



ROYAL INSTITUTE
OF TECHNOLOGY

Frequency Control

Lectures 5-6 in EG2050 System Planning

Lars Abrahamsson

Course Objectives

To pass the course, the students should show that they are able to

- explain how the balance between production and consumption is maintained in an electric power system,
- and calculate how the frequency is affected by various events in the power system.

To receive a higher grade (A, B, C, D) the students should also show that they are able to

- determine if the frequency control of an electric power system has sufficient margins, and
 - if necessary be able to choose between various measures to increase the margins.
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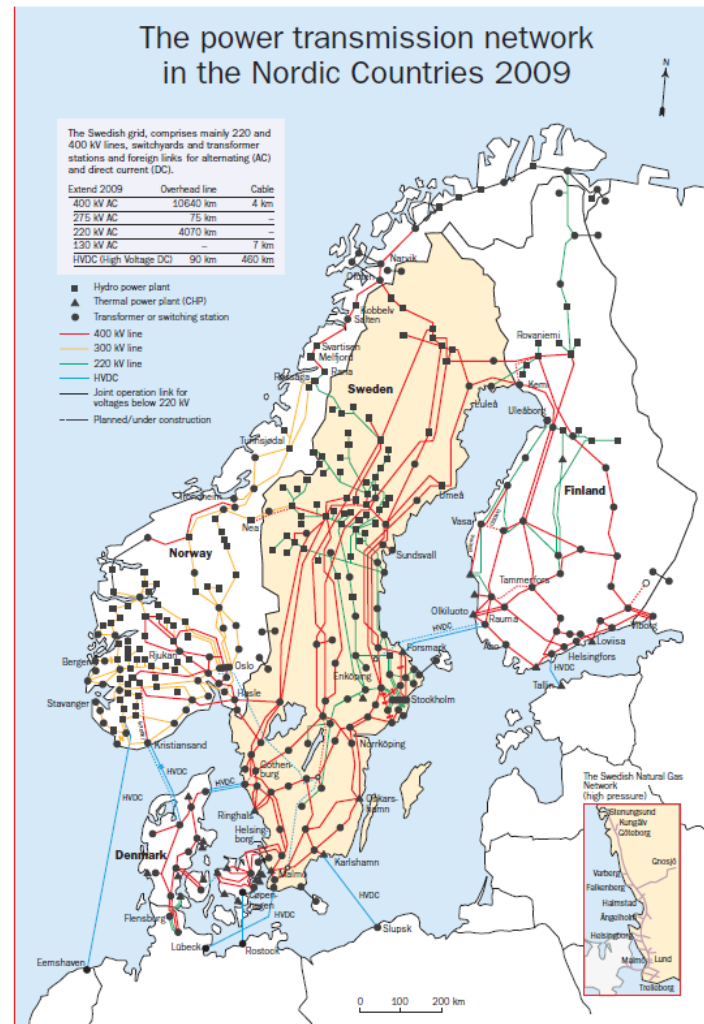
Power Systems

- Electric energy cannot be stored in practical power system applications
 - Power lines do not store energy
 - Plate capacitors store electric energy
 - Not much, not for so long
 - Non-electric energy storage in power systems
 - Pump storage (potential energy)
 - Chemical capacitors, (chemical energy, batteries)
 - Flywheels, rotating masses of generators (kinetic energy)
 - Electricity has to be generated the instant it is used
 - Automatic control systems are necessary in all larger power systems
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Synchronous Grids

- A power system connected by AC lines and transformers constitutes a **synchronous grid**.
 - There can only be one frequency in a synchronous grid.
 - **Analogies:**
 - Trains – each wagon has to travel in the same speed
 - If one locomotive stops, the speed goes down
 - Until the other locomotive(s) have compensated
 - The stable speed will be lower (primary control)
 - Create speed increase – stop when satisfied (secondary control)
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Synchronous Grids – Nordel



Frequency Range (1/4)

The frequency of a large power system must be kept around the nominal value!

- Certain frequencies can harm important equipment in the power system.
 - Harmonic vibrations in turbine blades and shafts.
 - Heating of generators and transformers.
 - Some loads might be disturbed.
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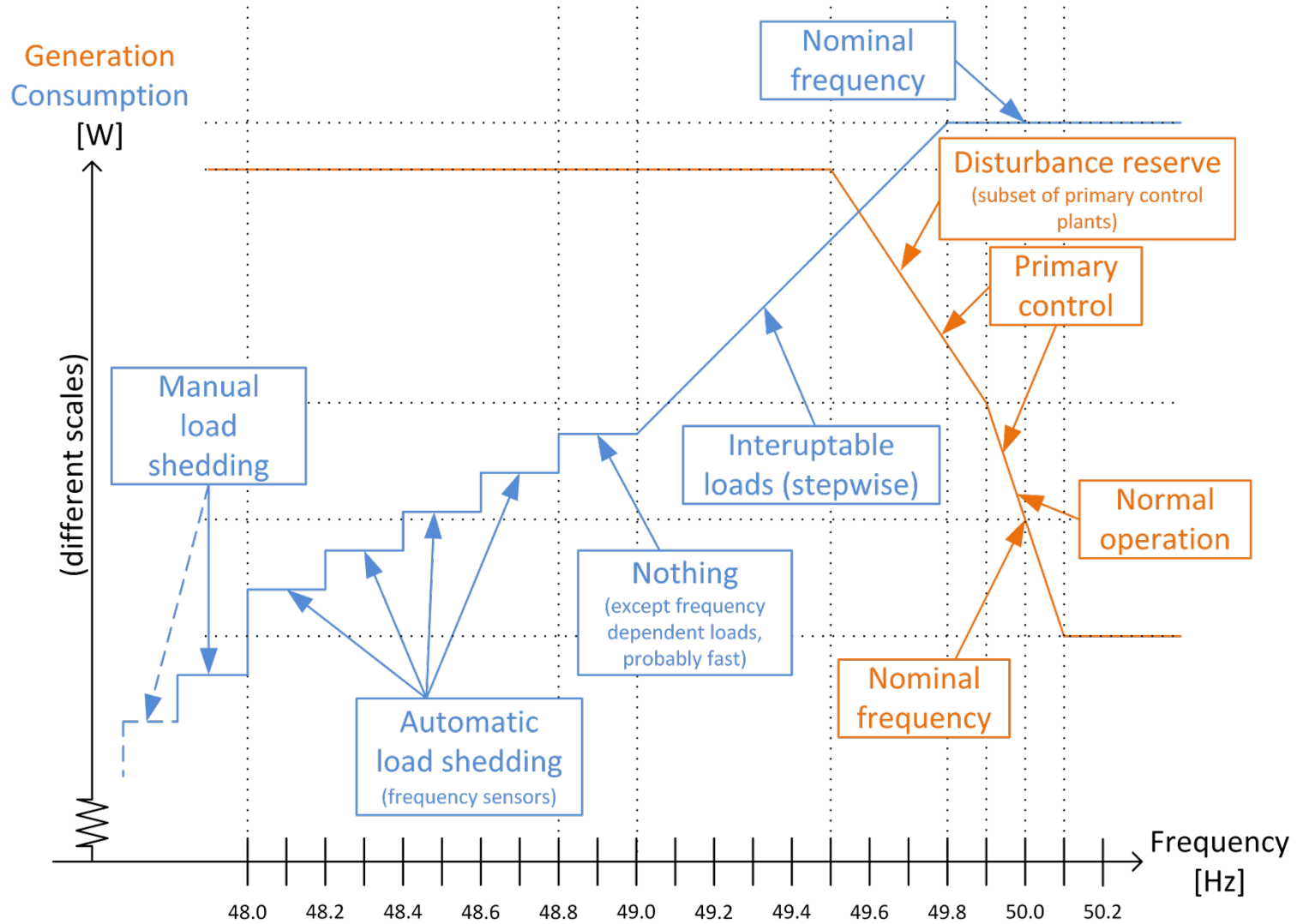
Frequency Range (2/4)

- Automatic control systems—primary control
 - Normal operation (In Sweden: 49.9 - 50.1 Hz)
 - Disturbance reserve (In Sweden: 49.5 – 49.9 Hz)
 - Disconnection of interruptible loads
 - (In Sweden: 49.0 - 49.8 Hz)
 - Export on HVDC lines
 - Electric boilers,
 - Heat pumps
 - Pumped storage hydro (no such in Sweden)
 - *Continues ...*
-

Frequency Range (3/4)

- *Continued ...*
 - Automatic load shedding
 - Stepwise, parts of distribution grids
 - (In Sweden: 49.0 - 49.8 Hz)
 - Manual load shedding (rotating load curtailment)
 - Larger areas, e.g. Stockholm Metropolitan Area
 - (In Sweden: < 48.0 Hz)
 - Never happened
 - **Note!**
 - We assume here the grid works perfectly
 - Blackouts have occurred at major transformer outages
 - Different countermeasures for that
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Frequency Range (4/4)



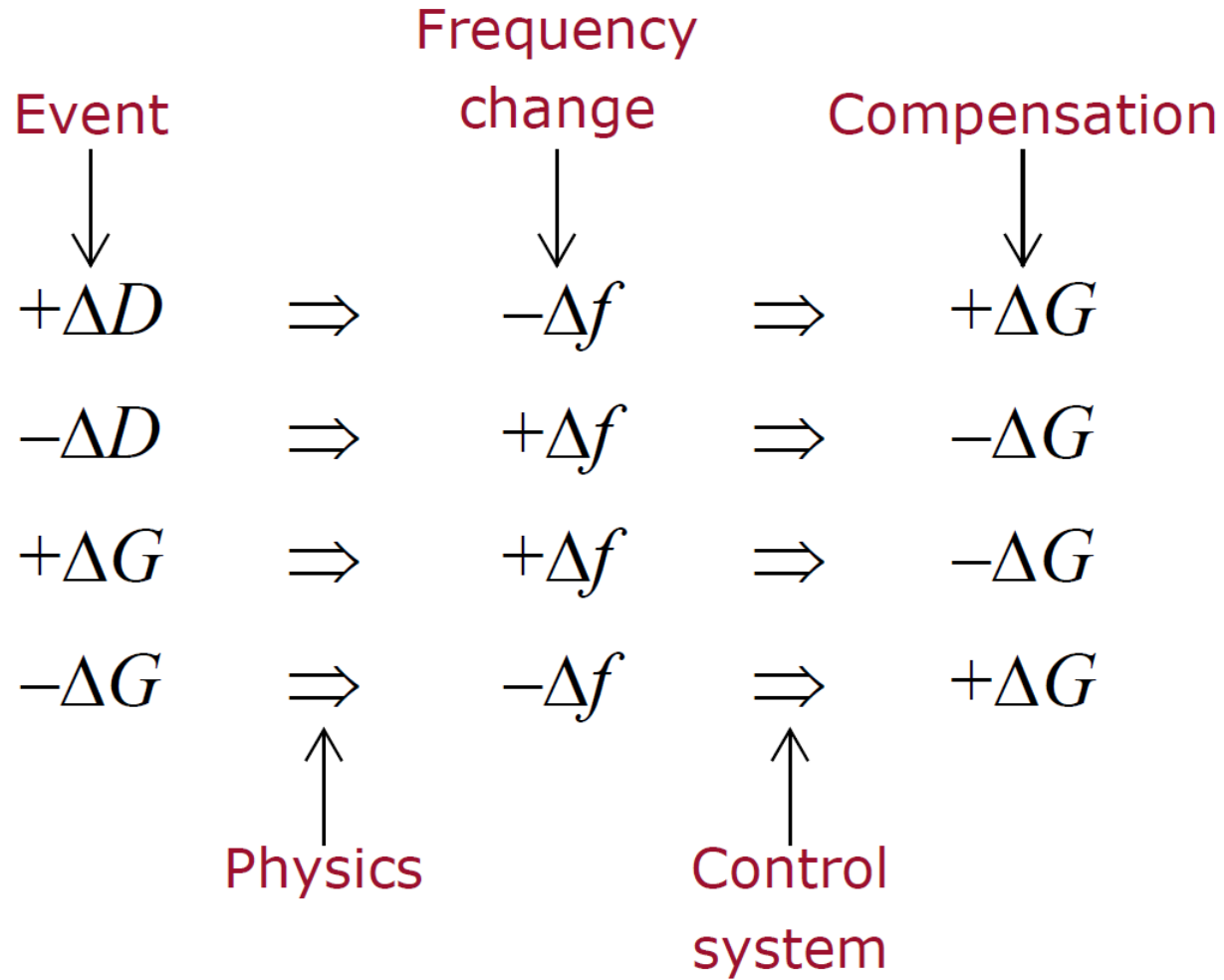
Primary Control

- The objective of the primary control is to maintain the balance between generation and load
 - In control theory, the primary control corresponds to a proportional controller (P controller).
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Primary Control – Load increase

- System in balance
 - Load increases – generation unaffected
 - Energy is taken from the kinetic energy of all synchronous machines.
 - The synchronous machines will rotate slower.
 - The frequency decreases.
 - Frequency sensors in some power plants
 - detect the frequency decrease
 - increase generation in that power plant until the frequency is stable again.
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Primary Control - Overview



Gain (1/7)

Definition 1: The gain states the change in generation for specific change in frequency:

$$G = G_0 - R(f - f_0)$$

where G_0 denotes the base generation, R the gains, f_0 the nominal frequency, and f the actual frequency.

Gain (2/7)

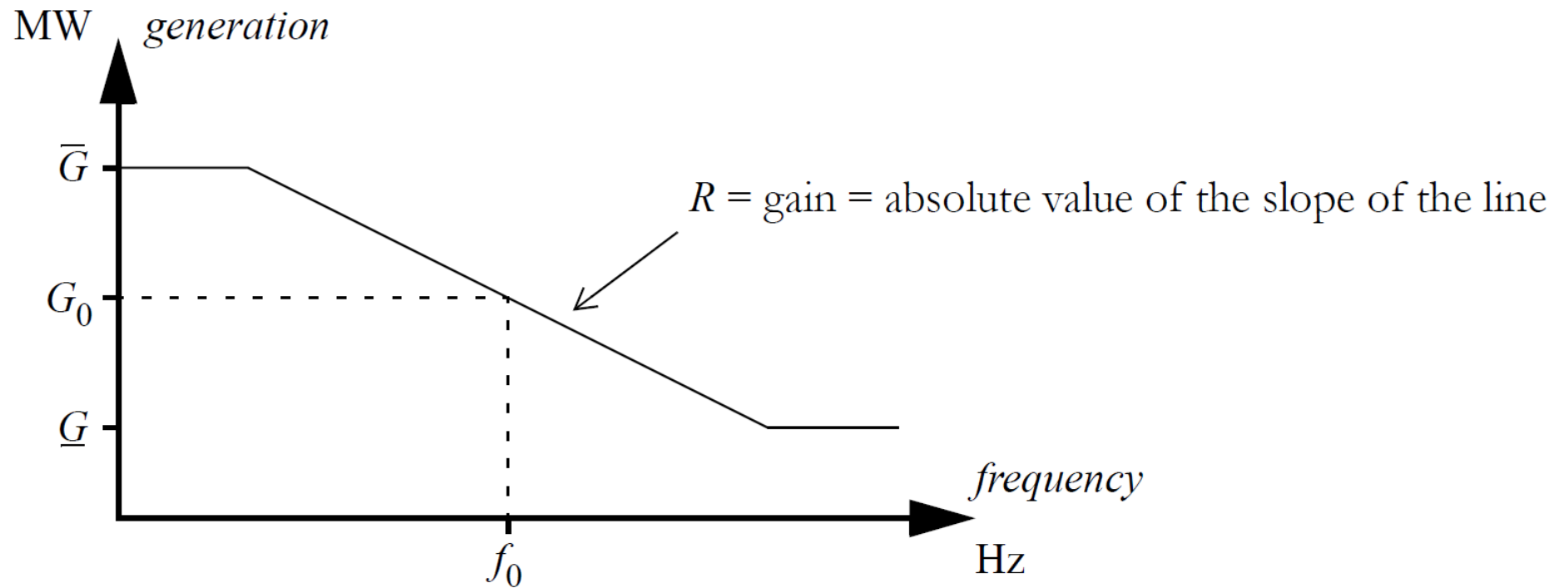


Figure 4.1 The relation between frequency and generation in a power plant participating in the primary control.

Gain (3/7)

Simpler to only consider the changes

$$\Delta G = R \cdot \Delta f$$

Example 1:

- Generation 1000 MW
 - Load 1000 MW
 - Gain 200 MW/Hz
 - Frequency 49.98 Hz
 - What is the new frequency going to be if the load increases by 10 MW?
-

Gain (4/7)

Example 1 (continued):

$$\Delta f = \frac{\Delta G}{R} = \frac{10}{200} = 0.05$$

- Load increase => Frequency increase
 - The new frequency: $49.98 - 0.05 = 49.93$ Hz
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Gain (5/7)

Example 2:

- One minute after the load increase in Example 1, the load decreases by 6 MW.
 - What is the new frequency going to be?
-

Gain (6/7)

Example 2 – Solution I

Compare to the situation **after** the load increase in Example 1

$$\Delta f = \frac{\Delta G}{R} = \frac{6}{200} = 0.03$$

- Load decrease => frequency increase
 - The new frequency is $49.93 + 0.03 = 49.96$ Hz
-

Gain (7/7)

Example 2 – Solution II

Compare to the situation **before** the load increase in Example 1

$$\Delta f = \frac{\Delta G}{R} = \frac{10 - 6}{200} = \frac{4}{200} = 0.02$$

- Load increase => frequency decrease
 - The new frequency is $49.98 - 0.02 = 49.96$ Hz
-

Limitations in primary control

- When designing a power system, it is important to consider that there are limitations to the primary control:
 - Plants in primary control have limited primary control reserves
 - The gain must be fairly even distributed in the system – in order not to overload transmission
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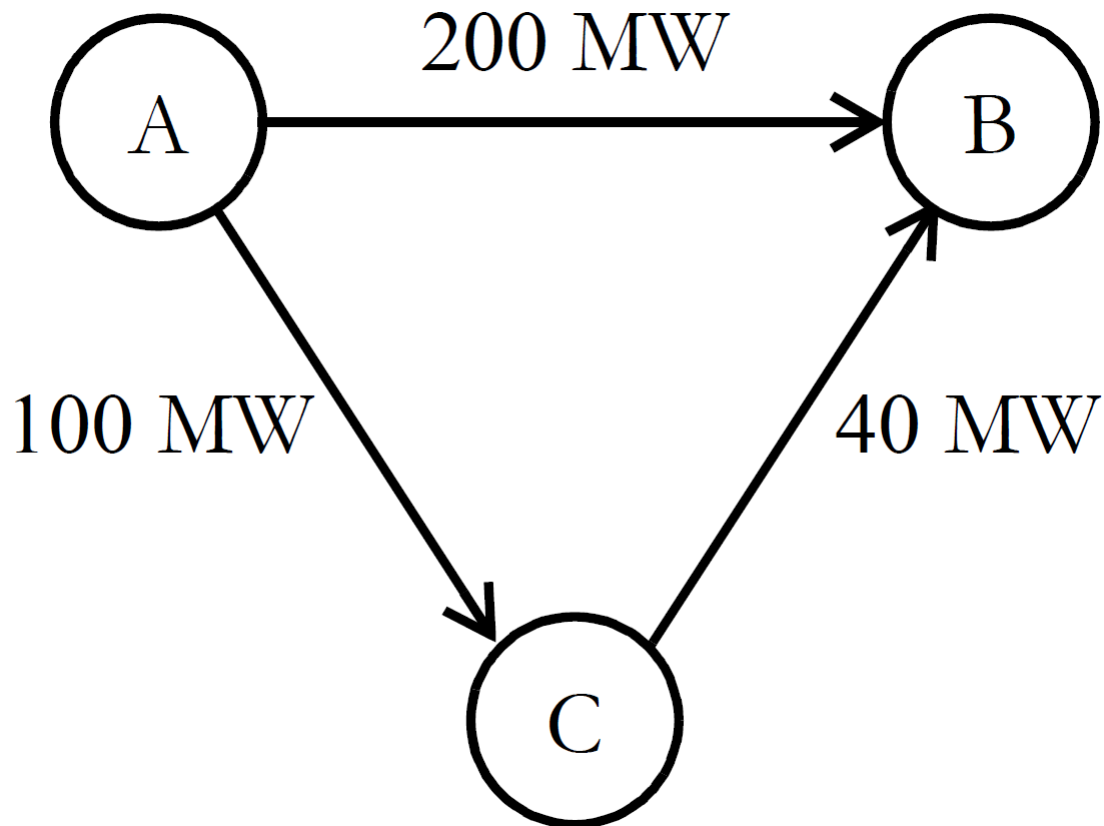
Example 4.1 - Problem

- Power system in balance, nominal frequency (50 Hz).
 - Two power plants participating in primary control:
 - Unit 1:
 - 500 MW capacity,
 - current generation 420 MW,
 - gain 300 MW/Hz
 - Unit 2:
 - 100 MW capacity,
 - current generation 75 MW,
 - gain 300 MW/Hz
 - 85 MW of generation is lost in another unit.
 - What is the frequency after restoring balance?
-

Example 4.1 - Solution

- Same gain \Rightarrow both units increase their generation by the same amount, i.e., $85/2 = 42.5$ MW.
 - Unit 2 can only increase generation by 25 MW!
 - When the frequency is about 49.916 Hz unit 2 will stop regulating.
 - To restore balance, unit 1 must increase its generation by $85 - 25 = 60$ MW.
 - $\Delta f = \frac{\Delta G}{R} = \frac{60}{300} \text{ Hz} = 0.2 \text{ Hz}$.
 - New frequency $f = 50 - 0.2 = 49.8 \text{ Hz}$.
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Example 4.2 - Problem



- $R_A = 900 \text{ MW/Hz}$
- $R_B = 50 \text{ MW/Hz}$
- $R_C = 50 \text{ MW/Hz}$
- $P_{AB} = 200 \text{ MW}$
- $P_{AC} = 100 \text{ MW}$
- $P_{BC} = -40 \text{ MW}$
- $\widehat{P}_{AB} = 300 \text{ MW}$
- $\widehat{P}_{AC} = 150 \text{ MW}$
- $\widehat{P}_{BC} = 120 \text{ MW}$
- 240 MW lost in area B
- Calculate the resulting
 - Frequencies, and
 - power flows induced by primary control

Example 4.2 – Solution (1/6)

- Generation has to increase by 240 MW.
 - The increase is distributed between the areas according to their share of the total gain,
 - $R_{ABC} = 900 + 50 + 50 = 1000 \text{ MW/Hz}$
 - $\Delta G_A = \frac{R_A}{R_{ABC}} \cdot 240 = 216 \text{ MW.}$
 - $\Delta G_B = \frac{R_B}{R_{ABC}} \cdot 240 = 12 \text{ MW.}$
 - $\Delta G_C = \frac{R_C}{R_{ABC}} \cdot 240 = 12 \text{ MW.}$
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Example 4.2 – Solution (2/6)

- Area A
 - Same load, increased generation => increased export
 - Only 150 MW export capacity available
 - Both transmission lines will be overloaded
 - The area is isolated from the rest of the system
 - Export reduced by 300 MW (compared to before fault)
 - Equivalent to a load reduce
 - Frequency increase $\Delta f_A = \frac{300}{900} \approx 0.33$ Hz
-

Example 4.2 – Solution (3/6)

- Areas B and C
 - Total deficit 540 MW
 - 240 MW lost generation
 - 300 MW lost import
 - Equal gain => both areas increase generation by 270 MW
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Example 4.2 – Solution (4/6)

- Area C
 - Increased export by 170 MW
 - Decreased import 100 MW
 - Increased generation 270 MW
 - Only 80 MW export capacity left
 - Transmission line overloaded
 - Area C is isolated from A since before, now also from B
 - Now there is a deficit of 60 MW compared to before fault
 - Lost 100 MW import from A
 - Lost 40 MW export to B
 - Frequency increase $\Delta f_C = \frac{60}{50} = 1.2 \text{ Hz}$
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Example 4.2 – Solution (5/6)

- Area B
 - Area is isolated – as well as the other two areas
 - Deficit of 480 MW
 - Lost 240 MW import and
 - Lost 240 MW generation
 - Frequency decrease $\Delta f_B = \frac{480}{50} = 9.6 \text{ Hz}$
-

Example 4.2 – Solution (6/6)

- Summary
 - All lines overloaded
 - New frequency in Area A: 50.33 Hz
 - New frequency in Area B: 40.4 Hz
 - New frequency in Area C: 48.8 Hz
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Primary control in restructured electricity markets

- The system operator is responsible for primary control, but does not have sufficient generation capacity.
 - Two solutions:
 - Require producers to supply certain amounts of gain to be allowed to connect to the grid.
 - Pay producers to supply gain.
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Primary control pricing

- The players who supply primary control to the system can be reimbursed for
 - provision of primary control capacity (€/MW·Hz)
 - utilization of primary control (€/MWh)
 - The energy price may for example be obtained from the real-time market.
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Costs of primary control (1/3)

- The costs of supplying primary control capacity depends on the generation technology.
 - Wind power, photovoltaics:
 - Non-dispatchable units \Rightarrow very high costs.
 - (ickereglerbara)
 - Hydro power:
 - Negligible fuel costs,
 - small efficiency losses
 - \Rightarrow Low costs.
 - *Continues ...*
-

Costs of primary control (2/3)

- The costs of supplying primary control capacity depends on the generation technology.
 - *Continued ...*
 - Large thermal units:
 - Fuel costs,
 - efficiency losses
 - ⇒ high costs.
 - Nuclear power plants:
 - Designed to be operated at installed capacity
 - ⇒ quite high costs.
 - *Continues ...*
-

Costs of primary control (3/3)

- The costs of supplying primary control capacity depends on the generation technology.
 - *Continued ...*
 - Small thermal units:
 - Fuel costs,
 - small efficiency losses
 - ⇒ rather high costs.
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Primary control reserves

- The capacity available for primary control depends on the requirements for the system.
 - **Example:** The Nordic system
 - Total gain $R = 6\ 000\ \text{MW/Hz}$
 - Primary control should work properly for frequencies within $50 \pm 0.1\ \text{Hz}$
 - The necessary reserves are $\Delta G = R \cdot \Delta f = 600\ \text{MW}$.
-

Secondary control (1/2)

The objective of the secondary control is to

- restore the frequency to its nominal value,
- release used primary control reserves,
- reduce the integrated time error.

In control theory, the secondary control corresponds to an integral controller (I controller).

Secondary control (2/2)

Secondary control operates by changing the base generation* of the system.

Examples of such:

- Change generation in a power plant that is not participating in the primary control.
- Change base generation in a power plant that is participating in the primary control.

* By which we mean the generation at nominal frequency

Controlling the frequency (1/2)

- If the frequency is less than the nominal then
 - some generation capacity needs to be started, or
 - the load decreased.
 - If the frequency is larger than the nominal then
 - some generation capacity needs to be stopped, or
 - the load increased.
 - In both cases, some primary control reserves will be released.
-

Controlling the frequency (2/2)

Secondary control can be performed by

- Automatic control systems
 - (AGC – Automatic Generation Control).
 - Manual control (using real-time trading).
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Time Error

- The integrated time error is the deviation between
 - normal time and
 - synchronous time
 - (i.e., a clock controlled by the grid frequency).
- The time deviation during a certain period T in a 50 Hz system is given by

$$t_d = \int_0^T \frac{f(\tau) - 50}{50} d\tau$$

Controlling the time error

- To reduce a **negative** time error, the frequency must be **larger** than the nominal value for some time.
 - To reduce a **positive** time error, the frequency must be **lower** than the nominal value for some time.
 - generally not a problem
 - system components less sensitive for under-frequencies
 - The time error is not considered very important for the operation of the power system.
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Time Error - Example

- Current time deviation: -2 s.
- Frequency the next five minutes: 50.1 Hz.
- What is the time deviation after this period?
- Solution:
- During each second the grid clock will pass 0.1 cycles more than normal time.
- Grid clock will gain $0.1/50 \cdot (5 \cdot 60) = 0.6$ s compared to normal time.
- Time error after five minutes

$$t_d = -2 + 0.6 = -1.4 \text{ s}$$

Time Error – Practical usage (1/4)

The time error can be used to calculate the real-time trading of a balance responsible player participating in primary control:

Example:

- Power Ltd. is a balance responsible player.
 - During the trading period 9-10 am. (09.00-10.00) they have sold
 - 3 000 MWh to the power pool, and
 - 3 560 MWh directly to consumers.
-

Time Error – Practical usage (2/4)

- The generation in the base power plants of the company (i.e., power plants not participating in primary control) was 4 650 MWh.
 - Power Ltd. also has power plants participating in the primary control
 - Base generation (G0) 2 000 MW
 - Gain (R) 1 000 MW/Hz
 - Neglect limitations in primary control reserves
 - The time error
 - 09:00 is -0.42 and
 - 10:00 is $+0.30$.
-

Time Error – Practical usage (3/4)

- The relation between frequency and time deviation is linear \Rightarrow Assume constant frequency during the hour.
- The grid clock changes by $(f - 50)/50$ s every second.
- The total change during 3 600 s is +0.72 s $\Rightarrow f = 50.01$ Hz.
- At $f = 50.01$ Hz, the power plants participating in primary control generate

$$G = G_0 - R(f - f_0) = 2000 - 1000(50 - 50.01) = 2000 - 10 = 1990 \text{ MW}$$

Time Error – Practical usage (4/4)

- Hence, Power Ltd. is buying 10 MWh from the system operator during the real-time trading.
 - The imbalance of Power Ltd. Is
$$4\,650 + 1\,990 + 10 - 3\,000 - 3\,560 = 70 \text{ MWh}$$
 - i.e., the company must sell **70 MWh** imbalance power to the system operator.
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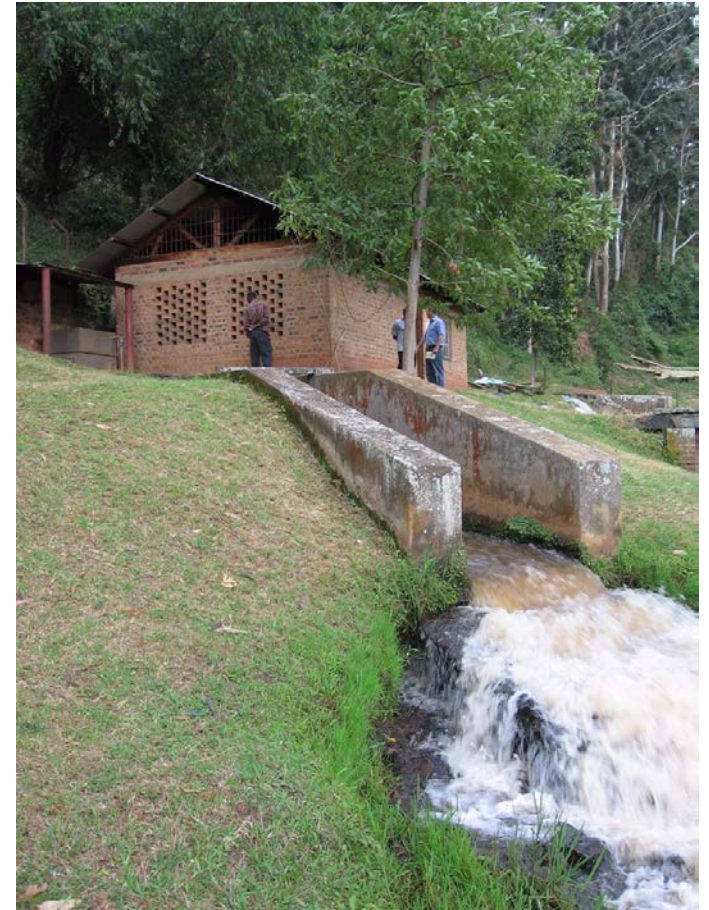
Frequency control in smaller power systems – Load control (1/2)

- It might be preferable to let the primary control govern the electrical load instead of the mechanical input.
 - If the generation is larger than the load, the load is increased in a “dummy load” (for example a water heater).
 - In railways – voltage control instead of frequency control:
 - If braking too hard regeneratively – heating resistors
 - Example:
 - Stand-alone hydro power plant, which is always operating at installed capacity.
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Frequency control in smaller power systems – Load control (2/2)



Kisiizi Hydro Power Plant, Uganda



Frequency control in smaller power systems – DC generation

- DC generators can feed an AC grid via an **inverter**.
 - A control system for the DC generator and inverter is necessary if there is no synchronous generator in the system.
 - **Example:** Solar home system.
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Time for "Lecture Assignments"

- On another slideshow ...
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