

## SENSITIVITY TO COEFFICIENT QUANTIZATION



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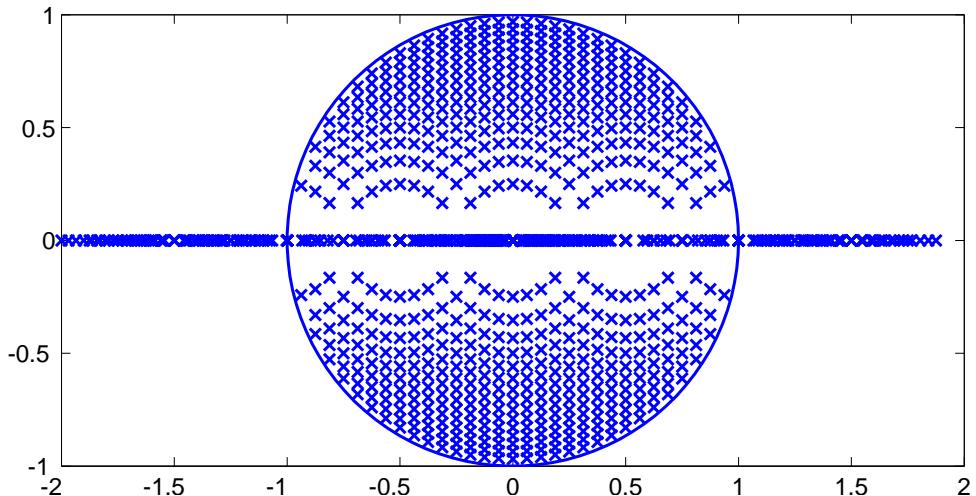
- Small roundoff in coefficient:  $c_k + \epsilon_{c_k} \implies$  transfer function changes approximately to  $H(z) + \epsilon_{c_k} \frac{\partial H(z)}{\partial c_k}$
- Sensitivity:  $\frac{\partial H(z)}{\partial c_k}$
- Different implementations of same transfer function give different sensitivity.



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## Ex. POLE POSITIONS DUE TO QUANTIZED COEFFICIENTS

Example:  $H(z) = \frac{1}{1+a_1z^{-1}+a_2z^{-2}}$ ,  $-1 \leq a_1 < 1$ ,  $0 \leq a_2 < 1$ , four bits each

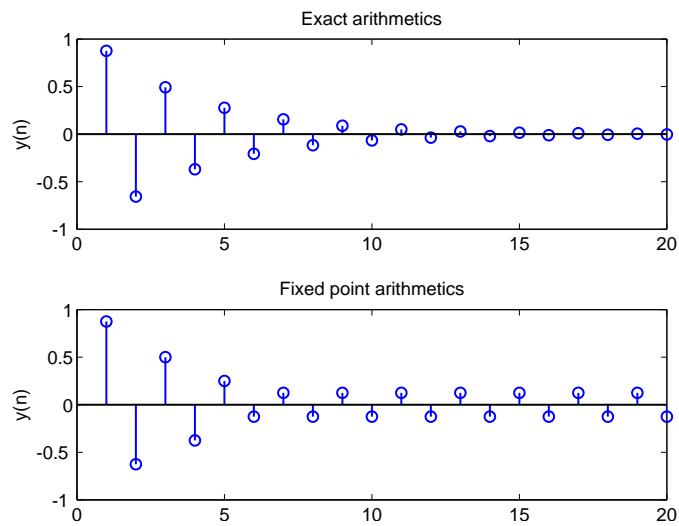


## "LIMIT CYCLES" — OSCILLATIONS DUE TO ROUND-OFF

Example:  $y(n) = -\frac{3}{4}y(n - 1)$ , 4 bit fixed point numbers



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86.3

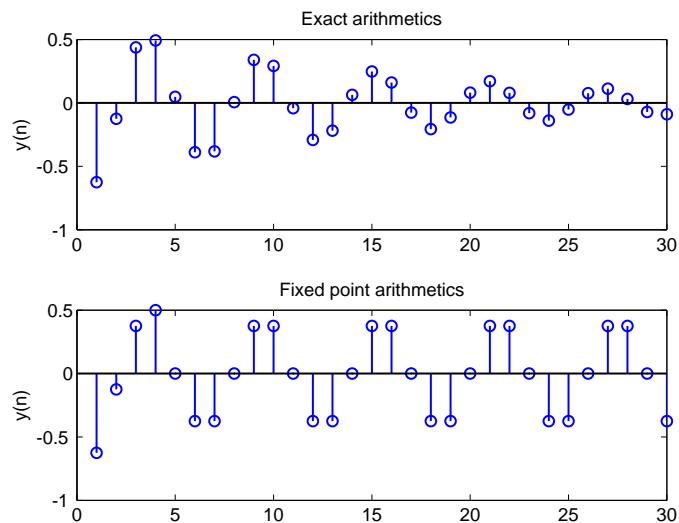
Lecture 10

## "LIMIT CYCLES" — OSCILLATIONS DUE TO OVERFLOW

Example:  $y(n) = \frac{7}{8}y(n - 1) - \frac{7}{8}y(n - 2)$ , 4 bit fixed point numbers



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