

## Modern Physics Chapter 1-2. Solutions to exercises.

$$2.1.1 \quad v = s/t = \frac{2\pi R}{T} = \frac{2\pi \times 6.3 \times 10^9}{365 \times 60 \times 60} \text{ m/s} = 30.1 \text{ km/s} \quad \text{Answer: 30 km/s}$$

$$2.4.1 \quad L = L_0 \sqrt{1 - (v/c)^2} = L_0 \sqrt{1 - 0.8^2} = L_0 \sqrt{1 - 0.64} = L_0 \sqrt{0.36} = L_0 0.6 \quad \text{Answer: } 0.6L_0$$

$$2.6.1 \quad m = m_0 / \sqrt{1 - (v/c)^2} = m_0 / \sqrt{1 - 0.6^2} = m_0 / \sqrt{0.64} = m_0 / 0.8 = 1.25m_0 \quad \text{Answer: } 1.25 m_0.$$

$$2.7.1 \quad \text{Relativistic Doppler: } f = f_0 \sqrt{\frac{1 - v/c}{1 + v/c}} \quad \text{Med } c = f\lambda \quad \text{fås } \frac{\lambda}{\lambda_0} = \sqrt{\frac{1 - \beta}{1 + \beta}} \quad \text{where } \beta = v/c$$

We insert the wavelengths 500nm och 600nm and square the expression

$$\frac{25}{36} = \frac{1 - \beta}{1 + \beta} \Rightarrow \frac{25}{36} = \frac{1 - \beta}{1 + \beta} \times \frac{1 - \beta}{1 - \beta} \Rightarrow \frac{25}{36} = \frac{1 - 2\beta + \beta^2}{1 - \beta^2} \approx \frac{1 - 2\beta}{1} \quad \text{where we neglect } \beta^2 \text{ that has become small. We get}$$

$$2\beta = 1 - \frac{25}{36} \Rightarrow \beta = \frac{1}{8} \quad \text{why } v = 0.8c \quad \text{Answer: } v = 0.8c$$

$$2.8.1 \quad \frac{F_E}{F_G} = \frac{ke^2}{r^2} / \frac{Gm^2}{r^2} = \frac{ke^2}{Gm^2} = \frac{9.0 \times 10^9 (1.6 \times 10^{-19})^2}{6.67 \times 10^{-11} (9.1 \times 10^{-31})^2} = 4.17 \times 10^{42} \quad \text{Answer: } 4.2 \times 10^{42}$$

$$2.8.2 \quad F_B = evB \text{ magnetic force, } F_C = mv^2/R \text{ Centripetal force. At equilibrium}$$
$$B = mv/eR = 9.1 \times 10^{-31} \times 3 \times 10^6 / (1.6 \times 10^{-19} \times 5 \times 10^{-2}) \text{ T} = 3.4 \times 10^{-4} \text{ T}$$

Answer:  $3.4 \times 10^{-4} \text{ T}$

$$2.8.3 \quad \text{The same derivation } B = mv/eR = 1.67 \times 10^{-27} \times 3 \times 10^6 / (1.6 \times 10^{-19} \times 5 \times 10^{-2}) \text{ T} = 0.62 \text{ T}$$

Answer:  $0.62 \text{ T}$