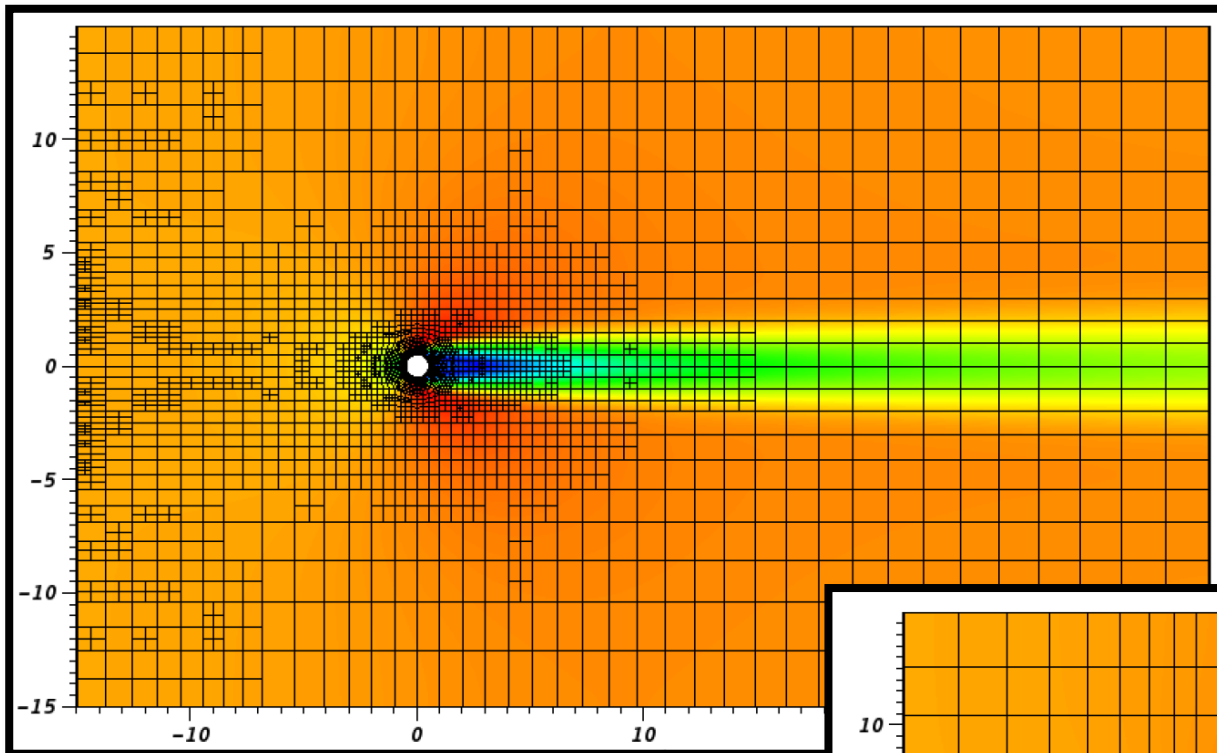
➡ DCT truncation removes data in an adaptive way by removing the weak modes with less contribution to the whole flow representation.

# RESULTS - wing case

- Compression ratio (Error:  $1e-4$ , Cr= 90% )

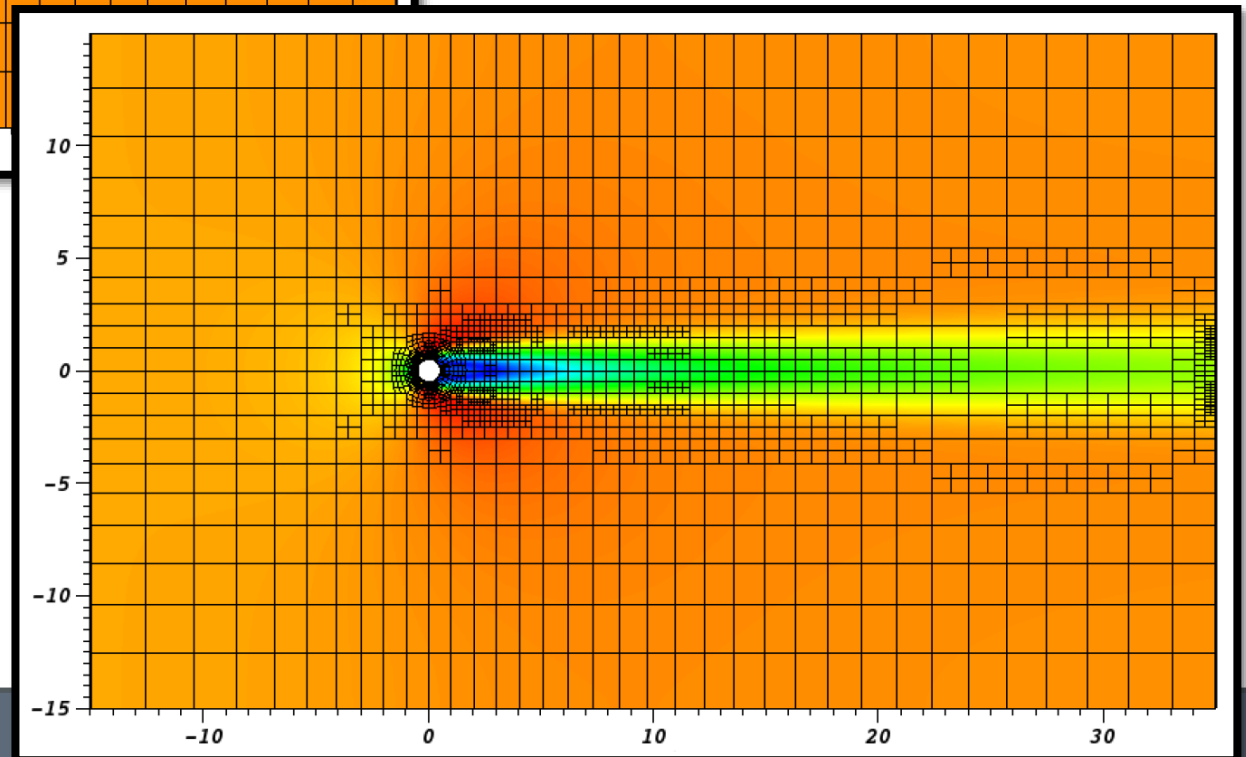


# Adaptive $h$ -refinement (AMR) – 2D cylinder flow



adjoint error estimators

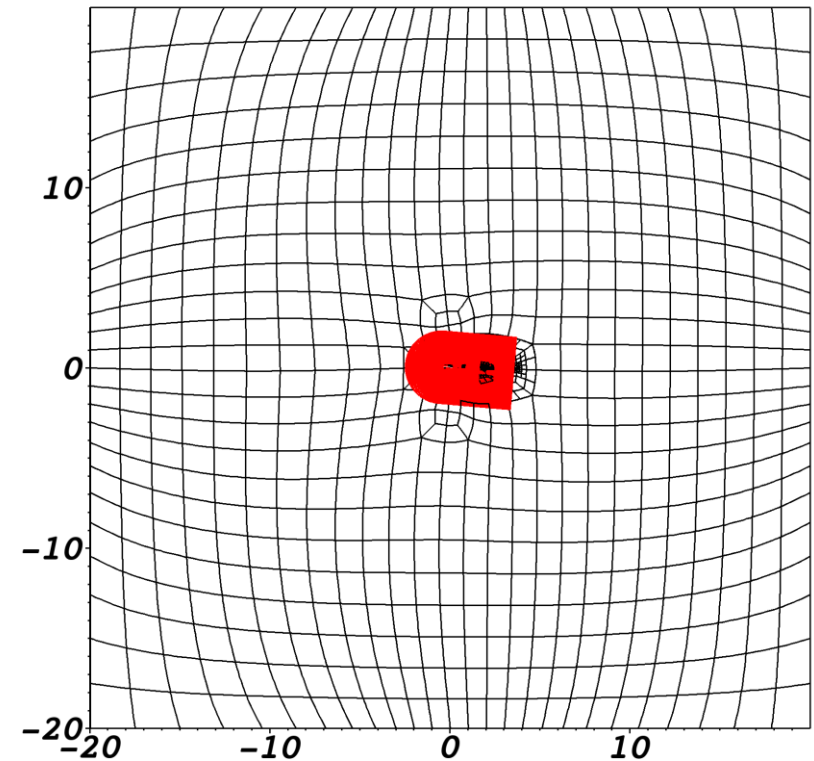
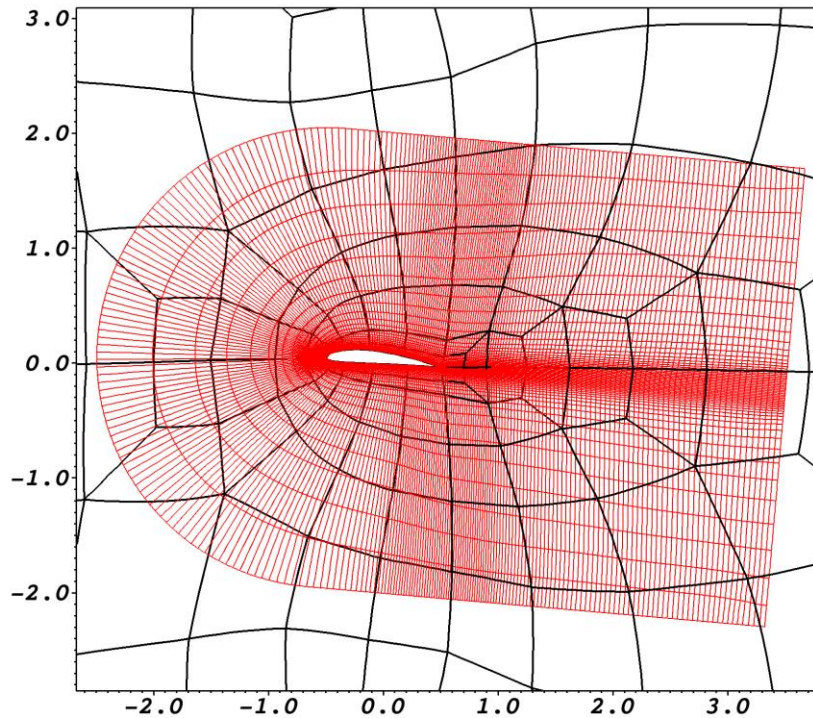
spectral error indicators



Ref. Offermans 2019



# 2D AMR NACA4412 $Re_c = 200\,000$



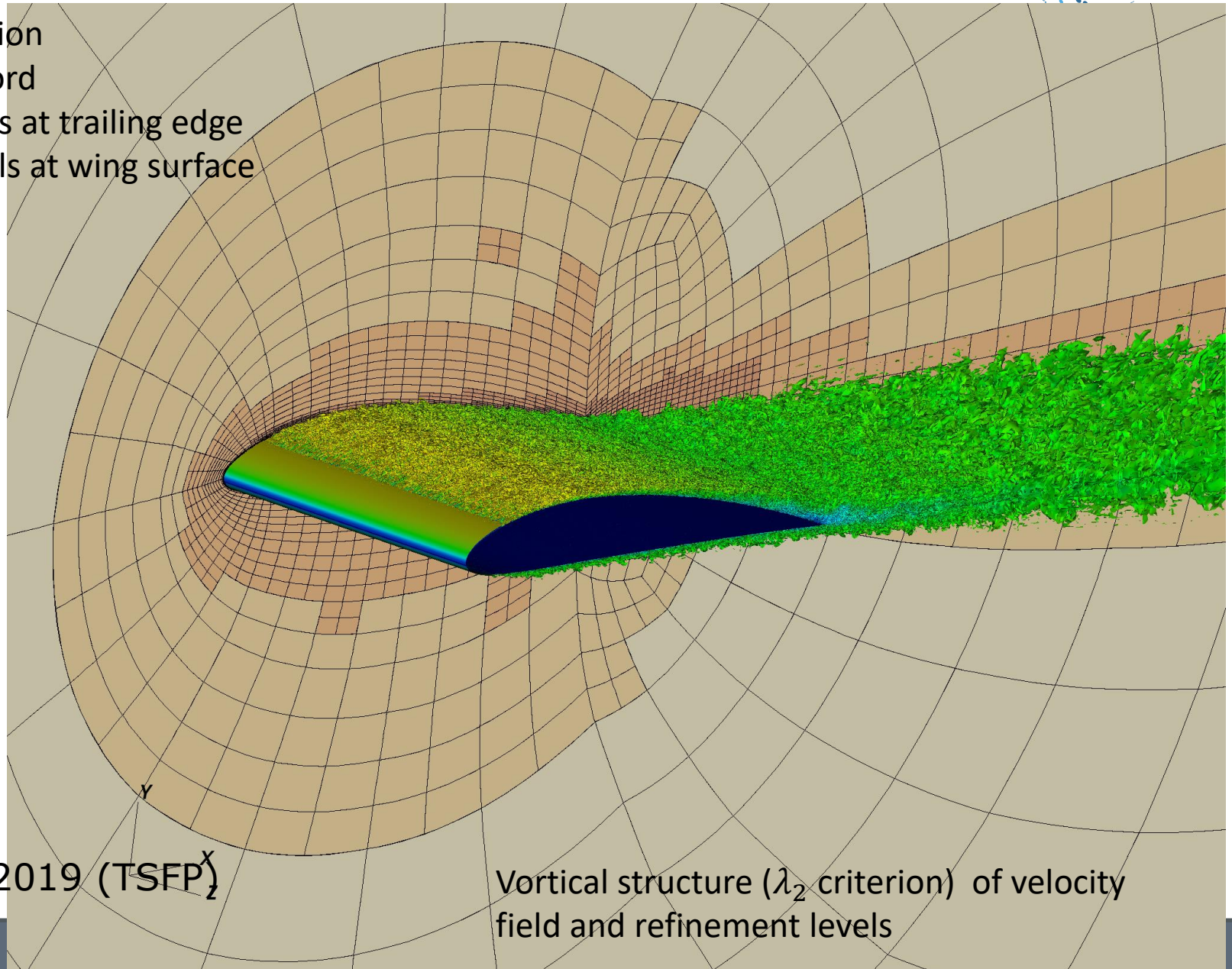
Comparison of mesh structure

Ref. Offermans 2019

# 3D AMR NACA4412 $Re_c = 200\,000$

Tripped AMR simulation

- tripping at 10% cord
- 7 refinement levels at trailing edge
- 5 refinement levels at wing surface



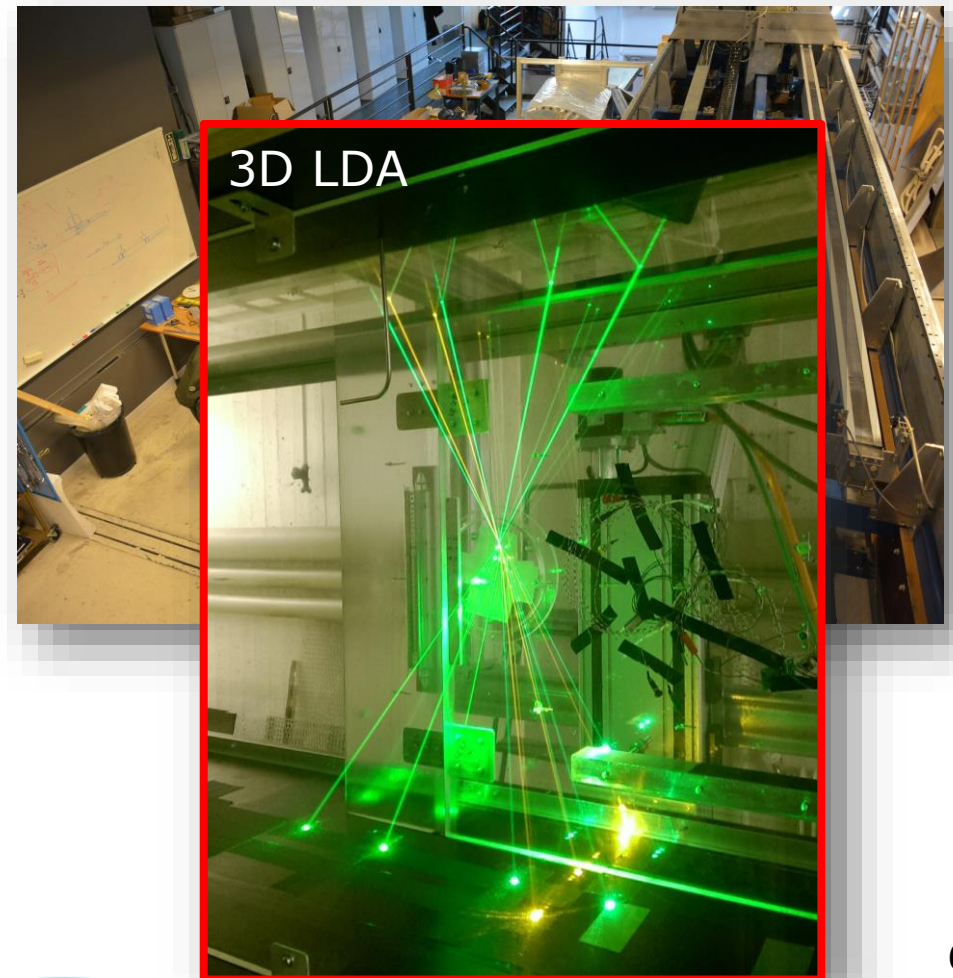
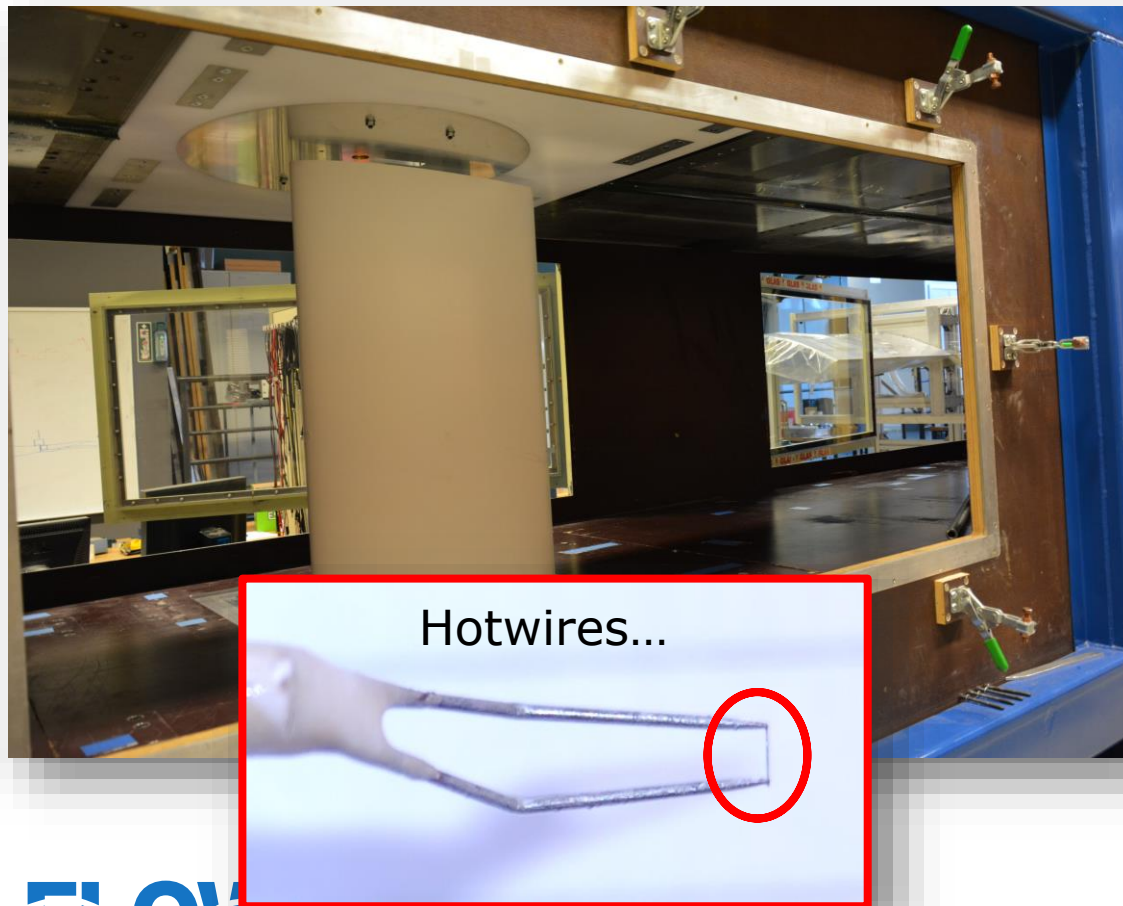
Ref. Tonarro *et al.* 2019 (TSFP)<sub>2</sub><sup>x</sup>

Vortical structure ( $\lambda_2$  criterion) of velocity field and refinement levels



# “Real Experiments” in the MTL wind tunnel (KTH Mechanics)

- Validation experiments to identify shortcomings
- Reynolds number “**only**” up to 1.6 M !!!





# Conclusions

- Large-scale simulations using **high-order (spectral) methods**
- Numerical databases with **highest  $Re$  in the literature:**  
**DNS  $Re_c = 400\,000$**  and **LES at  $Re_c = 1\,000\,000$**
- Non-conformal meshes in **Nek5000** with adaptation.
- “**Virtual experiments**” enables characterisation of complicated flow cases with an unprecedented level of detail:
  - Influence of pressure gradients, comparison to flat plates, tracking of turbulence features, control, ...
  - **Experiments in the MTL wind tunnel**
- **Code development**, new computer architectures, ...
- **uncertainty analysis** for simulations



Thank You!

