

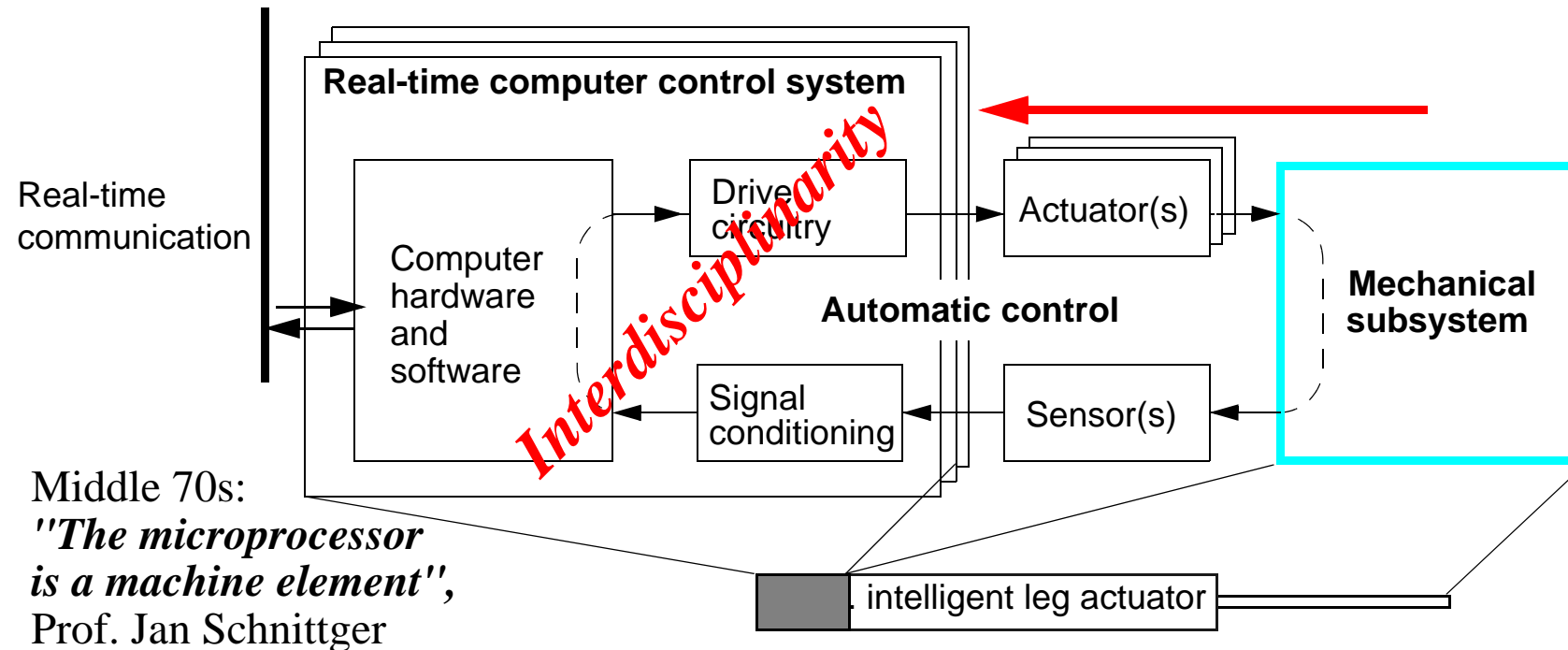
Dynamics and motion control

Lecture 1

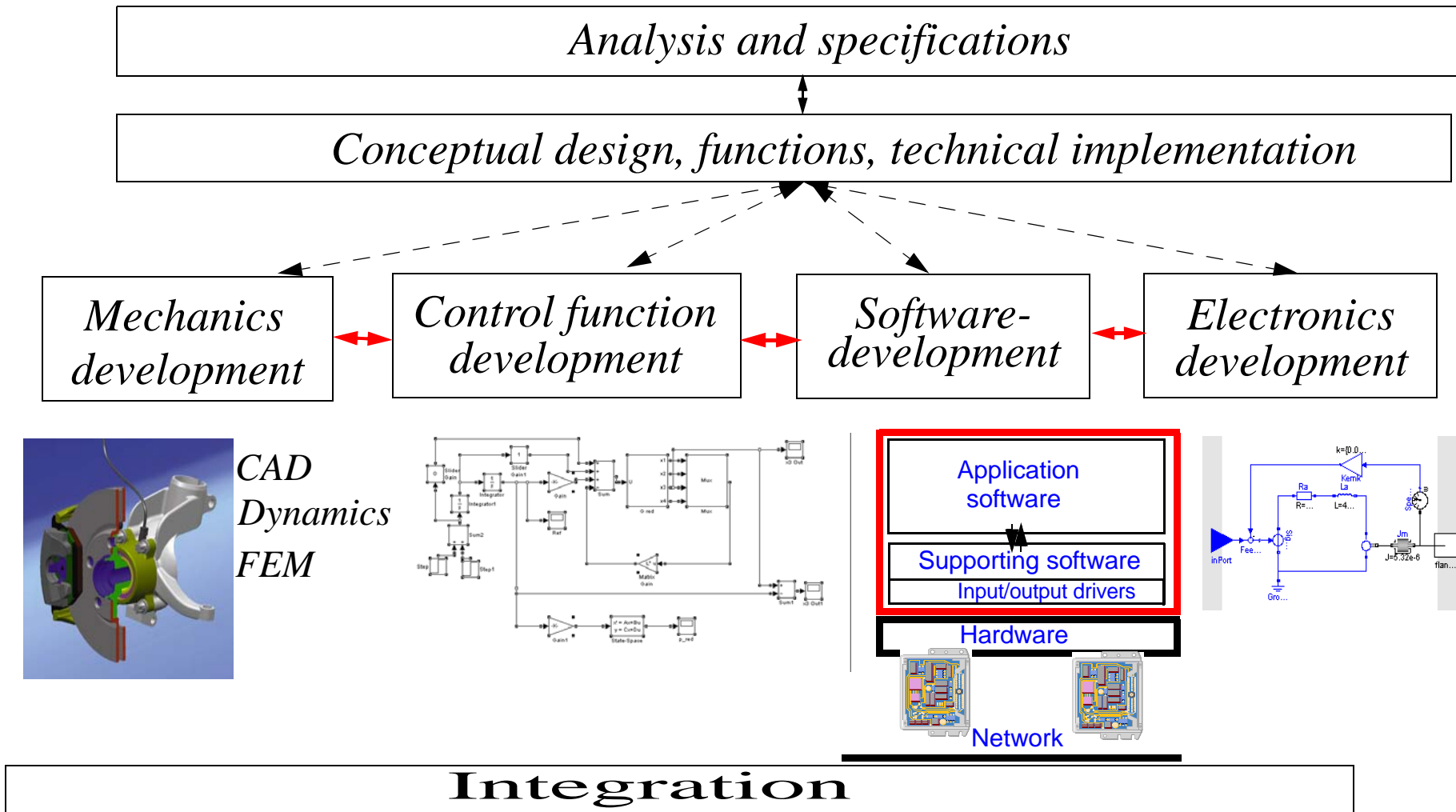
Course introduction and overview

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Mechatronics at Machine Design, KTH



Motivation: multidisciplinary is required!



1.1. Lecture outline

- **1. Course goal**
- **2. Course implementation**
- **3. Overview of and introduction to modelling and control of mechanical systems**

1.1.1 Overall course goal

To provide an understanding and the skills of modelling and design of motion control systems;

"from modelling to implementation"

1.1.2 After the course you should be able to

- Specify overall performance requirements for a motion control system
- Derive models of typical mechatronic applications
- Find good parameters of dynamic models in both frequency and time domain
- Design model based feedback and feed forward control both in continuous and discrete time
- Simulate process and control system models in both continuous and discrete time
- Design and structure the controller software for microprocessor implementation
- Understand the limitations and restrictions due to computing speed.

[Download and read more in the course PM from course homepage](#)

1.1.3 Further course goals

Learning how your theoretical knowledge from earlier courses in math, mechanics, numeric methods and control should best be used to avoid chaos in real world experiments.

$$\frac{s}{(s+a)^2} \quad \frac{(z-1)h e^{-ah}}{(z-e^{-ah})^2}$$

$$\frac{ab}{(s+a)(s+b)} \quad b_1 = \frac{b(1-e^{-ah}) - a(1-e^{-bh})}{b-a}$$
$$a \neq b \quad b_2 = \frac{a(1-e^{-bh})e^{-ah} - b(1-e^{-ah})e^{-bh}}{b-a}$$
$$a_1 = -(e^{-ah} + e^{-bh})$$
$$a_2 = e^{-(a+b)h}$$



1.2. Lecture outline

- 1. Course goal
- **2. Course implementation**
- 3. Overview of and introduction to modelling and control of mechanical systems

1.2.1 Prerequisites

- **Some mechanical and electrotechnical knowledge**
- **Very little programming knowledge**
- **Good control knowledge it should correspond to the content of a basic course in control engineering**

1.2.2 Course outline

- **2 two hour lectures per week (except first week -> three)**
 - Basic theory and calculated examples
- **2 three hour per week lab working**
 - Mainly computer simulation work, Matlab/Simulink
 - Working with Exercises and Workshops
 - Assistance by

1.2.3 Literature and course material

⇒ The course specification

⇒ The reading material

⇒ The lecture notes →

⇒ Standard book in control

⇒ The exercises

⇒ The workshops

L2, modelling

L3, feedback design in continuous time

L4, feedback design in discrete time

L5, Model following control -servo

L6, Implementation on real-time HW

L7, Robustness issues

1.2.4 Examination

- **1. Completed exercises**

- The exercises are completed by showing the results to an assistant in the lab.

Exercises part 1, modeling of mechanical systems

Exercises part 2, modeling of a DC motor system

Exercises part 3, control of a DC motor system

- **2. Written reports on the workshops, A and B.**

- **3. Written exam.**

Grading: A-F according to ECTS based on a weighted combination of the bullets 2 and 3 above.

1.2.5 Exercises and laboratory facilities

- Working in groups of preferably three people in each group
- Where to work?
 - MMT computer rooms: Matlab/Simulink
 - Mechatronics-lab: ("FIM-labbet") Matlab/Simulink and experiments on real motor.
 - Wennström-lab: ("elektro-labbet") Matlab/Simulink
 - Room A319 is equipped with special HW/SW for RCP
 - Your own computers, KTH CD'n with Matlab/Simulink
- Mechatronics-lab: "passerkort": need card numbers
- The labs are free to use 7/24 if they not are booked for other courses, booking schedule is available from course home page.

1.2.6 Additional useful material

- **The course builds upon earlier courses!**
 - mechanics, machine elements, numerical methods, control engineering, computer science and programming, electrical engineering
- General textbooks in
 - Control engineering -from a first course in automatic control. e.g. *Glad och Ljung: Reglerteknik - Grundläggande teori*
 - Electric circuit theory -from a first course in electric circuits. e.g. Hans Johansson Elektroteknik
 - Mechanical engineering. -from a course in dynamics. e.g. -----
- Selected parts of "**Mechatronics System Design**", *Klaus Janscheck*
 - Available as E-book from the KTH Library

1.2.7 Learning philosophy

- It is about *your learning* - for which *You* is the boss!
- We employ feed forward and feedback to improve the learning process
- *Feed forward* concepts: material, lectures, the project etc.
- *Feedback* mechanisms
 - 1) Participant representatives: to collect important feedback info
 - 2) Lecture and workshop follow up questions
 - 3) Hand ins of project parts
 - 4) Course evaluation in the end

1.3. Lecture outline

- **1. Course goal**
- **2. Course implementation**
- **3. Overview of and introduction to control of mechanical systems
and a brief introduction to tools**

1.3.1 Forecasts!

- *"I think there is a world market for about five computers", Tomas J Watson Sr, IBM 1943*
- *"There are no reasons for any individuals to have a computer in their home", Ken Olson, Digital Equipment 1977*
- *"The current rate of progress cannot continue much longer", various computer technologists, 1950*

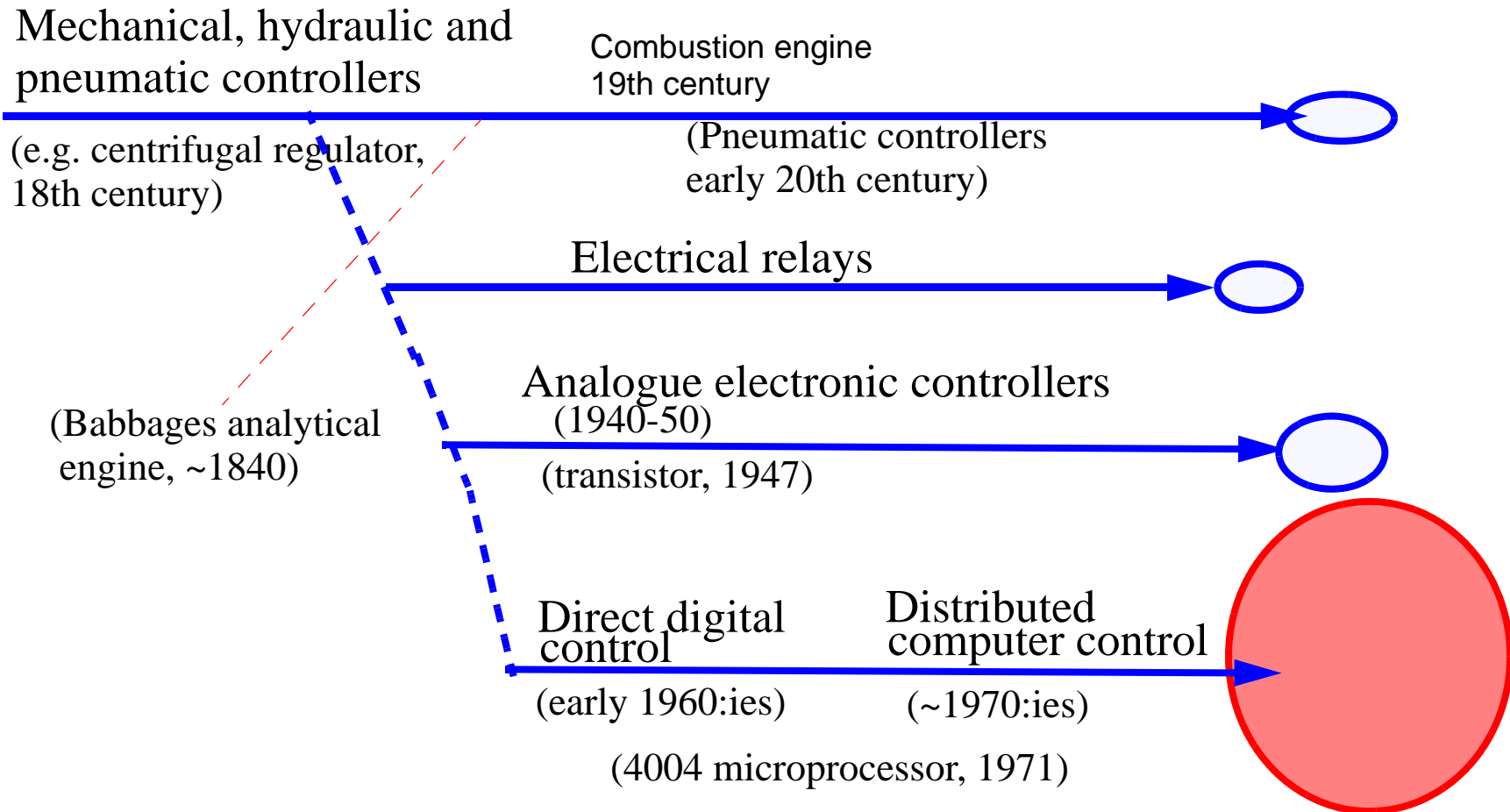
'Moore's law' (Intel, 1965):

Microelectronics (MOS) performance is ~doubled every 18 months and chip size is reduced by 50%

Intel 4004/1971 vs. Intel Pentium/1996: from 2300 to 5.5 million transistors

One prediction for "2006: One chip with 200M transistors with 2GHZ frequency"

1.3.2 Control technologies over time

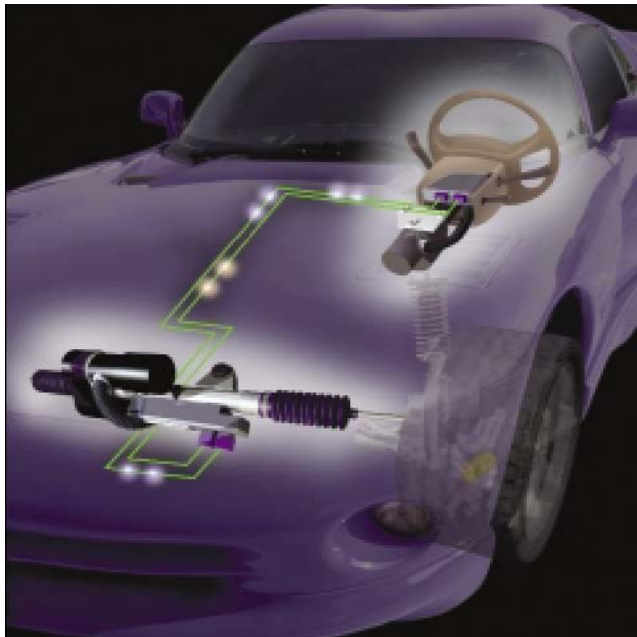


1.3.3 Control development over time

- All mechanical controllers, e.g. the centrifugal governor (wind mills, steam engines, telephones), from 1700 and onwards.
- Early theoretical results, e.g Routh, Hurwitz and Lyapunov on stability, late 1800's.
- Ziegler's and Nichols' method for tuning of PID controllers in 1942.
- Computers in control from the mid 50's.
- New control design methods in the late 20th century: Optimal, Adaptive, Non-linear, Robust, Fuzzy, Neural, etc.
- 95% of all process controllers are of PID type

1.3.4 The paradigm shift

Servo steering with
mechanical backup



Steer by wire

⇒ **More digital control!**

1.3.5 What can be achieved?

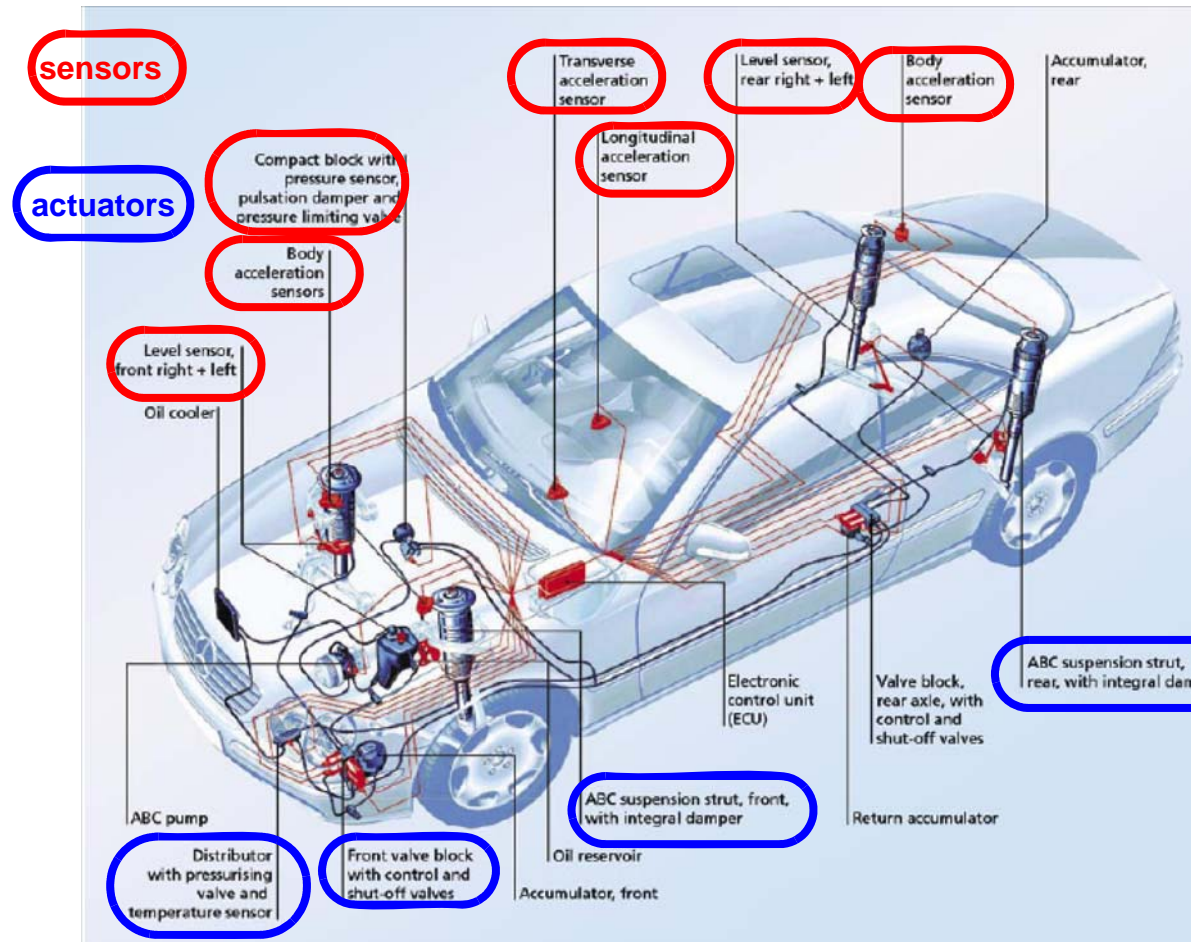
**Hy-Wire from GM
(autonomy 2)**



**Skateboard concept
Fuel cell 94kW
Integrated distributed control
Weight: 2 tons, Distance: 480kn**

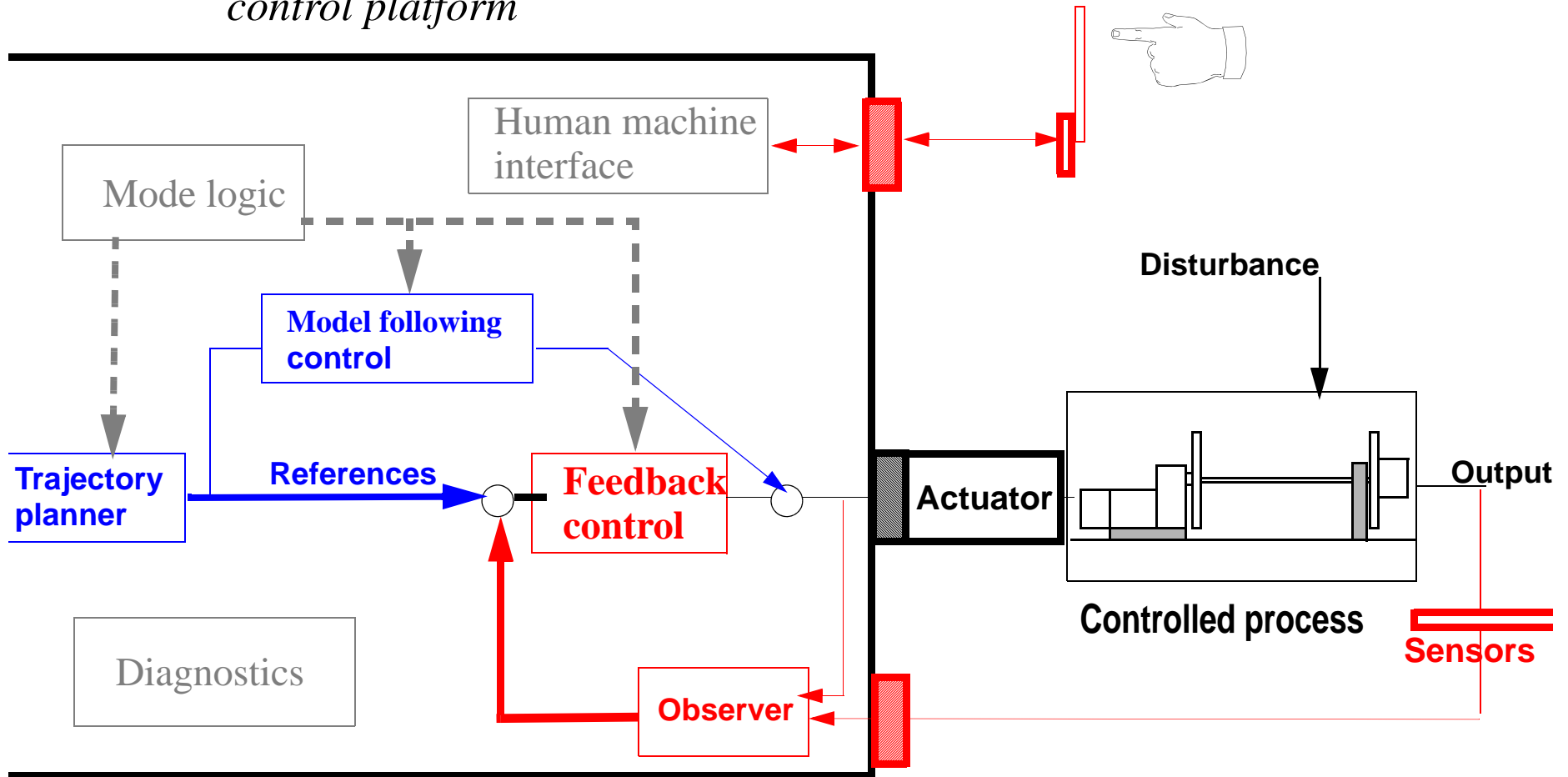
1.3.6 Why models? - active body control

- Many sensors
- 4 actuators
- Complex dynamics
- Mechanical and control design not separable
- Simulation necessary



1.3.7 More than just feedback

Implemented on embedded control platform



1.3.8 Example motion control applications

- Industrial robot control
- Vehicular systems (suspension, brakes, engine control...)
- Aircraft control and space applications
- Axis control in various production machines
- Hydraulic servo, e.g. in forest harvester or excavator
- Master and slave control in teleoperated systems
- Mobile robots/machines

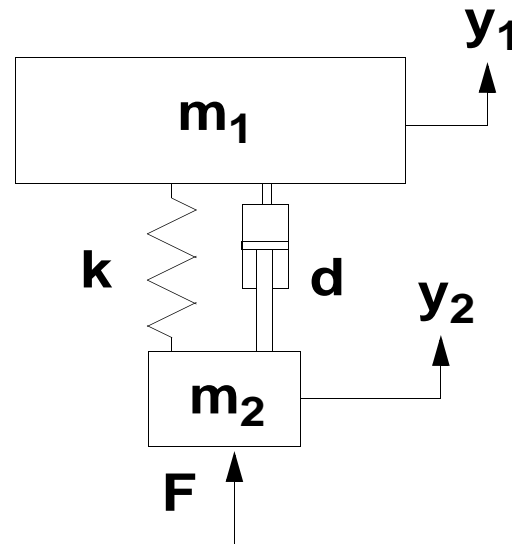
1.3.9 The complete *control* design process

- Design of the mechanical system
Either prior to, or in conjunction with control design
- **Modelling** of the system and in some cases also modelling of the system's interaction with the environment
- Analysis of **dynamic properties** including simulation
- Control requirement **specifications**
- **Control design** including choice of related components such as sensors, control computer and sometimes actuator(s)
- Simulation, verification and **control prototyping**
- Real-time **implementation**

1.3.10 Mechanical system modelling

- Degrees of freedom - DOF: The number of inertia in a dynamic system that can move relative each other
- The motion of each DOF is modelled by, $m\ddot{x} = \sum F_y$, or $J\ddot{\phi} = \sum M_y$.

Example:

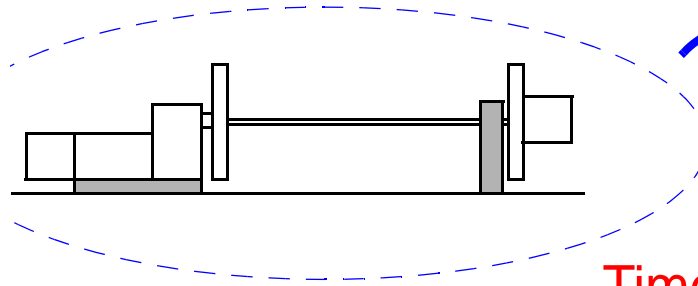


Two DOFs coupled by a weak link.
4:th order differential equation

1.3.11 Modelling and dynamic analysis of mechanical systems

- Putting up the differential equations
- Linearization
- Formulations:
 - State space; matrix equations
 - Input-output; transfer functions
- Different levels of simplification depending on purpose, e.g. simulation vs control design, feed forward vs feedback - *model validation*
- Finding the parameters; system identification
- Computer tools such as Maple and Matlab e.g. with the Identification toolbox

1.3.12 Different domains for different tasks

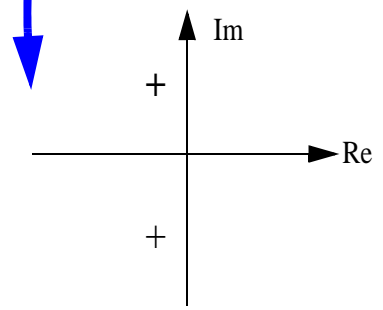


$$\frac{dx}{dt} = f(x, u) \quad y = h(x)$$

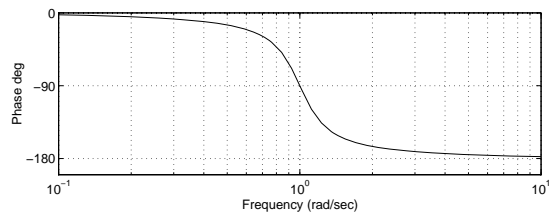
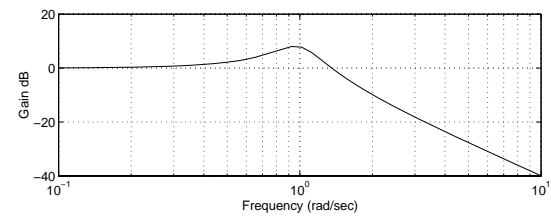
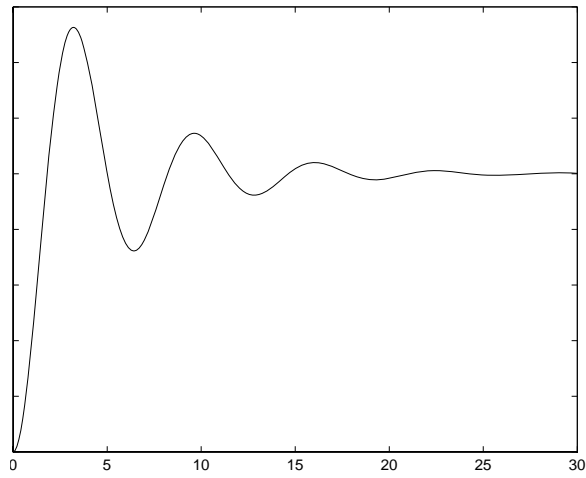
Time domain

$$y(t) = \sum A_i e^{-\lambda_i t} \cos(\omega_i t + \phi_i)$$

$$G(s) = \frac{\omega_0^2}{s^2 + 2\xi\omega_0 s + \omega_0^2}$$



Complex plane



Frequency domain

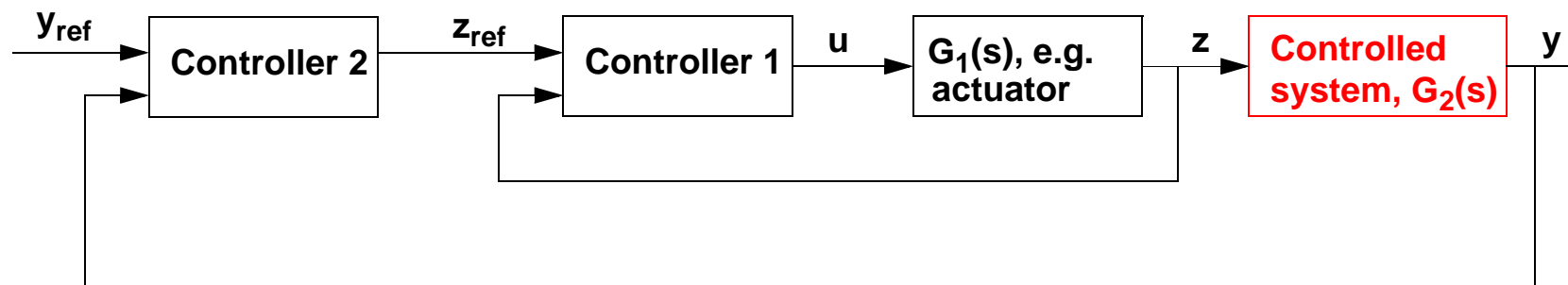
1.3.13 Feedback control

Different controller structures

- PID control:

$$u(t) = K_p \cdot e(t) + K_I \cdot \int_0^t e(s) ds + K_D \cdot \frac{d}{dt} e(t)$$

- Cascade control: inner loop viewed as an ideal servo by outer loop

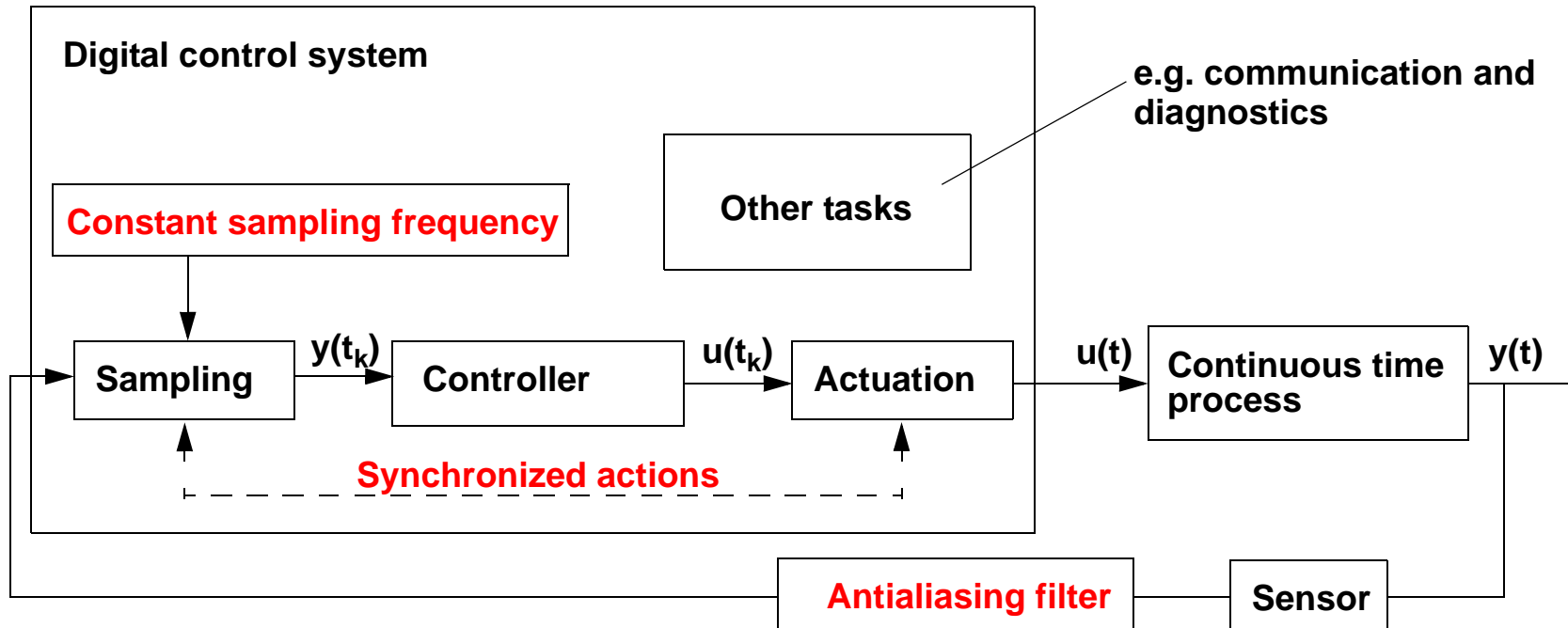


1.3.14 Feedback control properties

The main principle in control engineering

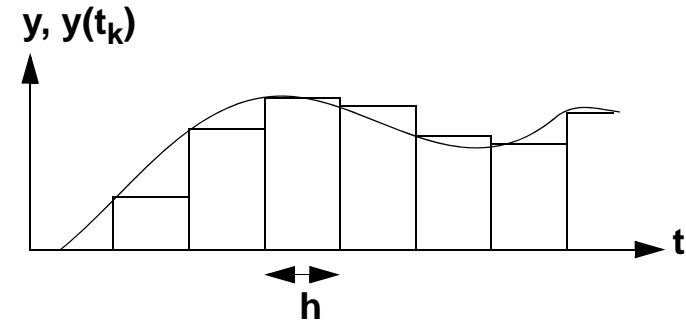
- Typically model based (but not required to be)
- Produces control signals after an error has occurred
- Disturbance rejection is achieved
- Effect of process parameter variations is reduced
- Leads to a closed loop
- Sensor noise may be amplified and deteriorate performance
- May lead to instability if designed incorrectly

1.3.15 Discrete time control



Sampling interval $h = t_k - t_{k-1}$

Sampling frequency $f = 1/h$



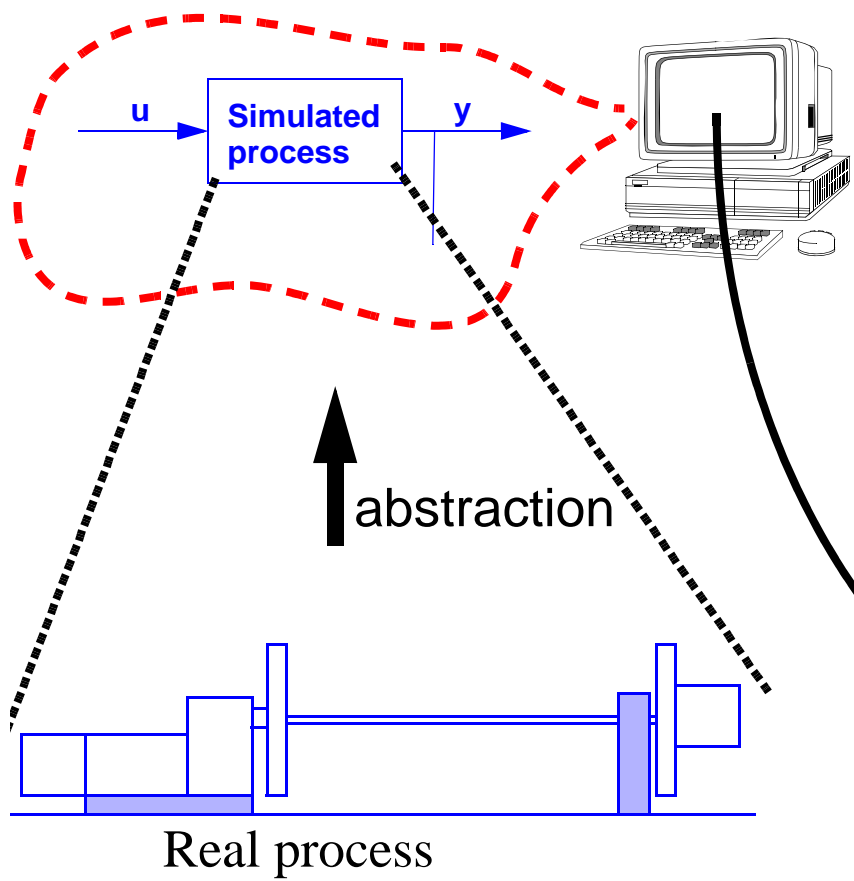
1.3.16 Brief introduction to tools

- **Modelling and simulation**
+ Matlab/Simulink
+ **Purpose: Modeling, analysis and design + model verification**
- **Rapid control prototyping (RCP), 2 different systems**

dSPACE

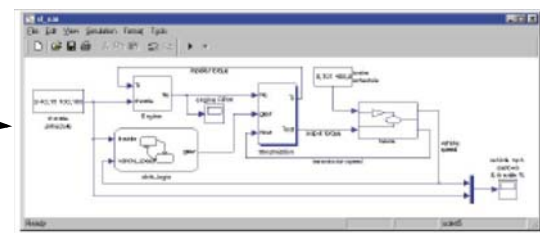
- Power PC on PCI bus inside PC
- I/O on the same PCI board
- Programmed with Simulink
- RTW, C-code generator
- Microtec C cross compiler
- 4 systems in lab
- Host PC env. ControlDesk

1.3.17 Modelling and simulation



$$\frac{dx}{dt} = f(x, u) \quad y = h(x)$$

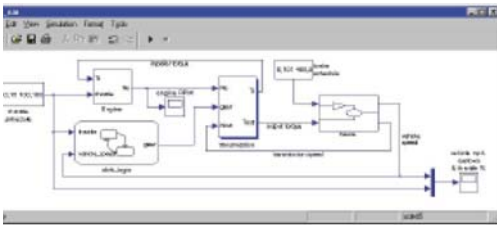
- Numerical solution: non real-time
Integration solvers, e.g., runge kutta order 2-5 using variable step size for efficient simulation time and stable solution.



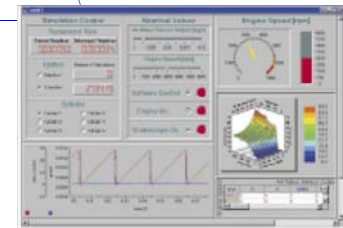
1.3.18 Rapid control prototyping (RCP)

Modelling and design

Non real-time simulation



Evaluate and redesign



Control implementation needs tools for quick iterations

Instrumentation for tuning and measurement



Include I/O drivers



Automatic C-code generation



Compile and download on RCP HW