

Modern physics Chapter 5-6. Solutions to exercises.

$$5.3.1 \quad v_p = \sqrt{\frac{2kT}{m}} = \sqrt{\frac{2 \times 1.3805 \times 10^{-23} (273 + 20)}{2 \times 14 \times 1.67 \times 10^{-27}}} m/s = 416 m/s \approx 420 m/s$$

$$5.3.2 \quad \text{Mean velocity } \bar{v} = \sqrt{\frac{8kT}{\pi m}} = \frac{2}{\sqrt{\pi}} v_p = \frac{2}{\sqrt{\pi}} 416 m/s \approx 470 m/s$$

$$5.3.3 \quad \text{RMS-velocity } v_{RMS} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3}{2}} v_p = \sqrt{\frac{3}{2}} 416 m/s \approx 510 m/s$$

$$5.3.4 \quad \text{Wien's law } \lambda_{\max} = \frac{2.898 \times 10^{-3}}{T} \quad \text{gives the temperature } T = \frac{2.898 \times 10^{-3}}{730 \times 10^{-9}} K \approx 3970 K$$

5.3.5 The emission at 300K is $e(300) = e_0$. The emission at 400K is looked for.

$$e = \sigma T^4 \quad \text{gives } e(400) = e_0 \left(\frac{400}{300} \right)^4 = 3.160 e_0 \approx 3.2 e_0$$

6.1.1 $n = 2$ gives $l = 0, 1$

For $l = 0$ the possible quantum number is $m_l = 0$

For $l = 1$ the possible quantum numbers are $m_l = -1, 0, 1$

$$6.1.2 \quad \text{The energy levels are } E_n = -\frac{me^4}{8\epsilon_0^2 h^2} \left(\frac{1}{n^2} \right) = -13.6 \left(\frac{1}{n^2} \right) eV$$

$$E_2 = -13.6 \left(\frac{1}{2^2} \right) eV = -3.4 eV = 5.4 \times 10^{-19} J$$