

# Mechanistic Empirical Design Exercise

AC thickness optimization against top down cracking

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Road Construction and Maintenance (AF 2903)

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1. The following four layer pavement system has to be checked against top down fatigue cracking. The pavement is subjected to a single-axle dual-wheel load of magnitude 22480pound (100KN) and a tyre pressure of 166psi (800KPa). The spacing between the dual wheels is 12inch (30.5cm) center-to-center. The expected traffic during the design period is 10 million ESALs and it is designed with a reliability of 95%. The design period is 20 years and the pavement is located in an area with a mean annual air temperature (maat) of 75°F. A reference temperature of 50°F should be used to predict aging condition).

The tensile stress at the bottom of the AC layer for the trial pavement system should be calculated based on the following structure. **Use English units in the Matlab calculation (inch, psi...)**

- AC layer: thickness 4.5 inch, AC stiffness, from AC stiffness predictive model
- Base layer: thickness 12 inch, modulus 63600 psi
- Subbase layer: thickness 12 inch, modulus 51000 psi
- Subgrade: semi-infinite layer 999 inch, modulus 361000 psi

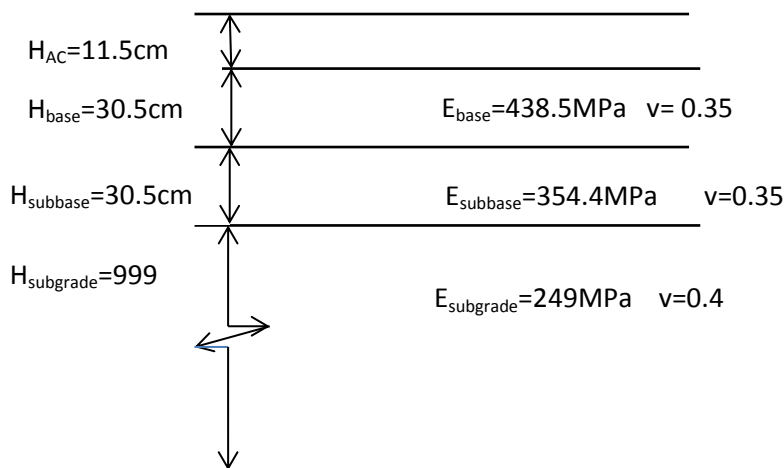


Figure 1 Pavement system

The aging effect on the AC stiffness is considered by dividing the AC layer into sub-layers and since aging is most pronounced close to the surface, the Ac stiffness can be obtained at  $1/8H_{AC}$  and  $1/2H_{AC}$ .

A predictive equation is provided to calculate the AC stiffness, tensile strength and creep parameters at different depths in the AC layer. Use time of loading  $t=0.1$  sec for the AC stiffness prediction and  $t=1800$  sec for tensile strength prediction.

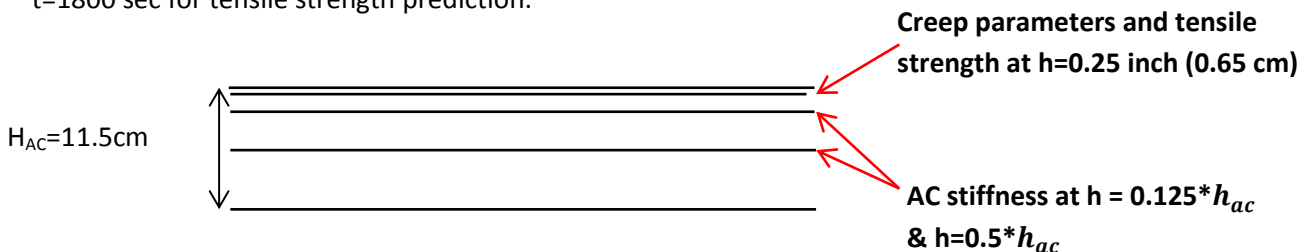


Figure 2 AC layer

Use the following mix gradation, volumetrics and rheological properties of the AC layer as input in the predictive equations.

Gradation (Percent passing by weight)				Volumetric		Rheological properties	
$\rho_{\frac{3}{4}}$ (19 mm)	$\rho_{\frac{3}{8}}$ (9.5 mm)	$\rho_4$ (4.75 mm)	$\rho_{200}$ (0.075 mm)	$V_a$ (%)	$V_{beff}$ (%)	A	VTS
100	93.7	74.6	5.6	3.2	10.7	10.6316	-3.548

## Tasks

1. Estimate the energy ratio optimum,  $ER_{opt}$

- Uncomment line 13 to 21 in the file *eropt.m* and write the necessary expression for energy ratio optimum for the given reliability

$$\begin{array}{l}
 \text{Reliability (\%)} \qquad \qquad \qquad ER_{opt} = f(x: \text{ESALs in 10 millions}) \\
 \qquad \qquad \qquad x < 0.14 \qquad \qquad \qquad 0.14 \leq x < 0.8 \qquad \qquad \qquad x \geq 0.8 \\
 95 \qquad \qquad ER_{opt} = 0.329x + 0.65 \qquad ER_{opt} = 0.640x + 0.61 \qquad ER_{opt} = 0.256x + 0.92
 \end{array}$$

- Use traffic, reliability and the file *fcm.m* to determine  $ER_{opt}$

2. Estimate the tensile strength  $S_t$

- Uncomment line 19 and 20 in the file *tensile\_strength.m* and write the necessary expression for the curve fitting parameters (delta and alpha)

$$\begin{aligned}
 \delta = & 2.718879 + 0.079524 \times p_{200} - 0.007294 \times (p_{200})^2 + 0.002085 \times \rho_4 \\
 & - 0.01293 \times V_a + 0.08541 \frac{V_{be}}{V_{be} + V_a}
 \end{aligned}$$

$$\begin{aligned}
 \alpha = & 3.559267 - 0.005451 \times \rho_4 + 0.020711 \times p_{3/8} - 0.000351 \times (p_{3/8})^2 \\
 & + 0.00532 \times p_{3/4}
 \end{aligned}$$

$\rho_{3/4}, \rho_{3/8}, \rho_4$  : percent weight retained on 19mm, 9.5mm and 4.75mm sieve respectively

$\rho_{200}$  : percent passing on 0.075 mm sieve

$V_a$ : Air void  $V_{be}(V_{beff})$ : effective asphalt content

- To determine the tensile strength uncomment line 40 in the same file and write the tensile strength predictive equation, use the regression constants at line 7 & 8 and tensile dynamic modulus at line 39

$$S_t = \sum_{n=0}^5 a_n \cdot (\log S_f)^n$$

- Use the required inputs and the file *fcm.m* to determine the tensile strength

### 3. Estimate creep parameters $D_1$ and $m$

- Uncomment line 16 and 17 in the file *creep\_parameters.m* and write the necessary expression for the curve fitting parameters (delta and alpha).
- To determine  $D_1$  and  $m$  uncomment lines 29 and 31 and write the necessary description for  $D_0$  and temp

$$\log(D_0) = -\delta - \alpha - \log \lambda_r, \quad \log(D_0 + D_1) = -\delta - \frac{\alpha}{1 + e^\beta} - \log \lambda_r$$

$$m_0 = \alpha \gamma \times \frac{\exp(\beta + 3\gamma)}{[1 + \exp(\beta + 3\gamma)]^2} \quad m = m_0 + \frac{\kappa}{\log \log \eta}$$

- Use the required inputs and the file *fcm.m* to determine  $D_1$  and  $m$

### 4. Determine the AC thickness $H_{tot}$

- Uncomment line 12 and 13 in the file *AC\_modulus.m* and write the necessary expression for the curve fitting parameters (delta and alpha)
- Uncomment line 21 and specify depth levels at which the AC Stiffness has to be calculated.
- Open and run the file *fcm.m* after you have inputted all the necessary inputs to get optimized thickness