



# AF2901 Road and Railway Track Engineering

## Life Cycle Cost Analysis

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- A process for evaluating the total economic worth of a useable project segment by analyzing initial costs and discounted future costs, such as resurfacing costs, over the life of the project
- The concept was introduced in the 1930s as part of U.S. federal legislation regarding flood control
- From the beginning of 1950s it has begun to be used for the evaluation of highway projects

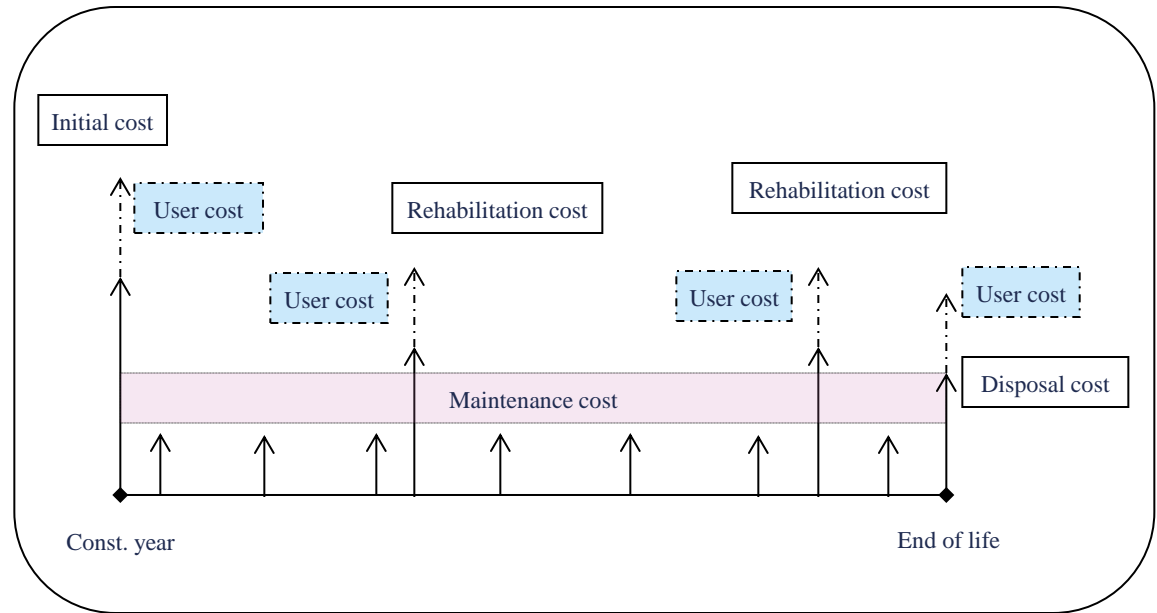
- The value of money today and money that will be spent in the future are not equal.
  - This concept is referred to as the “time value of money”.
- The time value of money results from two factors: (1) inflation, which is erosion in the value of money over time, and (2) opportunity cost.
- For cash or existing capital, opportunity cost is equivalent to the benefit the cash could have achieved had it been spent differently or invested. For borrowed money, opportunity cost is the cost of borrowing that money (e.g., the loan rate).

- Inflation reduces the value or purchasing power of money over time
- It is the result of the gradual increase in the cost of goods and services due to economic activity

$$\text{Dollars}_{\text{base year}} = \text{Dollars}_{\text{data year}} \times \frac{\text{Price Index}_{\text{base year}}}{\text{Price Index}_{\text{data year}}}$$

# Net Present Value

$$NPV = \text{Initial Cost} + \sum_{t=1}^N \text{Future Cost} \times \left[ \frac{1}{(1+i)^t} \right]$$



$$NPV = \text{Initial Cost} + \sum_{n=0}^L \frac{\text{Rehab Cost}_n}{(1+i)^n} + \text{Annual Operating Cost} \times \frac{(1 - (1+i)^{-n})}{i}$$

$$EAC = NPV \times \frac{i}{1 - (1+i)^{-n}}$$

# Discount factor

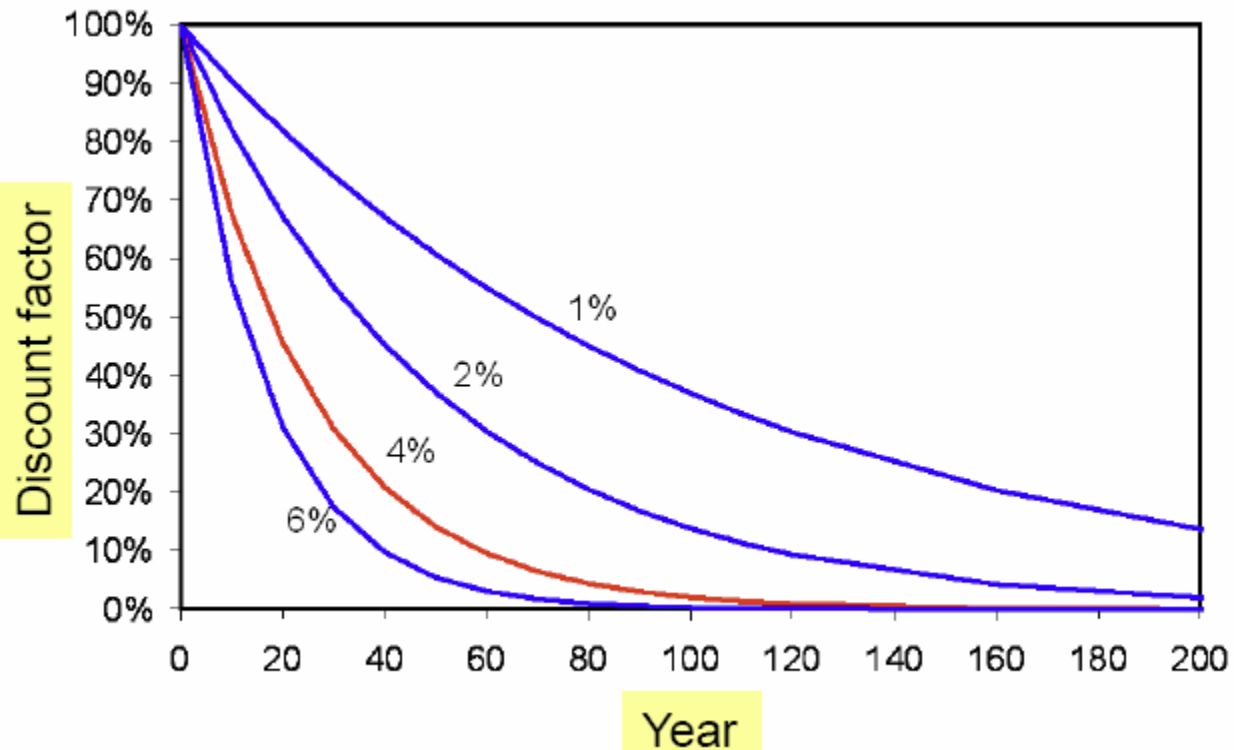
$$NPV = Value \cdot \frac{1}{(1+r)^n}$$

Discount factor (DF)

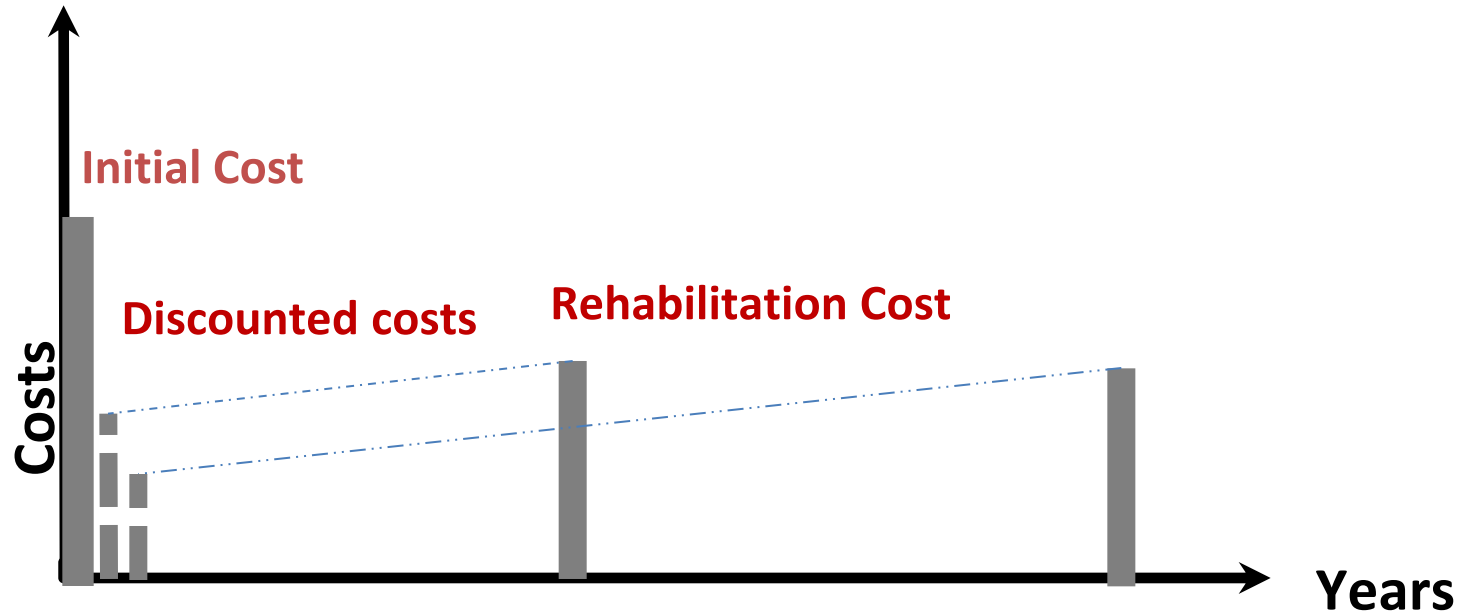
where

$r$  = rate of return

$n$  = number of years



# Net Present Value



$$r = \frac{1 + i}{1 + j} - 1$$

where:

Discount = calculated discount rate,

*interest* = expected interest rate, and

*inflation* = expected inflation rate.

- Costs for Production, Transportations, Laying

Const.  
Agency



- Costs for Production, Transportations, Milling, Remixing, Laying

Rehab.  
Agency



- Costs Related to Delay, and Energy Consumption, ...

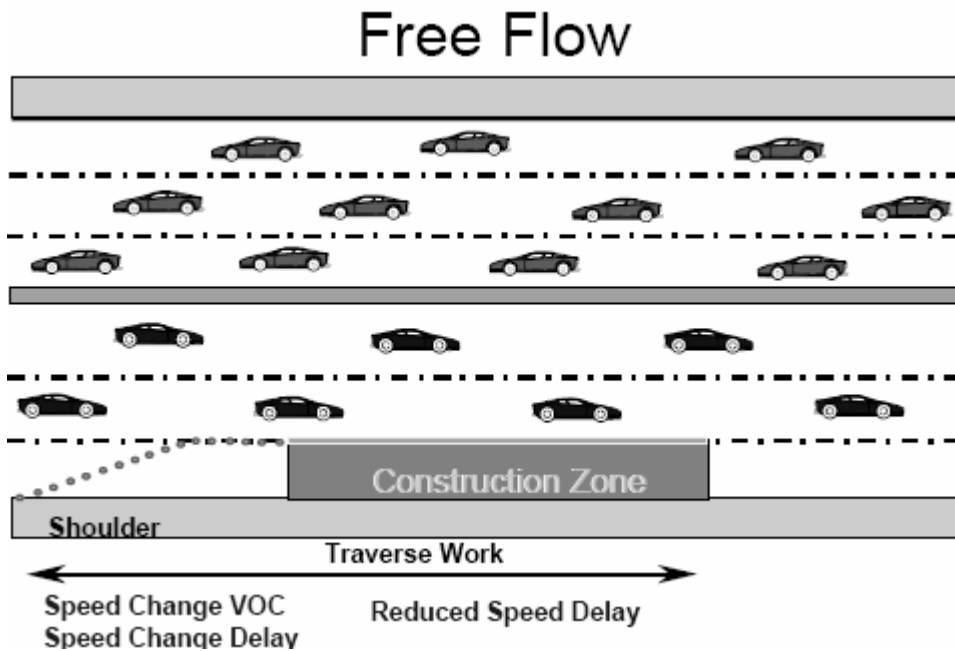
Road  
Users





- For early construction completion, maintenance and rehabilitations
- Delay-of-use
- Time delay
- Fuel consumption
- Driver discomfort
- Vehicle operating costs
- Accidents

# Road user costs

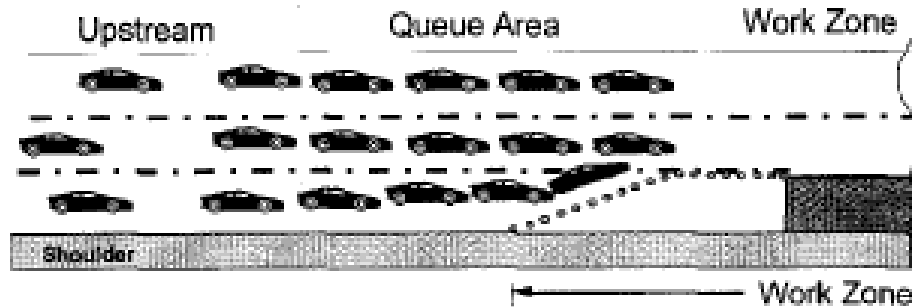


- ❖ Maximum capacity for 2-lane directional freeway = 2200
- ❖ Lane width = 3,5 m
- ❖ No. Of lanes in each direction = 2
- ❖ Heavy vehicles proportion = % 12



Free Flow Capacity = 2075 vphpl

## Forced Flow



Speed Change  
VOC & Delay

Stopping  
VOC & Delay

Queue  
Idling & Delay

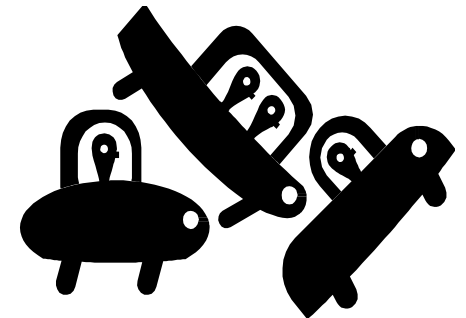
Reduced Speed Delay  
(Traverse Work Zone)

| Directional Lanes    |                         | Number<br>of<br>Studies | Average Capacity     |                               |
|----------------------|-------------------------|-------------------------|----------------------|-------------------------------|
| Normal<br>Operations | Work Zone<br>Operations |                         | Vehicles Per<br>Hour | Vehicles per<br>Lane per Hour |
| 3                    | 1                       | 7                       | 1,170                | 1,170                         |
| 2                    | 1                       | 8                       | 1,340                | 1,340                         |
| 5                    | 2                       | 8                       | 2,740                | 1,370                         |
| 4                    | 2                       | 4                       | 2,960                | 1,480                         |
| 3                    | 2                       | 9                       | 2,980                | 1,490                         |
| 4                    | 3                       | 4                       | 4,560                | 1,520                         |

## Accident Costs:

$$AC = L \times ADT \times N \times (Aa - An) \times ca$$

- $L$  = Length of affected road way
- $ADT$  = Average daily traffic (vehicles per day)
- $N$  = number of days of maintenance activity
- $Aa$  = Accident rate during maintenance activity
- $An$  = Normal accident rate
- $ca$  = Cost per accident



# Life-Cycle Cost Analysis

## RealCost


### USER MANUAL



U.S. Department of Transportation  
Federal Highway Administration

RealCost v. 2.1

**Traffic Data** [X]

|   |                                       |
|---|---------------------------------------|
| AADT Construction Year (total for both directions):   | <input type="text" value="75400"/>    |
| Single Unit Trucks as Percentage of AADT (%):   | <input type="text" value="5"/>        |
| Combination Trucks as Percentage of AADT (%):   | <input type="text" value="6"/>        |
| Annual Growth Rate of Traffic (%):  | <input type="text" value="1.25"/> ... |
| Speed Limit Under Normal Operating Conditions (mph):  | <input type="text" value="65"/>       |
| Lanes Open in Each Direction Under Normal Conditions:   | <input type="text" value="3"/>        |
| Free Flow Capacity (vphpl):   | <input type="text" value="2085"/> ... |
| Free Flow Capacity Calculator  |                                       |
| Queue Dissipation Capacity (vphpl):   | <input type="text" value="1800"/> ... |
| Maximum AADT (total for both directions):   | <input type="text" value="250000"/>   |
| Maximum Queue Length (miles):   | <input type="text" value="100"/>      |
| Rural or Urban Hourly Traffic Distribution:   | <input type="text" value="Urban"/> ▼  |

**Value of User Time** [X]

Value of Time for Passenger Cars (\$/hour):  ...

Value of Time for Single Unit Trucks (\$/hour):  ...

Value of Time for Combination Trucks (\$/hour):  ...

**Probability Function** [X]

Variable Name:

Probability Distribution:  ▼

Value:

**Probability Function** [X]

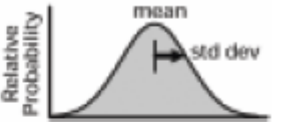


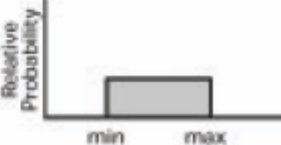
Variable Name: Value of Time for Passenger Cars

Probability Distribution: **Deterministic**

Value:

- Deterministic
- Uniform
- Normal**
- Log Normal
- Triangular
- Beta
- Geometric
- Truncated Normal

Ok Cancel

| Distribution Type | Spreadsheet Formula                                   | Illustration   |
|-------------------|---|--|
| Normal            | lccanormal (mean, std dev)                            |  <p>Relative Probability</p> <p>mean</p> <p>std dev</p>                 |
| Truncated Normal  | lccatnormal (mean, std dev, lower bound, upper bound) |  <p>Relative Probability</p> <p>mean</p> <p>std dev</p> <p>min max</p> |
| Triangular        | lccatriang (minimum, most likely, maximum)            |  <p>Relative Probability</p> <p>most likely</p> <p>min max</p>        |
| Uniform           | lccauniform (minimum, maximum)                        |  <p>Relative Probability</p> <p>min max</p>                           |



# NPV Computation using Monte Carlo

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Combine Variability of Inputs to Generate a Probability Distribution of Results

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$$\text{NPV} = \text{Initial Cost} +$$



$$\sum \text{Future Cost} \times \left[ \frac{1}{(1 + i)^n} \right]$$

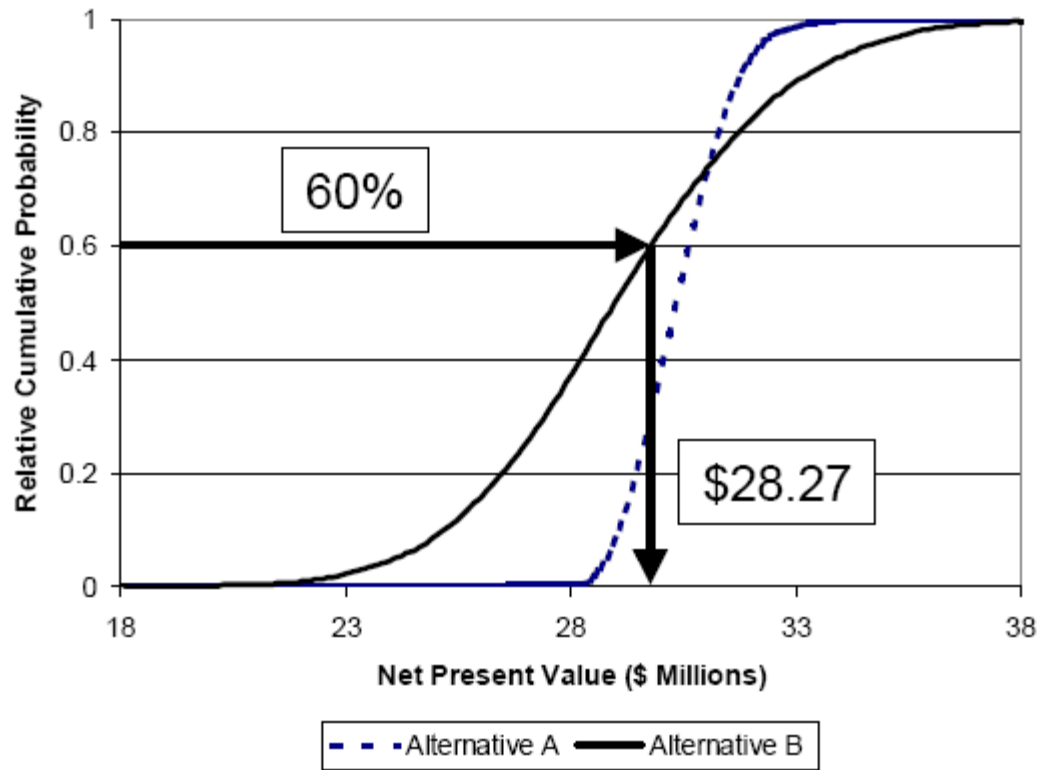
# Deterministic Results

**Deterministic Results** ✖

Deterministic Results

| Total Cost                       | Alternative 1: Hot Mix Asphalt -<br>Deterministic Class Exercise |                    | Alternative 2: Stone Matrix Asphalt -<br>Deterministic Class Exercise |                    |
|----------------------------------|--|--------------------|---|--------------------|
|                                  | Agency Cost<br>(\$1000)  | User Cost (\$1000) | Agency Cost<br>(\$1000)   | User Cost (\$1000) |
| <b>Present Value</b>             | <b>\$5,909.73</b>  | <b>\$21,450.18</b> | <b>\$6,026.59</b>   | <b>\$18,764.58</b> |
| Lowest Present Value Agency Cost | <b>Alternative 1: Hot Mix Asphalt</b>                            |                    |   |                    |
| Lowest Present Value User Cost   | <b>Alternative 2: Stone Matrix Asphalt</b>                       |                    |   |                    |

# Probabilistic Results



- The inflation indexes are suggested to be chosen from broad (e.g., Gross Domestic Product chain deflator) to intermediate (e.g., a Consumer Price Index) to narrow sector (e.g., highway construction or resurfacing cost such as road construction index (Vägindex)) depend on how results are to be interpreted

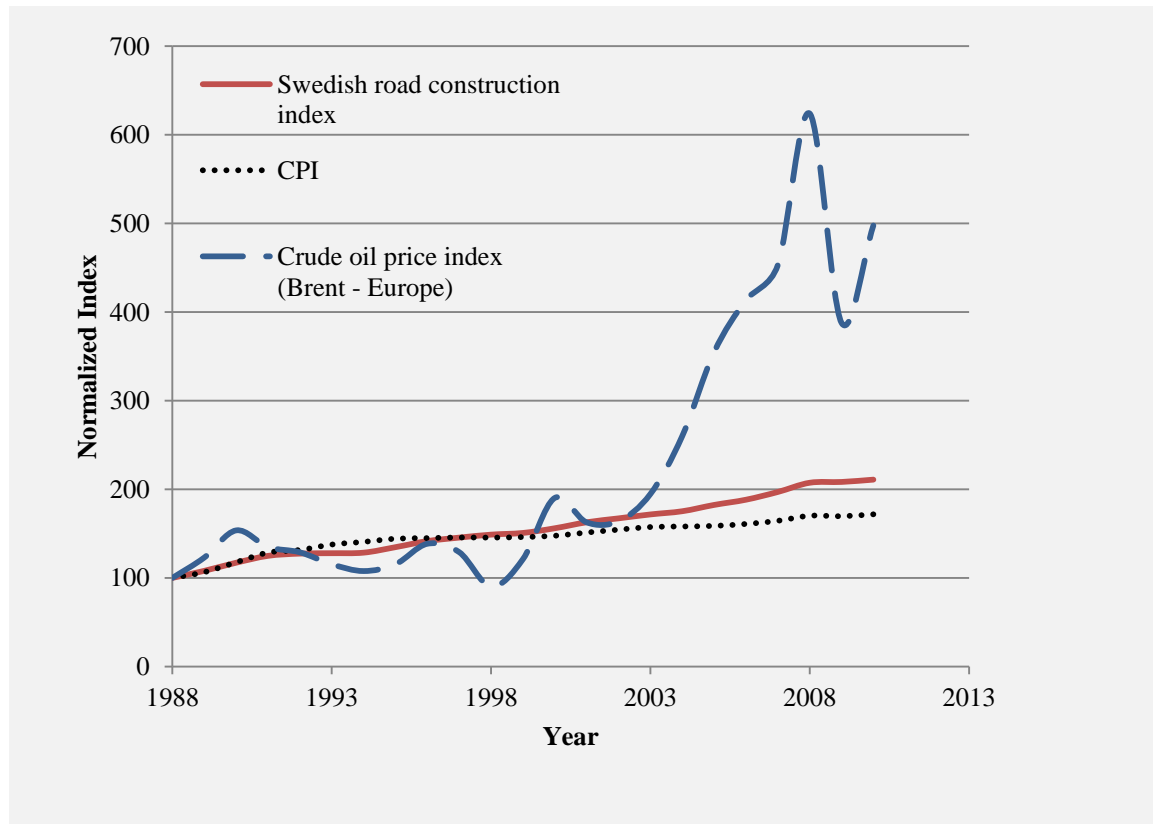
| Description   | Near-Term Value<br>(Years 0-5) | Long-Term Value<br>(Years 6+) |
|---|--------------------------------|-------------------------------|
| “Nominal” U of C Discount Rate                                  | 6%                             | 7%                            |
| Inflation   | 1.5%                           | 3.0%                          |
| “Real” U of C Discount Rate<br>(Adjusted to take out inflation) | 4.4%                           | 3.9%                          |

$$r = \frac{1+i}{1+j} - 1$$

- Recognizing that the broader indices may not adequately reflect the development of future costs related to road construction, the Swedish Transport Administration adopted a road construction cost index entitled the 'Vägindex' (STA, 2012)
- The use of the Vägindex was criticized by the Swedish National Audit Office (NAO, 2010)

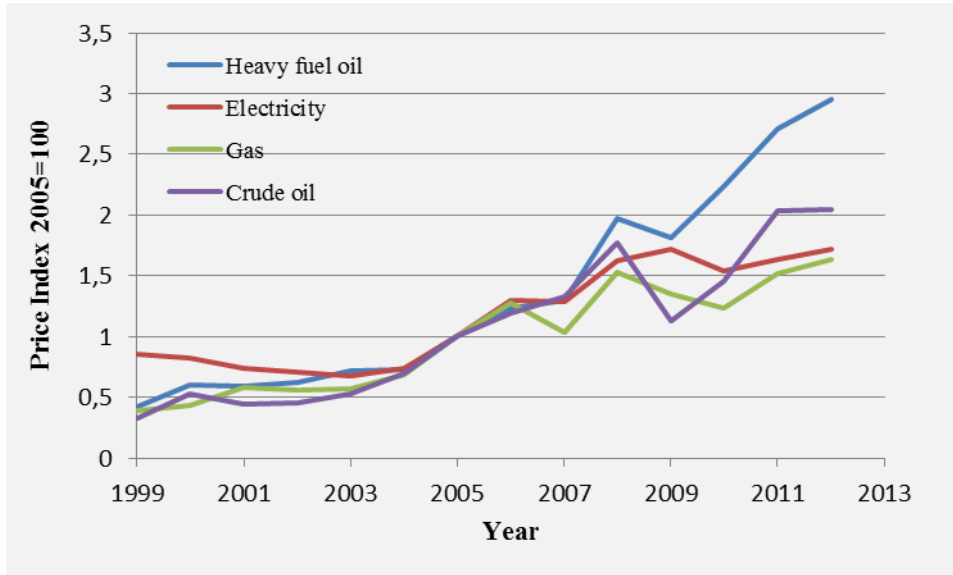
- Cost trends in the road construction sector are not comparable with that of the general economy
- The use of Vägindex does not adequately reflect the cost increases resulting from the relatively high price trends in the construction industry
- The widespread use of Vägindex is likely to reduce the awareness of potential future costs at the Swedish Transport Administration since fundamental cost drivers may be disguised

- Trafikväverket (2009) and SCB (2012)



- A significant part of the costs associated with asphalt pavements is related to the cost of oil products such as bitumen, fuel oil and transportation fuel.
- Therefore, application of one generalized inflation index based on Vägindex or CPI on the total cost may lead to a false estimation of future costs





- Products refined from crude oil, such as transportation fuels, gas oil and fuel oil, are obviously closely linked to the price of crude oil and follow oil price fluctuations
- There is a lag between the change in the price of oil and that of other fuels
- The lag is shortest for oil products, like fuel oil
- For electricity the lag is delayed

# Energy cost calculation

|                           | Crude oil<br>(MJ) | Energy<br>source A<br>(MJ) | Energy<br>source B<br>(MJ) | Cost of<br>Energy (€) |
|---------------------------|-------------------|----------------------------|----------------------------|-----------------------|
| Bitumen                   | $qc_1$            | -                          | -                          | $E_1$                 |
| Modifier                  | $qc_2$            | -                          | -                          | $E_2$                 |
| Aggregate production      | -                 | $qa_3$                     | $qb_3$                     | $E_3$                 |
| Bitumen production        | -                 | $qa_4$                     | $qb_4$                     | $E_4$                 |
| Modifier production       | -                 | $qa_5$                     | $qb_5$                     | $E_5$                 |
| Asphalt production        | -                 | $qa_6$                     | $qb_6$                     | $E_6$                 |
| Transportation            | -                 | $qa_7$                     | $qb_7$                     | $E_7$                 |
| Laying asphalt            | -                 | $qa_8$                     | $qb_8$                     | $E_8$                 |
| Compacting asphalt        | -                 | $qa_9$                     | $qb_9$                     | $E_9$                 |
| <i>User's energy loss</i> | -                 | $qa_{10}$                  | $qb_{10}$                  | $E_{10}$              |

$$E_k = c_k \times P_c + a_k \times P_a + b_k \times P_b + \dots$$

Where:

$P_c$ ,  $P_a$ ,  $P_b$  are the unit cost (€/MJ) of crude oil, energy source A and energy source B

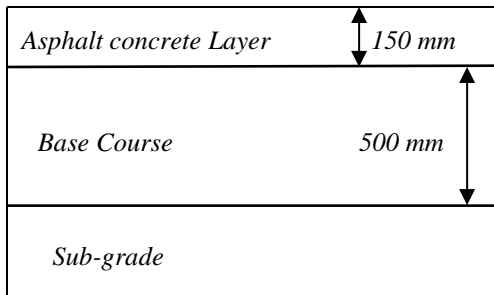
|                              | Item                    | Time Spent (Hr.) | Value of time (€/Hr.) | Cost of time (€) |
|------------------------------|-------------------------|------------------|-----------------------|------------------|
| <b>Labor &amp; Equipment</b> | Transportation          | $t_1$            | $C_L$                 | $T_1$            |
|                              | Laying asphalt          | $t_2$            | $C_L$                 | $T_2$            |
|                              | Compacting asphalt      | $t_3$            | $C_L$                 | $T_3$            |
|                              | Milling and resurfacing | $t_4$            | $C_L$                 | $T_4$            |
| <b>Road users</b>            | <i>User's time loss</i> | $t_5$            | $C_u$                 | $T_5$            |

$$NPV = \left[ \sum_{k=0}^n E_k \times (1 + j_c)^y + \sum_{k=0}^n T_k \times (1 + j)^y \right] \times \left( \frac{1}{1 + i} \right)^y$$

$$EAC = TNPV \times \frac{i}{1 - (1 + i)^{-d}}$$

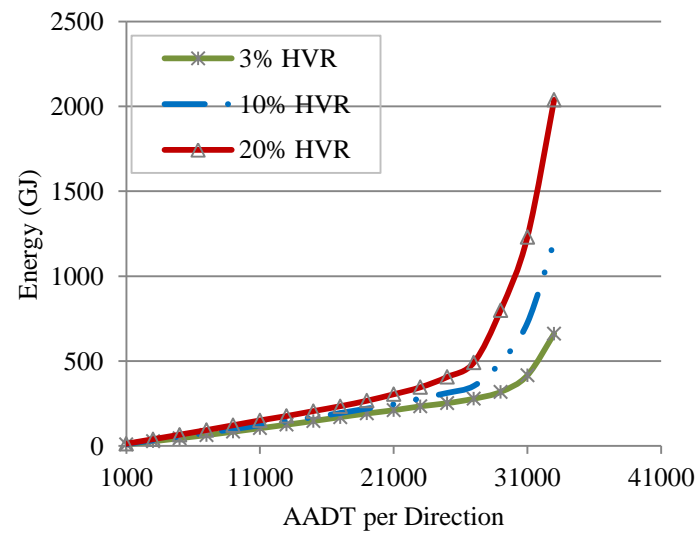
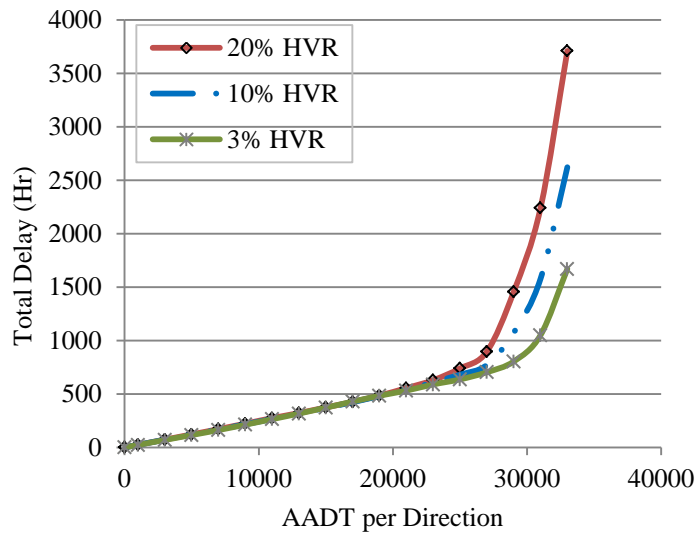
- $y$  : the number years after the construction
- $j_c$  : the yearly crude oil inflation rate
- $j$  : the yearly inflation according to CPI
- $i$  : the rate of interest
- $d$  : the design life of the pavement

- 25 years design life
- Rehabilitation at the 15th year

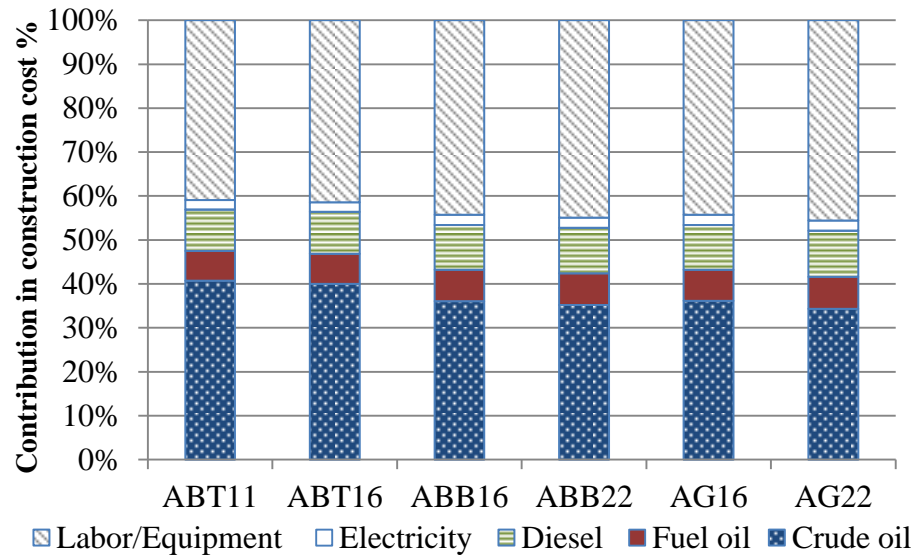
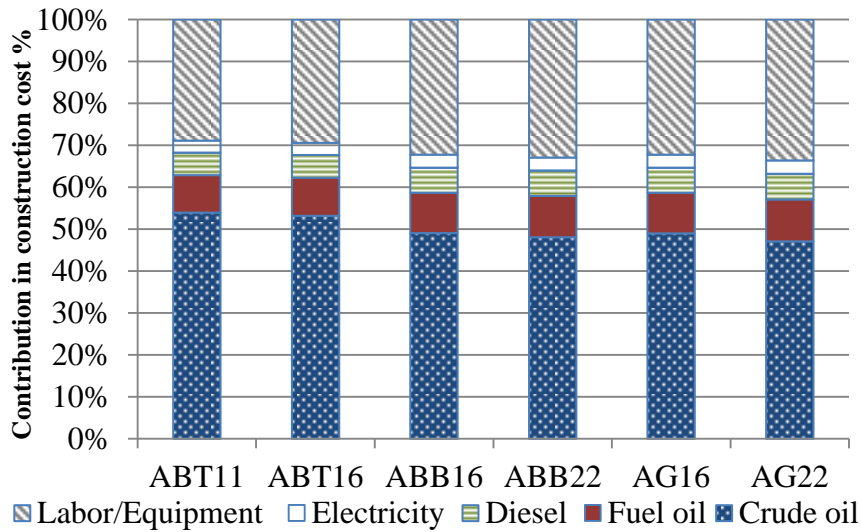


| Transport Material | From_To   | Distance <sup>4</sup><br>(km) |
|--------------------|---|-------------------------------|
| Binder             | Refinery <sup>2</sup> _ Mixing plant <sup>1</sup> | 100                           |
| Aggregate          | Quarry site <sup>1</sup> _ Mixing plant           | 5                             |
| Asphalt            | Mixing plant _ Construction site <sup>3</sup>     | 50                            |

- Microsimulation Models
  - VTI model (AIMSUN 5.1 by Transport Simulation Systems)

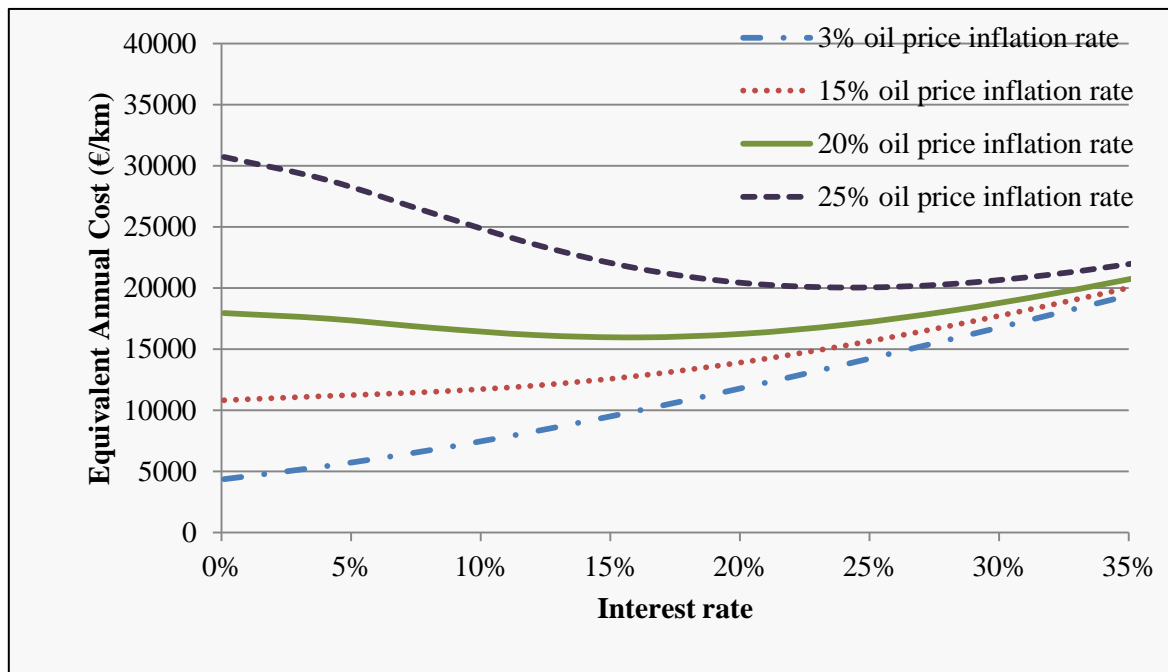


# Contribution of cost drivers



# Discount rate sensitivity analysis

- The general inflation rate for the time related cost was assumed to be 3%
- The average crude oil inflation rate for the last 10 years has been about 20%



- A transparent framework was presented for asphalt pavement LCC by applying energy and time as a basis for calculations which underlined main financial risks pertaining to asphalt paving works
- By applying the energy and time units as basis for cost calculations, the framework imposed separate inflation indices on the energy related costs and the labor/road user related costs
- The framework is capable of reflecting the price trends in the energy sector. Therefore, it can increase the awareness for the future costs related to maintenance and rehabilitation activities



- The prices of different energy sources in Europe during the recent years more or less have followed the fluctuation of the oil price
- Therefore, the crude oil inflation index was chosen as the inflation index for all energy sources
- The country general inflation index was used for the time related items

- The sensitivity analysis regarding the transportation distances showed that the transportation distances has a high impact on the total cost of asphalt pavement
- Therefore, it is believed that the transportation distance is one of the most important factors regarding the high variation in the price of laid asphalt pavements in Sweden

- In Sweden price of oil products are mostly affected by the global economy rather than the national economy
- Despite the price index of oil products which had a high fluctuation in different time periods, the cost fluctuation related to labor and equipment has been steady and followed the CPI
- Therefore, energy and time related costs are in this framework treated with different inflation indices in order to perform a better financial risk assessment regarding the future costs

- The calculated discount rate based on this model for the last 20 years was -4% which means the future costs in this period have been more expensive due to discounting
- Therefore, by assuming the similar pattern for the coming future, it is highly beneficial to minimize future costs
- This can be done by increasing the material quality to have a better performance regarding cracking and rutting in order to require less rehabilitation in the future
- The amount of future user costs regarding energy used by vehicles can also be decreased by using pavements with a lower rolling resistance

**Thank you!**