



SF1649 Vector Analysis and Complex Functions 7.5 credits

Vektoranalys och komplexa funktioner

This is a translation of the Swedish, legally binding, course syllabus.

Establishment

Course syllabus for SF1649 valid from Autumn 2008

Grading scale

A, B, C, D, E, FX, F

Education cycle

First cycle

Main field of study

Mathematics, Technology

Specific prerequisites

SF1624 Algebra och Geometri, SF1625 Envariabelanalys, SF1626 Flervariabelanalys.

Language of instruction

The language of instruction is specified in the course offering information in the course catalogue.

Intended learning outcomes

After the course the student should

Vector analysis

- be able to distinguish between different kinds of fields in mathematical physics: scalar field, vector field and tensor field.
- be able to explain the meaning of, and compute, divergence and curl of a vector fields, gradient of a scalar fields.
- be able to make vector analytic calculations by using the nabla operator.
- be able to compute flux integrals over (in general curved) surfaces in space, given in parametric or implicit form.
- be able to state and explain the meaning of Gauss' theorem and be able to use it in calculation of flux integrals.
- be able to compute line integrals and tell when they are independent of the path.
- be able to state and explain the meaning of Stokes' theorem and be able to use it in calculation of line integrals.
- be able to decide whether a given vector field has a scalar potential or not, and be able to compute it when it exists.
- be able to decide whether a given vector field has a vector potential or not, and in simple cases be able to compute it.
- be able to perform vector analytic calculations, not only in cartesian coordinates but also in curvilinear orthogonal coordinates (in particular cylindrical and spherical coordinates)
- describe how the Laplace and Poisson equations arise in mathematical physics and be able to solve them in simple cases.

Complex analysis

- have a good skill in calculation with complex numbers, in cartesian or polar form, in simple cases be able to interpret relations between complex numbers geometrically and in particular be able to determine reflection points with respect to straight lines and circles.
- know what is meant by an analytic function and be able to decide whether a given function is analytic or not, e.g. by checking Cauchy-Riemann's equations.
- know what is meant by a harmonic function and, to a given harmonic function, be able to find a conjugate harmonic function.
- have good working knowledge of the elementary analytic functions, e.g., be able to define them, compute their derivatives, discuss possible multivaluedness and choose natural domains of definition.
- know what is meant by a Möbius transformation and be able to decide how a given Möbius transformation maps a given circular region or half plane.
- be able to find out, in simple cases, how also other elementary functions map given domains and, conversely, find an analytic functions which performs a conformal map between two prescribed regions.
- be able to solve certain boundary value problems for Laplace's equation by mapping conformally onto regions (e.g., half planes or circular discs) for which explicit methods are available.

Course contents

Line integrals, surface integrals, flux integrals, divergence and curl. Gauss' and Stokes' theorems. Nabla calculus, curvilinear coordinates. Potential theory. Analytic function, conformal map, Laplace's and Poisson's equations, the Dirichlet and Neumann problems.

Course literature

P.C. Matthews, Vector Calculus, Springer (1998).
Exempelsamling i A. Ramgard, Vektoranalys, 3:e upplagen
Olle Stormark: Komplexa funktioner.

Examination

- TEN1 - Examination, 7.5 credits, grading scale: A, B, C, D, E, FX, F

Based on recommendation from KTH's coordinator for disabilities, the examiner will decide how to adapt an examination for students with documented disability.

The examiner may apply another examination format when re-examining individual students.

If the course is discontinued, students may request to be examined during the following two academic years.

Other requirements for final grade

Written examination, possibly combined with continuous examination.

Ethical approach

- All members of a group are responsible for the group's work.
- In any assessment, every student shall honestly disclose any help received and sources used.
- In an oral assessment, every student shall be able to present and answer questions about the entire assignment and solution.