

Home Work Set 1

Chapter 1 [S. Johnson]

1.26; 1.28

1.26 The encoder for a rate- $1/q$ repetition code repeats each message bit q times. For example, if $q = 2$ then the message $u = [u_1 u_2]$ will be encoded into the codeword $c = [u_1 u_1 u_2 u_2]$. If a codeword from a length $N = 6$, rate- $1/3$, repetition code is transmitted through a BSC and $y = [1 \ 1 \ 0 \ 0 \ 0 \ 1]$ is received, use ML decoding to find the most likely transmitted message, assuming that the message was generated by a binary equiprobable source,

- (a) when $p = 0.1$,
- (b) when $p = 0.4$,
- (c) when $p = 0.6$.

1.28 Repeat Exercise 1.26 but use MAP decoding.

Chapter 4,

4.1, 4.13, 4.17

4.1 The convolutional encoder used in the IS-95 code division multiple access (CDMA) system for mobile phones has the generators 753, 561.

- (a) Determine the code rate and maximum memory order,
- (b) give the generator matrix,
- (c) determine the codeword produced by the message $\mathbf{u}_{(1)} = [1 \ 0 \ 1 \ 1 \ 0]$,
- (d) draw this encoder's block diagram.

4.13 Find the MAP message using BCJR decoding (with probability metrics) for the encoder in Figure 4.3 assuming an equiprobable binary source:

- (a) for an 8-bit terminated codeword sent on the BSC with crossover probability 0.02 when $y = [1 \ 1; 1 \ 1; 0 \ 1; 1 \ 1]$ is received,
- (b) for an 8-bit terminated codeword sent on the BI-AWGN channel with signal-to-noise ratio 5 dB when $y = [1.1 \ 0.9; -0.1 \ 1.1; -1.1 \ 0.9; 1.1 \ 1.1]$ is received, for a biased source with $p(u_i = 1) = 0.4$.

4.17 Write a Matlab program to implement log BCJR decoding.

- (a) Using your program determine the MAP bit probabilities for the unterminated message corresponding to the received vector

$$y = [1 \ 1 \ 1; 1 \ 0 \ 1; 1 \ 1 \ 1; 0 \ 1 \ 0; 0 \ 0 \ 1; 0 \ 1 \ 1]$$

from the convolutional encoder of Figure 4.2. Assume a binary equiprobable source and a BSC with crossover probability 0.2.

- (b) Using your program find the average bit error rate of the IS-95 convolutional code (see Exercise 4.1) operating on a BI-AWGN channel with signal-to-noise ratios of 1 dB and 3 dB for message lengths of 10 bits and 100 bits respectively. Assume an equiprobable binary source.