## Computational Fluid Dynamics (SG2212/SG3114), 7.5 ECTS

## **Lecturers:**

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## **Assistants:**

Azad Noorani (AN), azad@kth.se, Mekanik, tel 790 8034

Office hours: Wednesday 14-17

Taras Khapko (TK), taras@mech.kth.se, Mekanik, tel 790 7152

Office hours: Thursday 14-17

#### Literature:

Relevant books:

- Computational Fluid Dynamics, John D. Anderson, Jr., McGraw-Hill, 1995
- Numerical Computation of Internal & External Flows, Charles Hirsch, Butterworth-Heinemann, Second Edition, ISBN: 978-0-7506-6594-0.

Lecture notes on Computational Fluid Dynamics (D. Henningson) Lecture notes on Basic Numerics (K. Gustavsson)

## **Grading:**

Exam total of 50p,

Homework (compulsory)  $6\times2$  + project (compulsory)  $5 \Rightarrow \max 15p$ .

Total points >28 (E), >30 (D), >40 (C), >50 (B), >55 (A).

## Web links:

https://www.kth.se/social/course/SG2212/

## **Homeworks:** (5 of 6 are compulsory)

•Homework 1, due 21/1

•Homework 2, due 28/1

• Homework 3, due 4/2

• Homework 4, due 11/2

• Homework 5, due 25/2

•Homework 6, due 4/3

## **Project (compulsory):**

Project, due 18/3

# Course plan

					Fluid dynamics I:	
Week 3	Mon	14 Jan	13-15	Q36	Introduction and outline of the course.  Derivation of the governing equation.	АН
	Tue	15 Jan	15-17	Q34	Fluid dynamics II Derivation of the governing equation , cont.	АН
Week 5 Week 4	Thu	17 Jan	13-15	Q34	Fluid dynamics III: Derivation of the governing equation , cont.	АН
	Mon	21 Jan	13-15	Q36	Basic numerics I: Mathematical behavior of hyperbolic, parabolic and elliptic equation. Well-posedness.	PS
	Wed	23 Jan	15-17	Q34	Basic numerics II: Discretization by finite differences. Analysis of discretized equation; order of accuracy, Convergence	PS
				001	Basic numerics III: Analysis of discretized equation, cont.	PS
	Thu	24 Jan	15-17	Q34	Homework review: Solution of HW1 Description of HW2	TK, AN
	Mon	28 Jan	13-15	V32	Analysis of discretized equations: Consistency, Convergence and Stability, CFL condition	PS
	Wed	30 Jan	10-12	Q31	Compressible flow I: Introduction to compressible flow, Euler equation, conservation laws, entropy	PS
					Compressible flow II: Numerical methods for conservation laws, Stability, Dispersion, Diffusion	PS
	Fri	1 Feb	13-15	Q34	Homework review: Solution of HW2 Description of HW3	TK, AN
Week 6	Mon	4 Feb	13-15	V32	Compressible flow III: Shock tube, boundary conditions, artificial viscosity	PS
	Wed	6 Feb	10-12	L52	Compressible flow IV: Systems of conservation laws, Riemann Invariants	PS
	Thu	7 Feb	13-15	V32	Introduction to incompressible flow. Navier-Stokes in integral form. Finite volume and finite difference methods: Laplace equation on arbitrary grids, equivalence with finite-differences.  Homework review: Solution of HW3	AH TK, AN
					Description of HW4	

Mon	11 Feb	13-15	Q36	Finite volume and finite difference methods: Cartesian grid and spurious solutions. Staggered grid/volume formulation + BC.	АН
Wed	13 Feb	08-10	V32	Steady incompressible flows: Artificial compressibility	АН
Fri	15 Feb	08-10	L52	Projection on divergence-free space, Unsteady incompressible flows: projection method, discrete Poisson pressure eq.  Homework review:	AH TK, AN
				Solution of HW4	
Mon	18 Feb	13-15	Q36	linear systems: Iterative methods, Gauss-Seidel as smothers for multi-grid	АН
Wed	20 Feb	10-12	V32	Complex geometries, Coordinate transformation.	AH
				Unstructured Node-Centered FV: consistency and accuracy.	АН
Thu	21 Feb	15-17	V34	Homework review: Description of HW5	TK, AN
Tue	26 Feb	08-10	Q36	Upwind schemes, Flux splitting	АН
Wed	27 Feb	08-10	Q36	High-order compact finite differences.	АН
				Introduction of project	
Thu	28 Feb	15-17	V34	Homework review: Solution of HW5 Description of HW6	PS, AH TK, AN
Mon	4 Mar	13-15	V34	Project lecture	PS
Thu	7 Mar	15-17	V34	Project supervision	TK, AN
Fri	8 Mar	10-12	Q34	Homework review: Solution of HW6 Demonstration of project	TK, AN
Fri	15 Mar	14-18	Q34 Q36	Examination	
Thu	30 May	09-13	E51	Re-exam	
	Wed Fri Mon Wed Thu Mon Thu Fri Fri	Wed 13 Feb  Fri 15 Feb  Mon 18 Feb  Wed 20 Feb  Tue 26 Feb  Wed 27 Feb  Thu 28 Feb  Mon 4 Mar  Thu 7 Mar  Fri 8 Mar  Fri 15 Mar	Wed       13 Feb       08-10         Fri       15 Feb       08-10         Mon       18 Feb       13-15         Wed       20 Feb       10-12         Thu       21 Feb       15-17         Tue       26 Feb       08-10         Wed       27 Feb       08-10         Thu       28 Feb       15-17         Mon       4 Mar       13-15         Thu       7 Mar       15-17         Fri       8 Mar       10-12         Fri       15 Mar       14-18	Wed       13 Feb       08-10       V32         Fri       15 Feb       08-10       L52         Mon       18 Feb       13-15       Q36         Wed       20 Feb       10-12       V32         Thu       21 Feb       15-17       V34         Tue       26 Feb       08-10       Q36         Wed       27 Feb       08-10       Q36         Thu       28 Feb       15-17       V34         Mon       4 Mar       13-15       V34         Thu       7 Mar       15-17       V34         Fri       8 Mar       10-12       Q34         Fri       15 Mar       14-18       Q34         Q34       Q36	Mon       11 Feb       13-15       Q36       Cartesian grid and spurious solutions. Staggered grid/volume formulation + BC.         Wed       13 Feb       08-10       V32       Steady incompressible flows: Artificial compressibility         Fri       15 Feb       08-10       L52       Projection on divergence-free space, Unsteady incompressible flows: projection method, discrete Poisson pressure eq.         Mon       18 Feb       13-15       Q36       linear systems: Iterative methods, Gauss-Seidel as smothers for multi-grid         Wed       20 Feb       10-12       V32       Complex geometries, Coordinate transformation.         Thu       21 Feb       15-17       V34       Unstructured Node-Centered FV: consistency and accuracy.         Thu       26 Feb       08-10       Q36       Upwind schemes, Flux splitting         Wed       27 Feb       08-10       Q36       Upwind schemes, Flux splitting         Wed       27 Feb       08-10       Q36       High-order compact finite differences.         Introduction of project         Homework review: Solution of HW5         Description of HW6         Mon       4 Mar       13-15       V34       Project lecture         Fri       8 Mar       10-12       Q34       Homework review: Solution of HW6 Demonstration of project